

Project 2: Fronts and temperature

Data class- atmosphere

1. Thermal wind and atmospheric fronts

- Margules equation for a real atmospheric fronts

2. Transport (advection) in the atmosphere:

- Example: transport of Saharan dust over the ocean

Next class:

2. Temperature Advection:

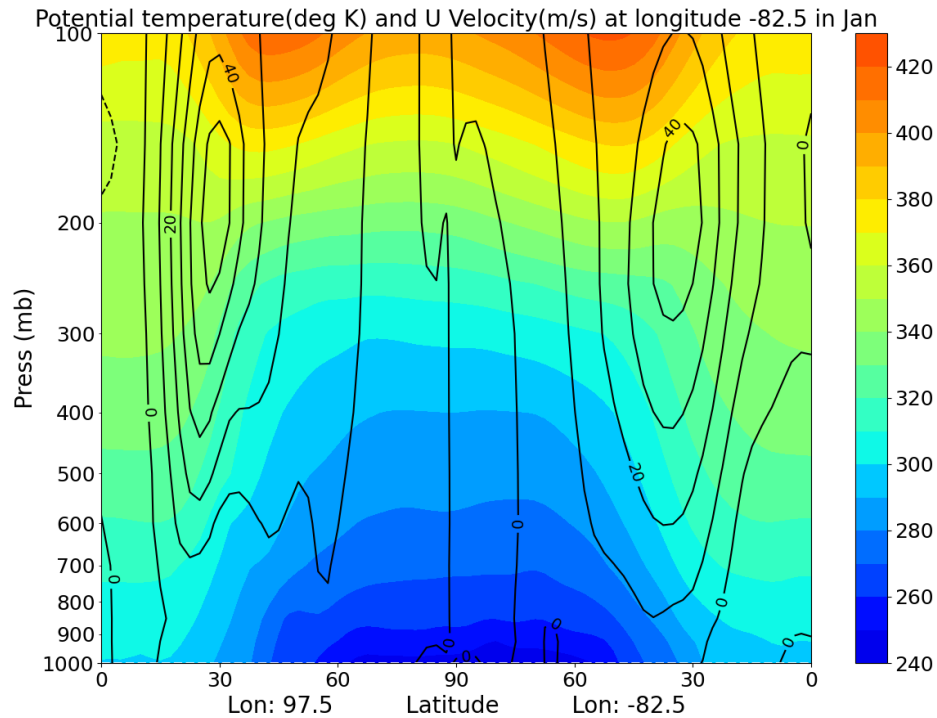
- Temperature change in a real front during winter

3. Temperature variability in current and future climate

- Temperature variations in the atmosphere
- Temperature variability in current and future climate (analyze state-of-the-art climate model data!)

Thermal wind

In terms of potential temperature- $f \left(\frac{\partial u_g}{\partial p}, \frac{\partial v_g}{\partial p} \right) = \frac{1}{\rho \theta} \left(\left(\frac{\partial \theta}{\partial y} \right)_p, - \left(\frac{\partial \theta}{\partial x} \right)_p \right)$





Fronts and the
Margules equation

HIGH

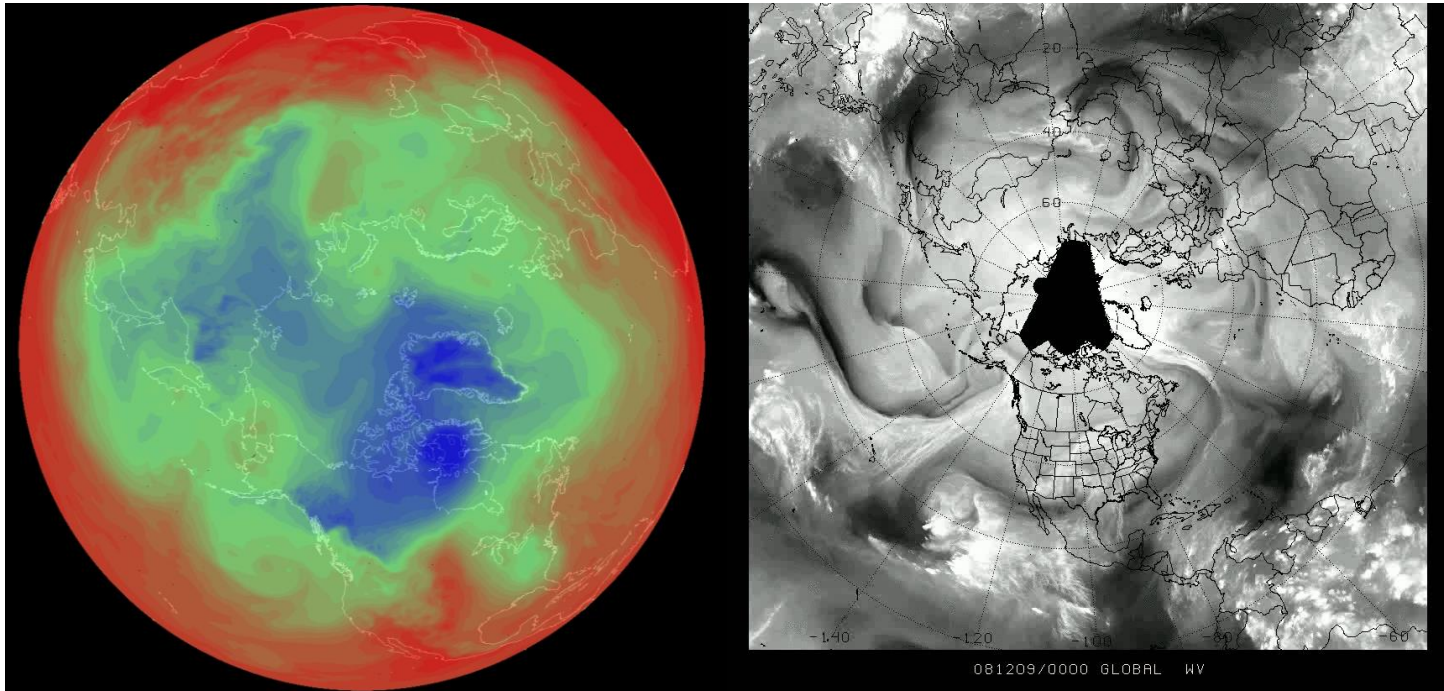
576

576

LOW

The Polar Front

The air mass over the pole is considerably colder (and dryer) than that over the equator

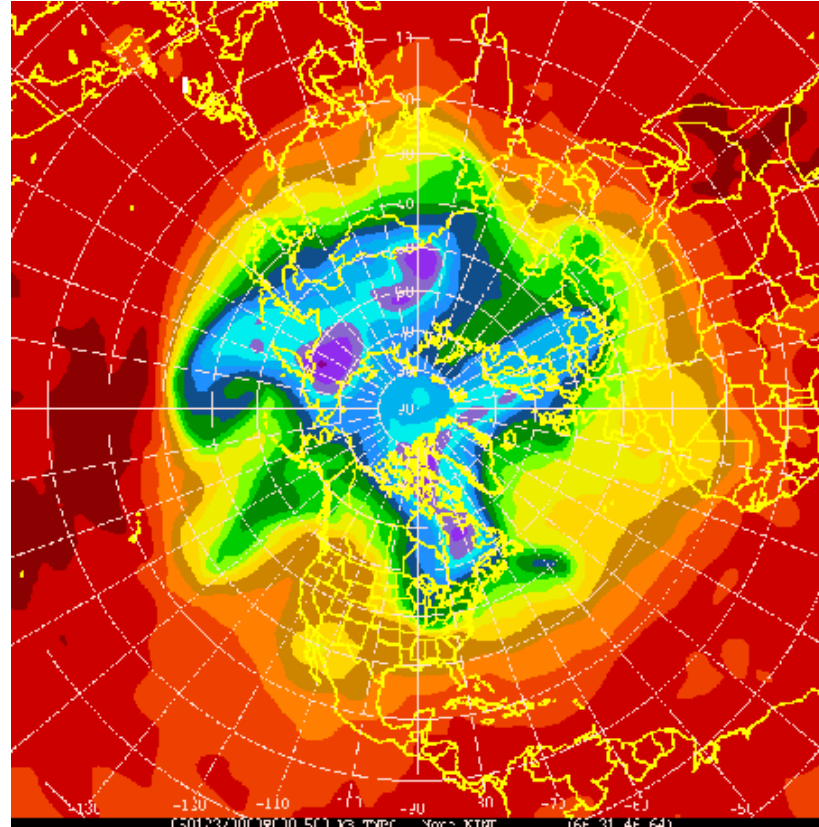


- The most active weather occurs in middle latitudes where the two air masses meet.
- The transition from cold to warm is not smooth, but occurs quite abruptly in a region of high gradients, known as the *polar front*.
- Much of our day-to-day weather is associated with the evolution of this frontal region

Synoptic fronts and weather systems

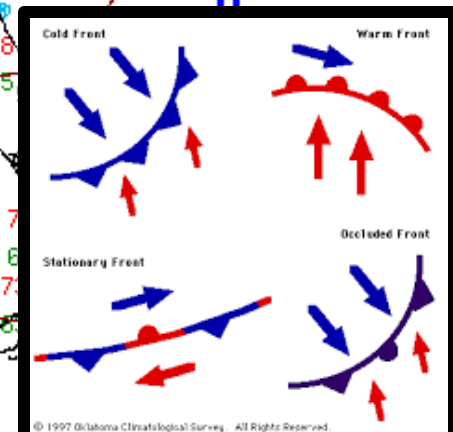
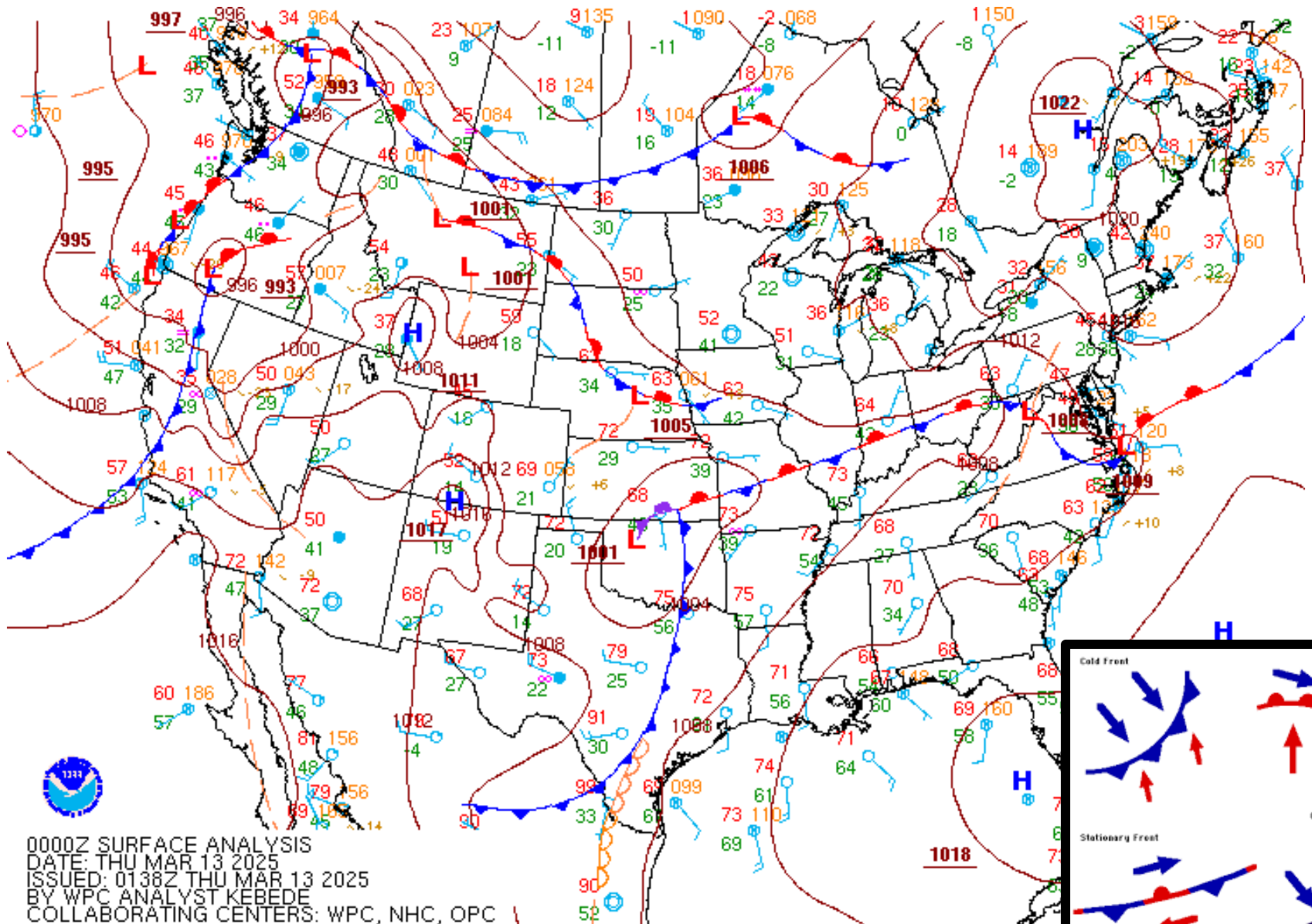
Northern Hemisphere 500 mb temperature on January 23, 2005 0z

Note the north-south undulations of the polar front, marked by the transition from orange to green color



- Everyday weather is often associated with undulations of this frontal surface
- Meanders of the frontal region are associated with high and low pressure synoptic systems which develop on the polar front

Synoptic fronts and weather systems



Synoptic fronts and weather systems

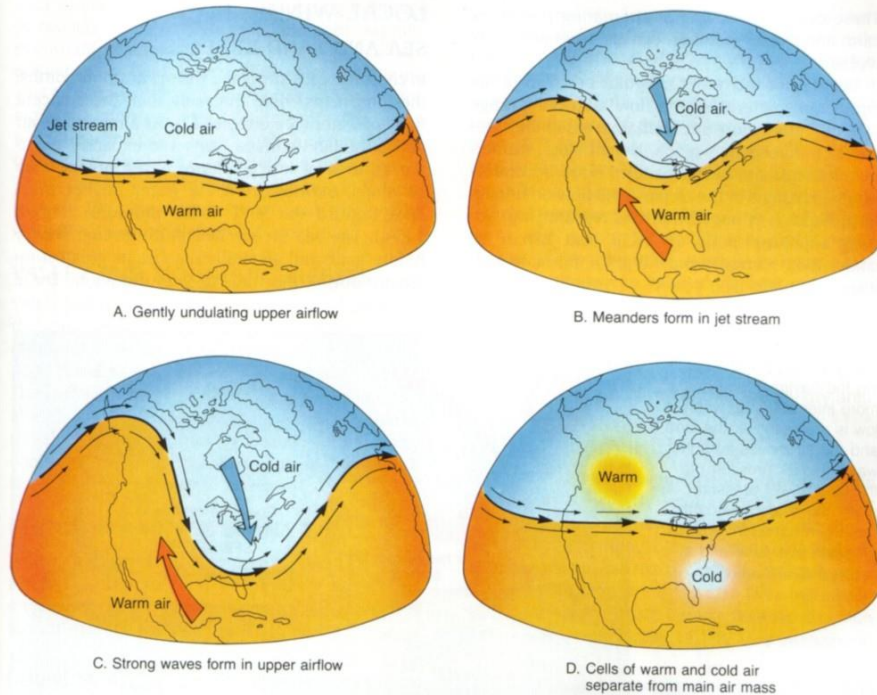


FIGURE 14.13
Cyclic changes that occur in the upper-level airflow of the westerlies. The flow, which has the jet stream as its axis, starts out nearly straight, then develops meanders, which are eventually cut off. (After J. Namias, NOAA)

As storms grow, they bring warm air poleward (and upward), and cold air equatorward (and downward)

Synoptic fronts and weather systems

The surface manifestations of these systems are warm and cold fronts

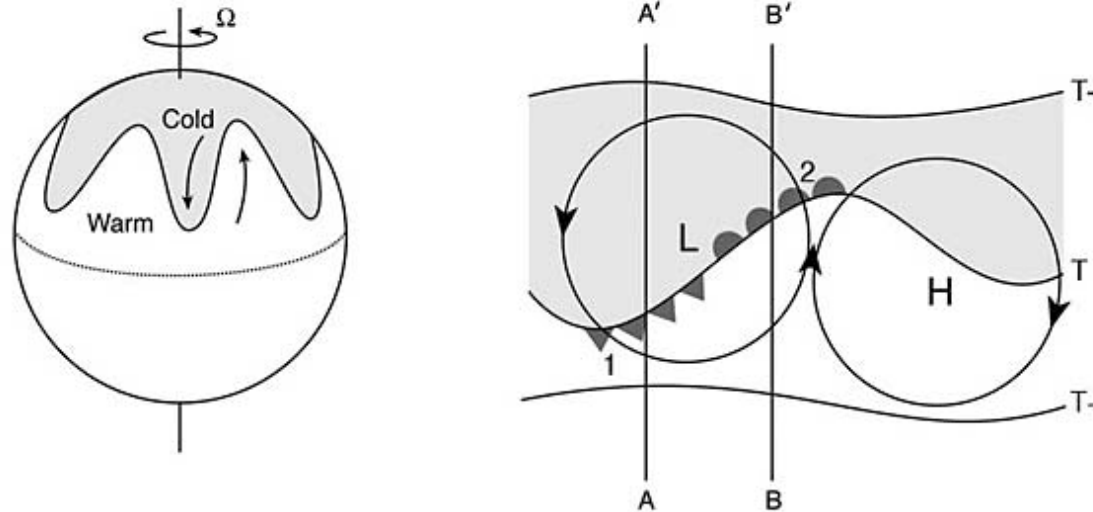


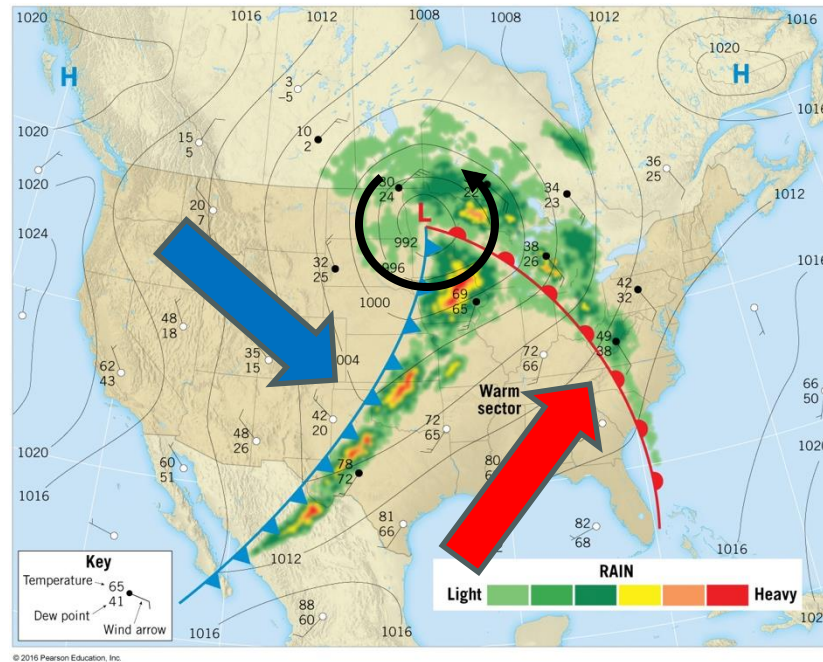
Figure 2: (left) In mid-latitudes, eddies form along the polar front and transport warm air poleward and cold air equatorward. (right) To the west of the 'L', or low pressure, cold air is carried to the tropics. To the east, warm air is carried toward the pole. The resulting cold front (triangles) and warm front (semicircles) are marked. The sections A-A' and B-B' through the fronts are sketched in Fig.6 below.

- In mid-latitudes, eddies form along the polar front (left) and transport warm air poleward and cold air equatorward. (right)
- To the west of the 'L' (low pressure), cold air is carried to the tropics. To the east, warm air is carried toward the pole. The resulting cold front (triangles) and warm front (semicircles) are marked.

Synoptic fronts and weather systems

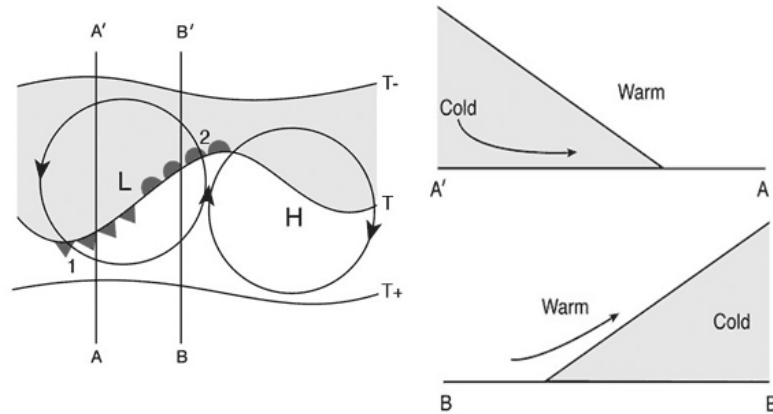
Synoptic scale fronts are associated with cyclones development

A **front** is a boundary separating two air masses with different temperatures



- As the **cold** air moves southward, where the air is warmer, the **cold front** develops. The cold air is lifting the warm and moist air and hence precipitation is formed
- As the **warm** air moves poleward, where the air is colder, the **warm front** develops. The warm and moist air travels above the cold air, and again precipitation is formed

Synoptic fronts and weather systems



potential
temperature
and wind

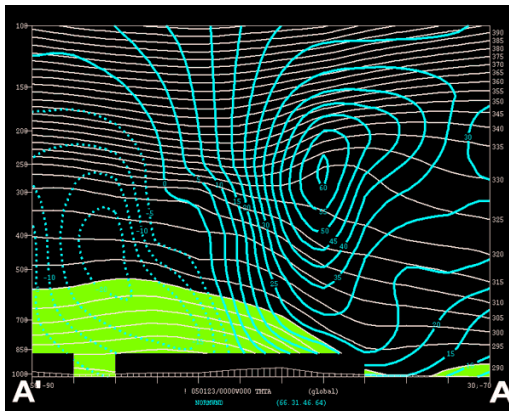


Figure 3: A similar section across the cold front as marked by the A'A line in the schematic diagram below.

*The region of cold air
is shaded in green*

**Thermal
wind!**

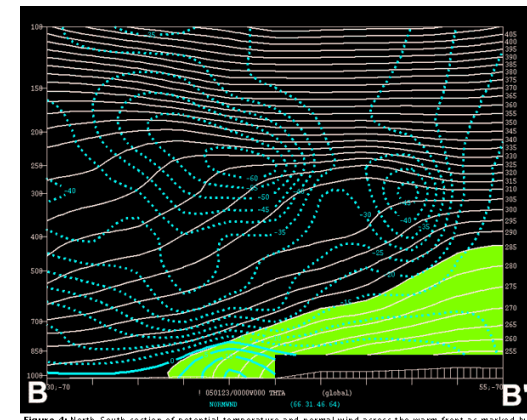


Figure 4: North-South section of potential temperature and normal wind across the warm front as marked by the B'B line in the schematic diagram at the bottom of the page. The region of cold air is shaded in green.

A section across the **cold front** as marked by the A'A line in the schematic diagram

A section across the **warm front** as marked by the B'B line in the schematic diagram

- Cold air wedges underneath warm air in the cold front, while warm air overrides cold air in the warm front
- In both cases, warm, moist air rises, cools and condenses, forming clouds & precipitation along the fronts
- Because the cold fronts are usually stronger than the warm fronts, the precipitation associated with the passage of a cold front is usually heavier than in a warm front

Cold fronts

- Produce strong convection and heavy precipitation at the boundary
- Are vertically steep
- Often produces cumulonimbus towers
- Move relatively fast

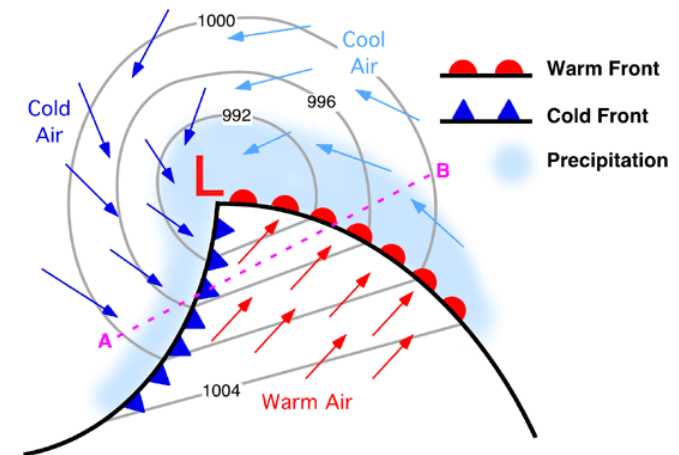
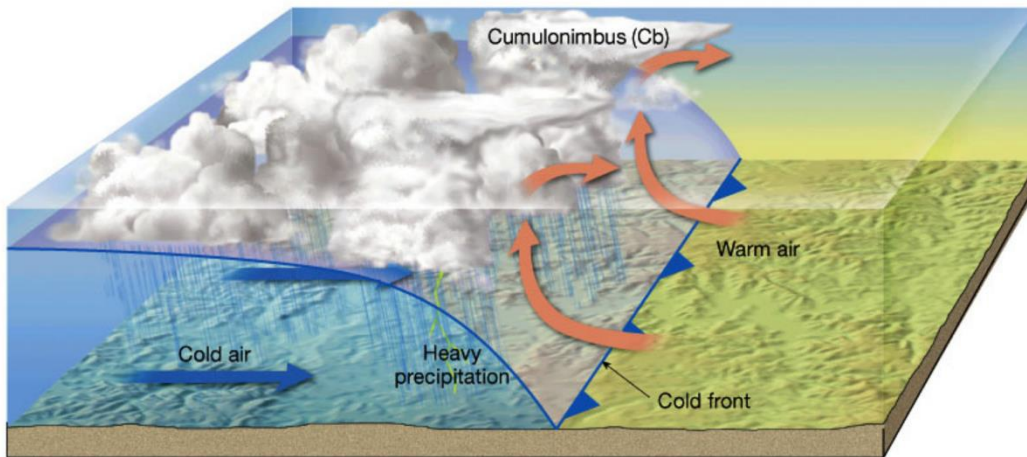


Figure 9.6 in *The Atmosphere, 8th edition*, Lutgens and Tarbuck, 8th edition, 2001.

Warm fronts

- Are braider in shape, more “wedge” shaped
- Precipitation is more moderate but can spread out more
- Various clouds at varying altitudes
- Moves relatively slower compared to the cold front

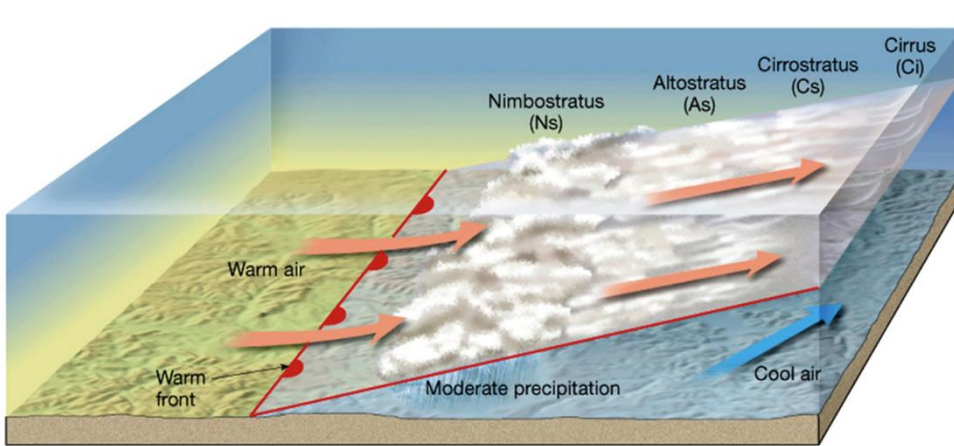
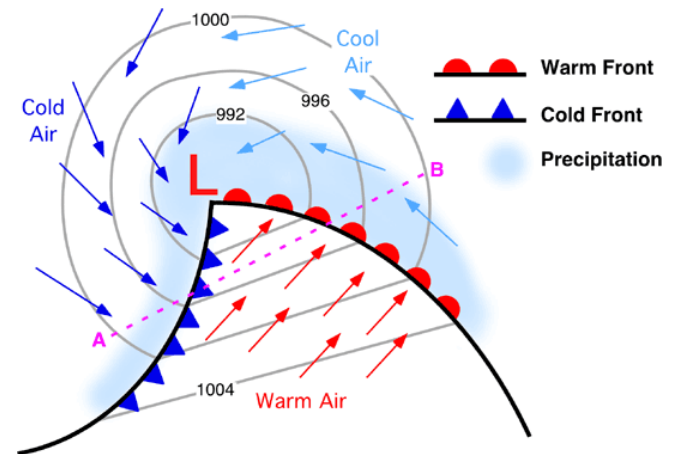


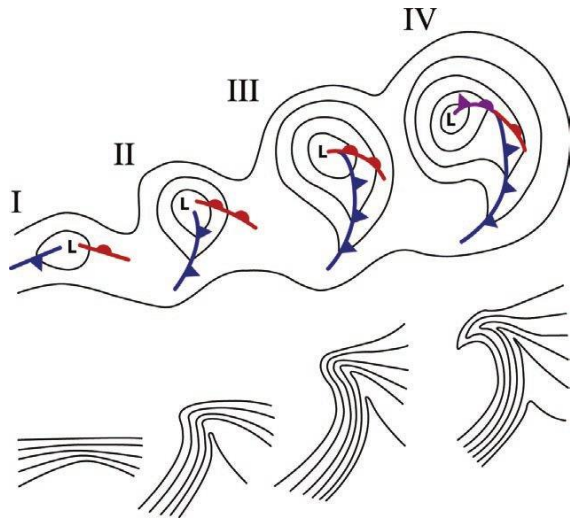
Figure 9.6 in *The Atmosphere, 8th edition*, Lutgens and Tarbuck, 8th edition, 2001.



Conceptual cyclone life cycle models

Norwegian cyclone model

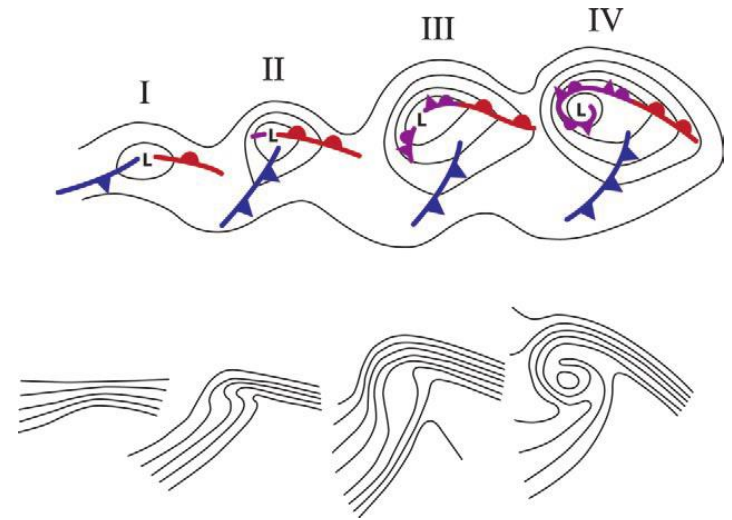
beginning of the last century



adapted from Schultz et al. (1998)

Shapiro-Keyser cyclone model

developed in the late 1980s,



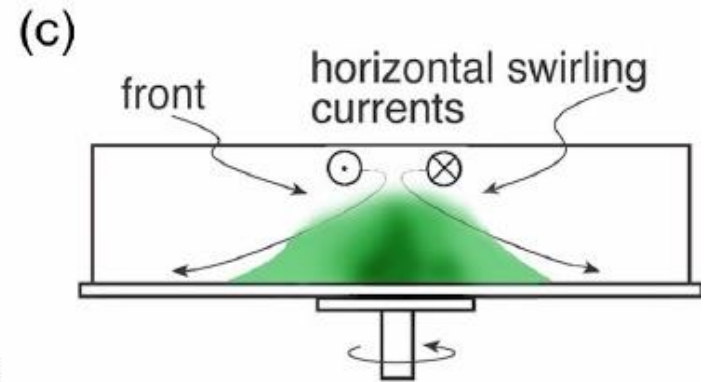
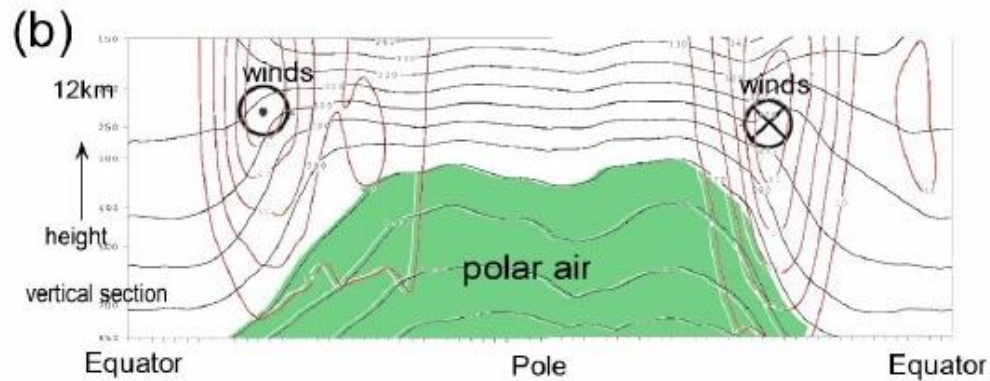
adapted from Shapiro and Keyser (1990)

(top) Lower-tropospheric geopotential height and fronts, and (bottom) lower tropospheric temperature. The stages in the respective cyclone evolutions are separated by approximately 6–24 h and the frontal symbols are conventional.

- By the end of the cyclone life, the cold front, moving faster than the warm front, "catches up" with the warm front, and an occluded front forms.
- In the Norwegian model, the cyclone remains "cold core" during the final occlusion
- In Shapiro-Keyser case, there is no occlusion during the mature stage, but instead warm seclusion and a typical T-bone pattern

Atmosphere vs lab: Fronts and Thermal wind

A tank experiment to illustrate the Polar Front and the Jet Stream

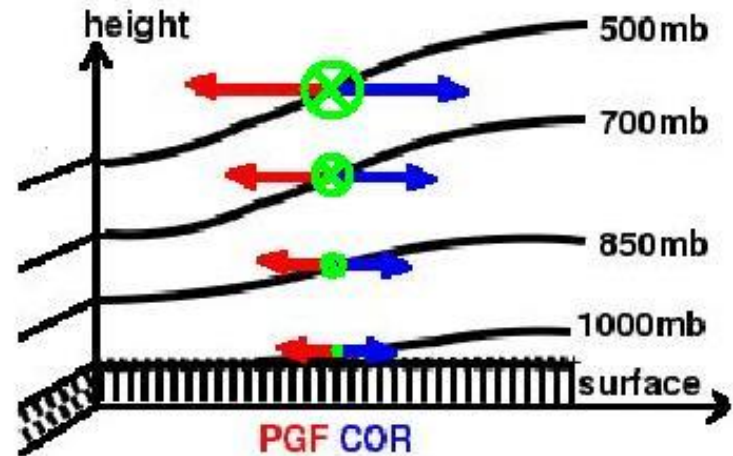
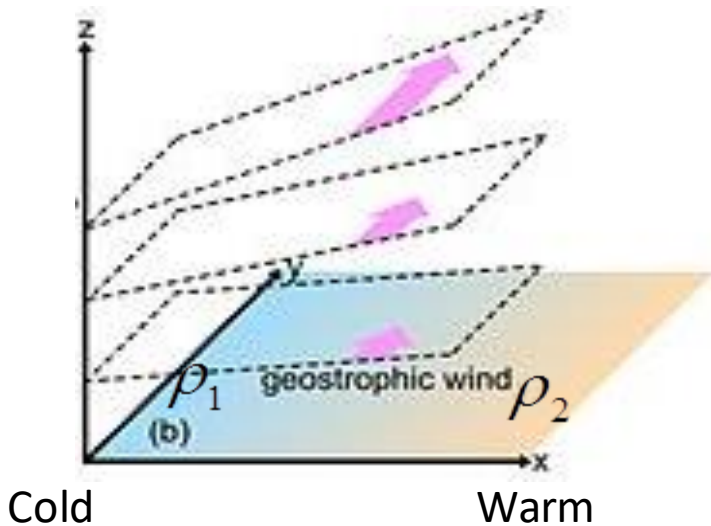


Atmosphere: fronts due to temperature difference

Lab: front due to a density difference

Thermal wind balance can be written in terms of density gradient as well

Fronts and Thermal wind

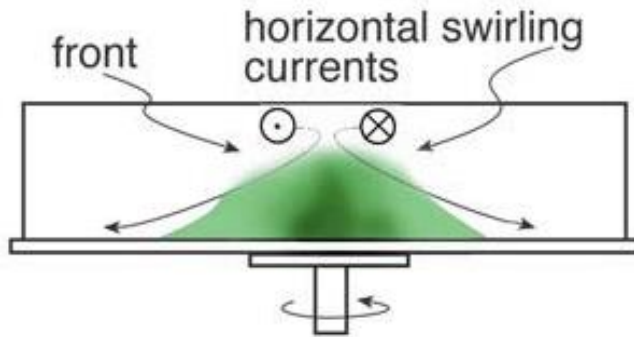


$$\frac{du}{dz} = \frac{g}{\rho_0 f} \frac{d\rho}{dy}$$

$$\frac{\partial u}{\partial p} = \frac{R}{f p} \left(\frac{\partial T}{\partial y} \right)_p$$

Vertical wind shear is proportional to the horizontal density (or temperature) gradient

The Margules relation- lab



The Margules equation:

$$\tan \gamma = \frac{f(u_2 - u_1)}{g\left(\frac{\rho_1 - \rho_2}{\rho_1}\right)}$$

Where ρ_1 is the denser fluid ($\rho_1 > \rho_2$)
and $u_2 > u_1$

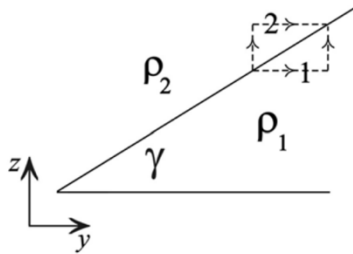


Figure 7.17: Geometry of the front separating fluid of differing densities used in the derivation of Margules relation, Eq.(7.21).

For rotation rates of ~ 10 rpm, a relative density of $\sim 2\%$, and a swirl speed of about $6 \frac{cm}{sec}$, the Margules equation predicts $\gamma \sim 30^\circ$

The Margules relation- polar front

Polar front

The Margules equation:

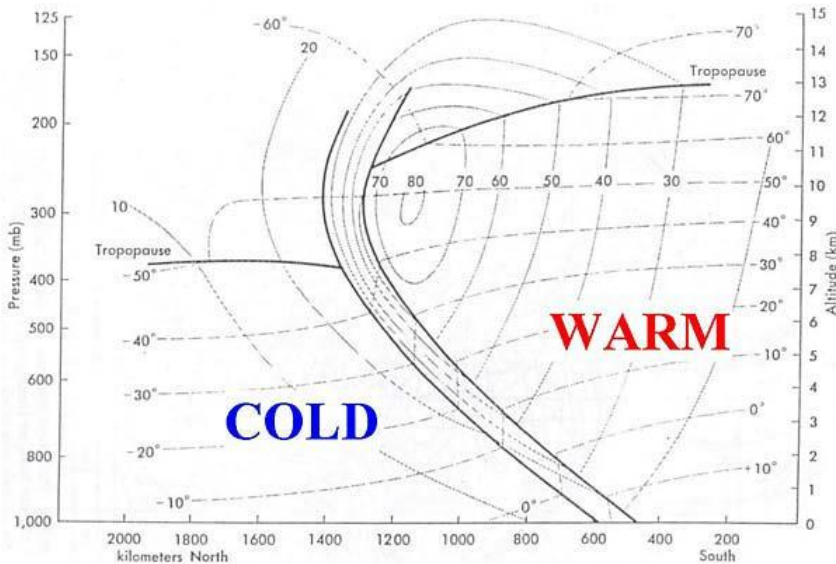


Figure 5: Schematic vertical north-south cross section in the Northern Hemisphere through the polar front, denoted by the heavy lines. Note that north is to the left in this schematic, whereas it is to the right in previous figures. Dotted isobars marked every 10 ms⁻¹ (from 10 to 80 ms⁻¹) show the jet in thermal wind balance with the temperature field. Dashed lines are isotherms marked every 10°C (from 10 to -70°C). (from E. Palmén and C. W. Newton, *Atmospheric Circulation Systems*, Academic Press, New York, 1969)

$$\tan \gamma = \frac{f(u_2 - u_1)}{g\left(\frac{T_2 - T_1}{\bar{T}}\right)}$$

A similar slope can be calculated for the atmospheric front!

The Margules relation- polar front

Polar front

The Margules equation:

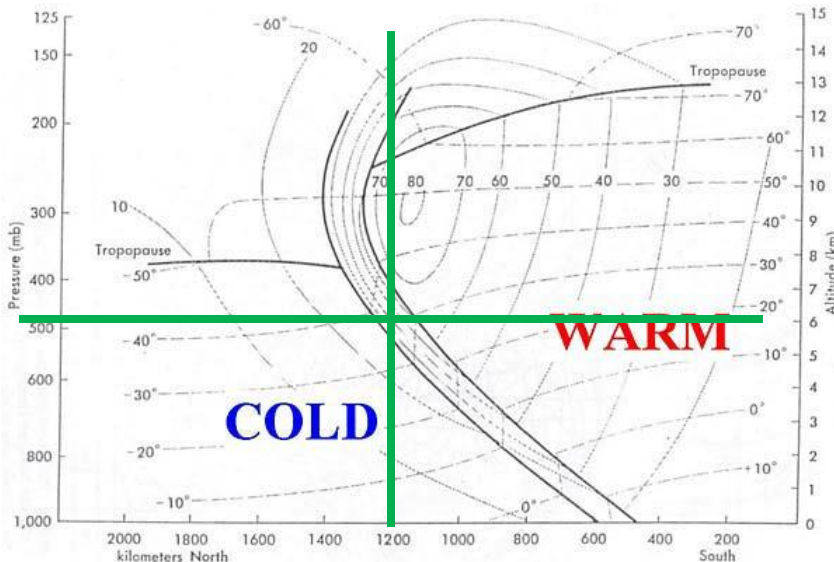


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What are typical values of this angle?

Horizontal length scales in the atmosphere are much larger than the vertical!

$$\tan \gamma = \frac{f(u_2 - u_1)}{g\left(\frac{T_2 - T_1}{\bar{T}}\right)}$$

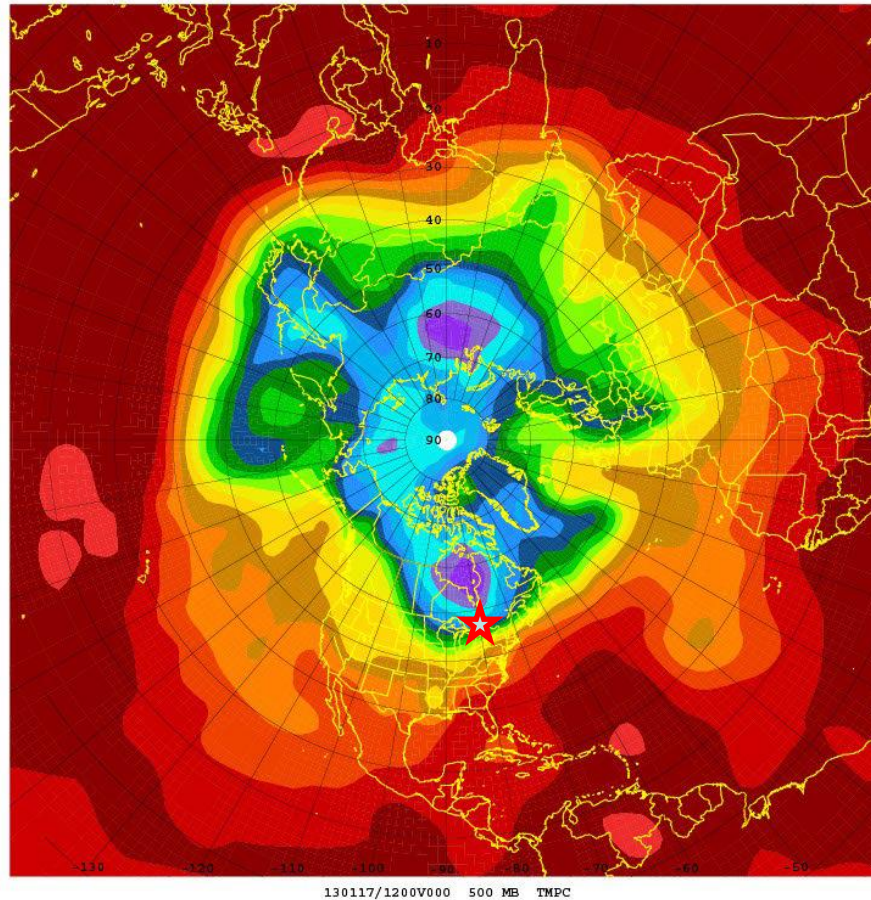
$$Z_{500} \approx 5.5 \text{ km}$$

$$\Delta y \approx 700 \text{ km}$$

$$\tan \gamma \approx \frac{5.5}{700} \rightarrow \gamma \approx 0.45^\circ$$

The Margules relation- polar front

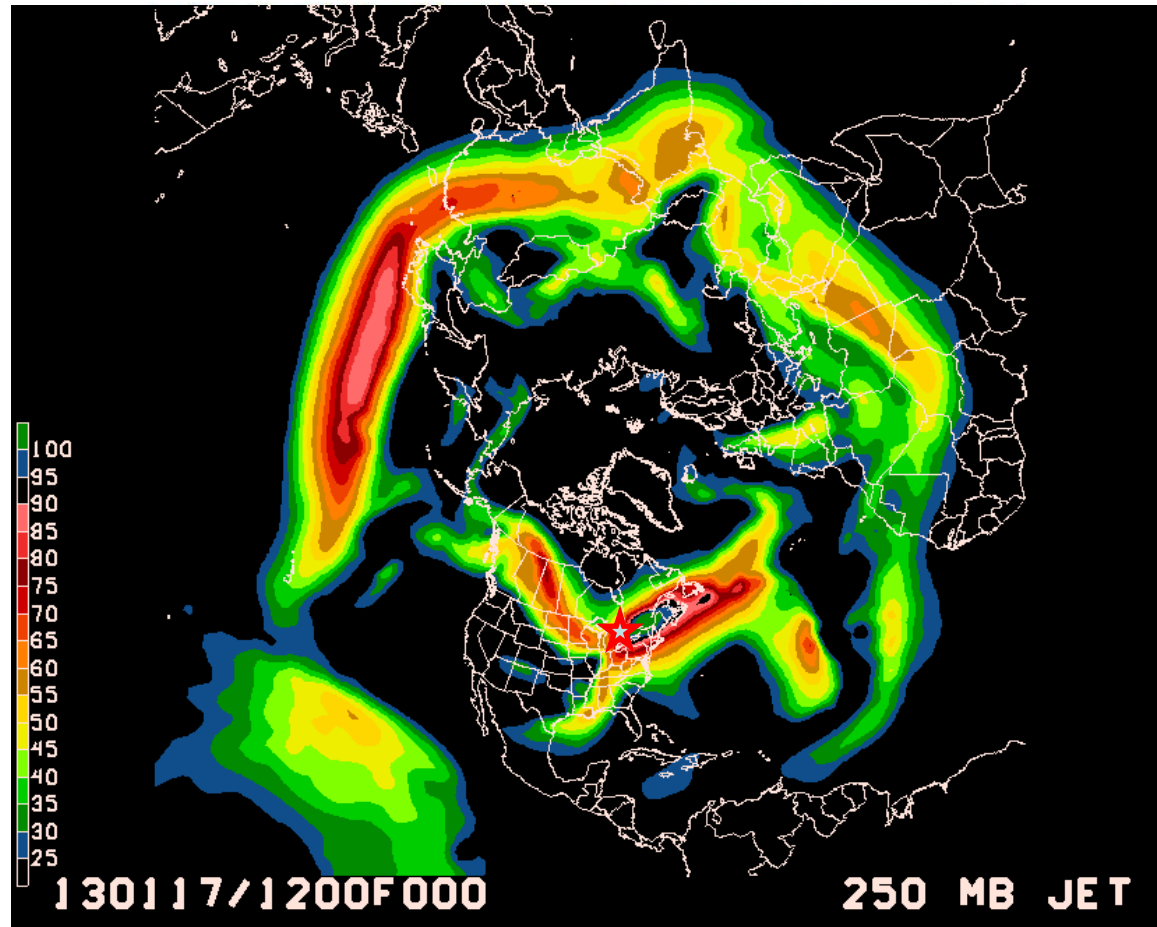
Let's examine a case study of a front that occurred on Jan 17th 2013, and make an analogy to the Front experiment we performed in class:



Jan 17th 2013

The Margules relation- polar front

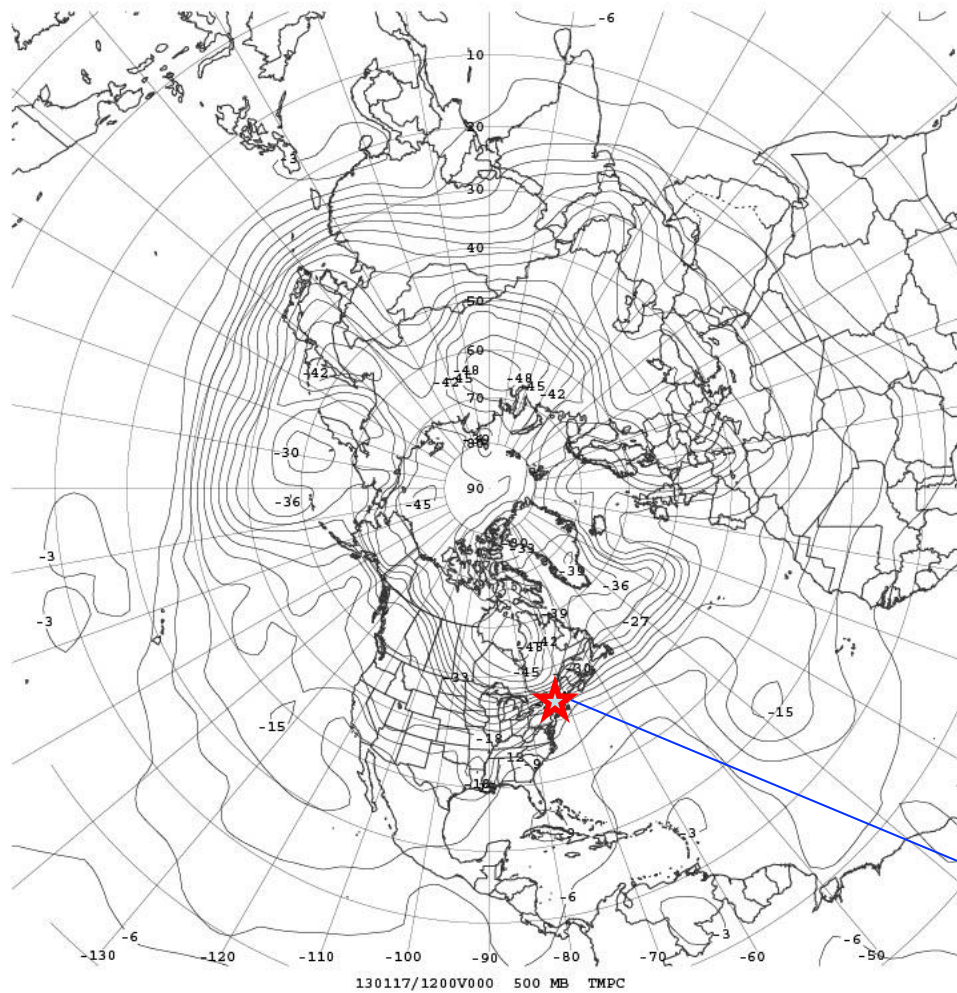
Let's examine a case study of a front that occurred on Jan 17th 2013, and make an analogy to the Front experiment we performed in class:



Jan 17th 2013

Temperature contours

*Temperature (C) at
500 mb over the
northern hemisphere
on the 17th of
January, 2013 12Z*



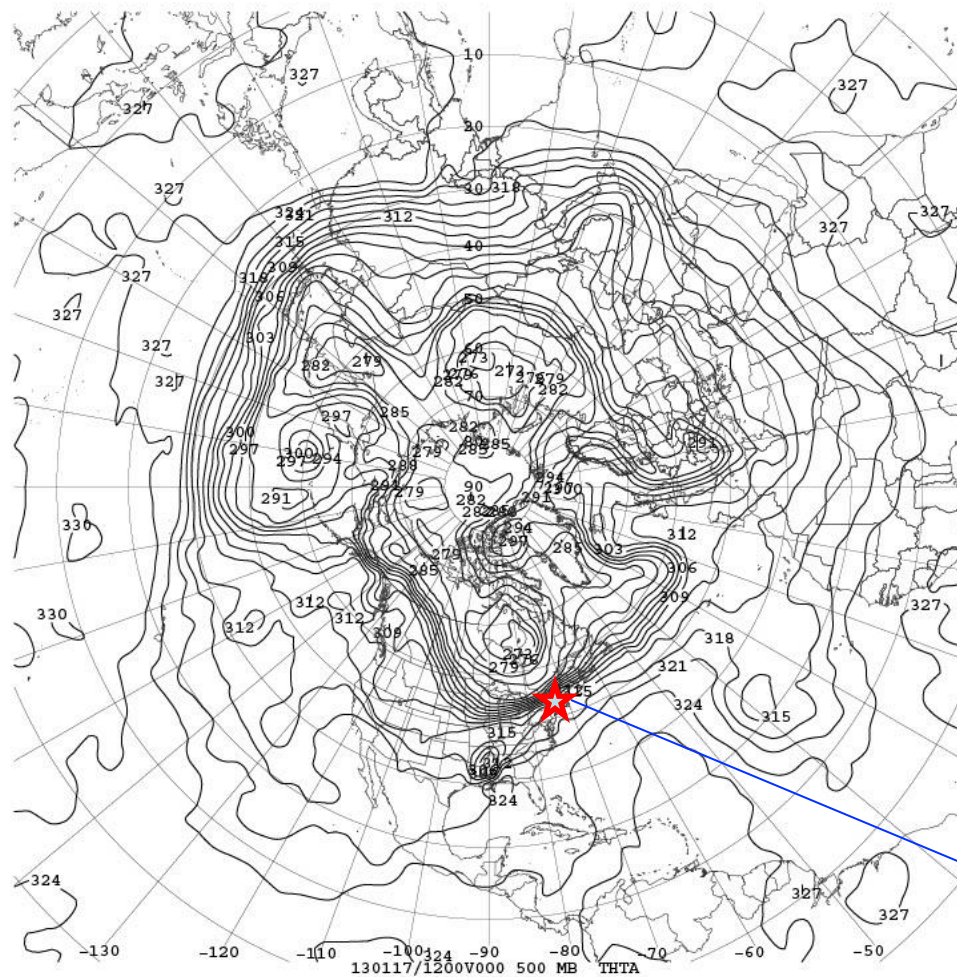
A front!

*Sharp temperature
change*

Jan 17th 2013

Potential temperature contours

*Potential temperature
(C) at 500 mb over
the northern
hemisphere on the
17th of January,
2013 12Z*



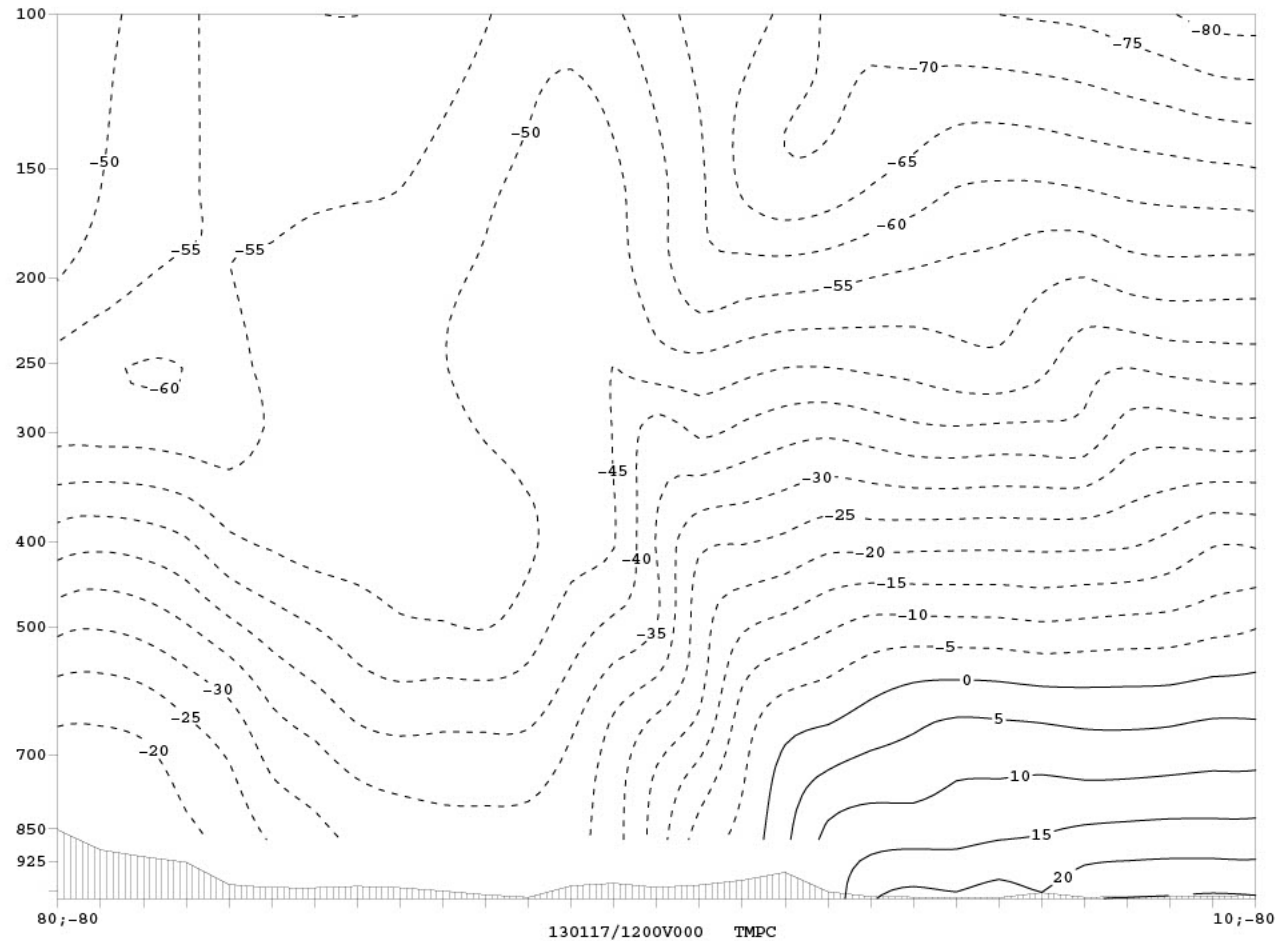
A front!

*Even clearer in potential
temperature field*

Jan 17th 2013

Temperature- vertical cross section

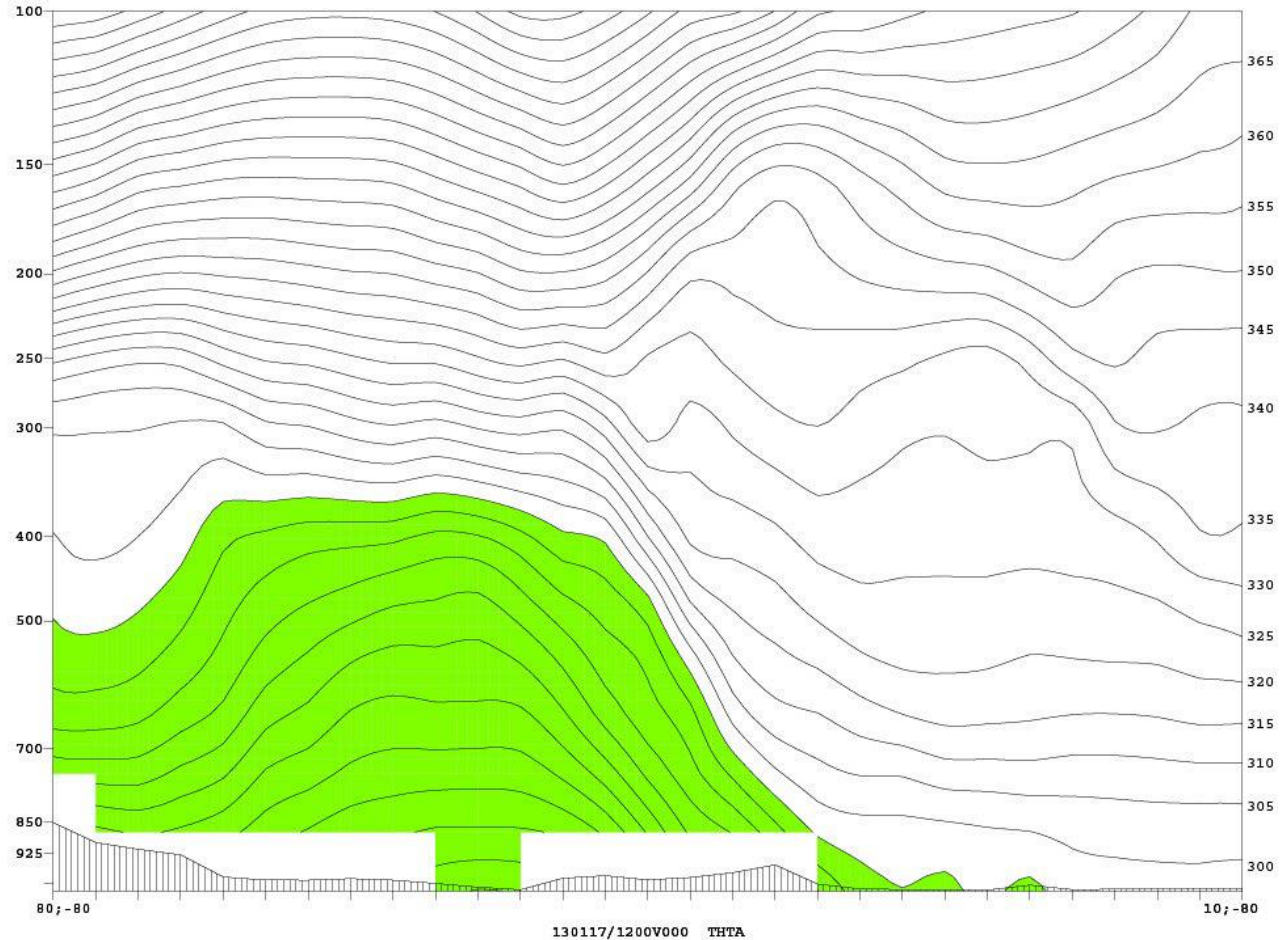
A north-south
vertical section of
temperature
along the 80W
longitude



Jan 17th 2013

Potential temperature- vertical cross section

A north-south
vertical section of
potential
temperature
along the 80W
longitude

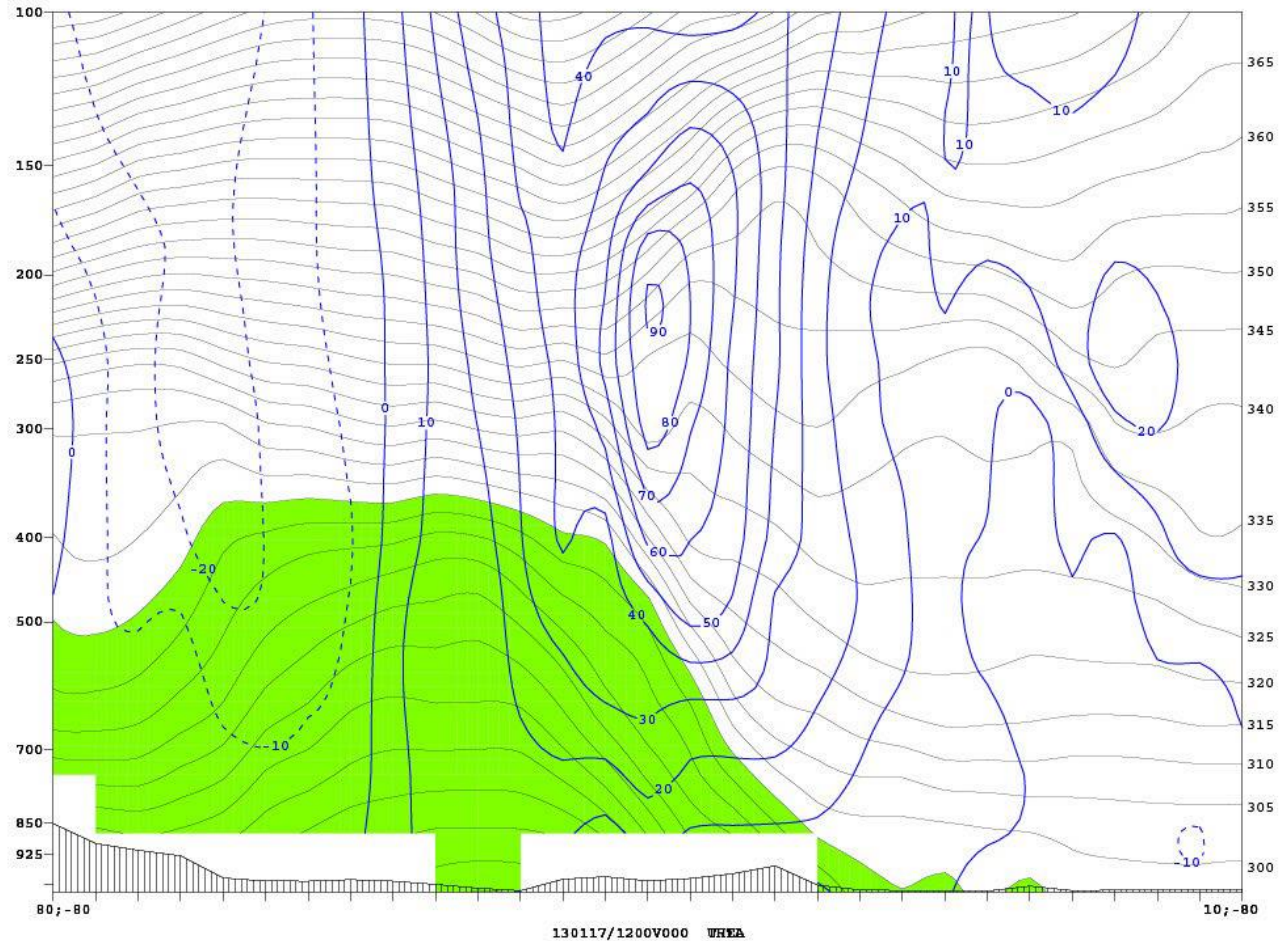


The frontal zone between the cold and warm air has been marked by shading in green air with temperature below 295 K

Jan 17th 2013

Potential temperature & U- vertical cross section

A north-south
vertical section of
potential
temperature
along the 80W
longitude



The frontal zone between the cold and warm air has been marked by shading in green air with temperature below 295 K

Jan 17th 2013

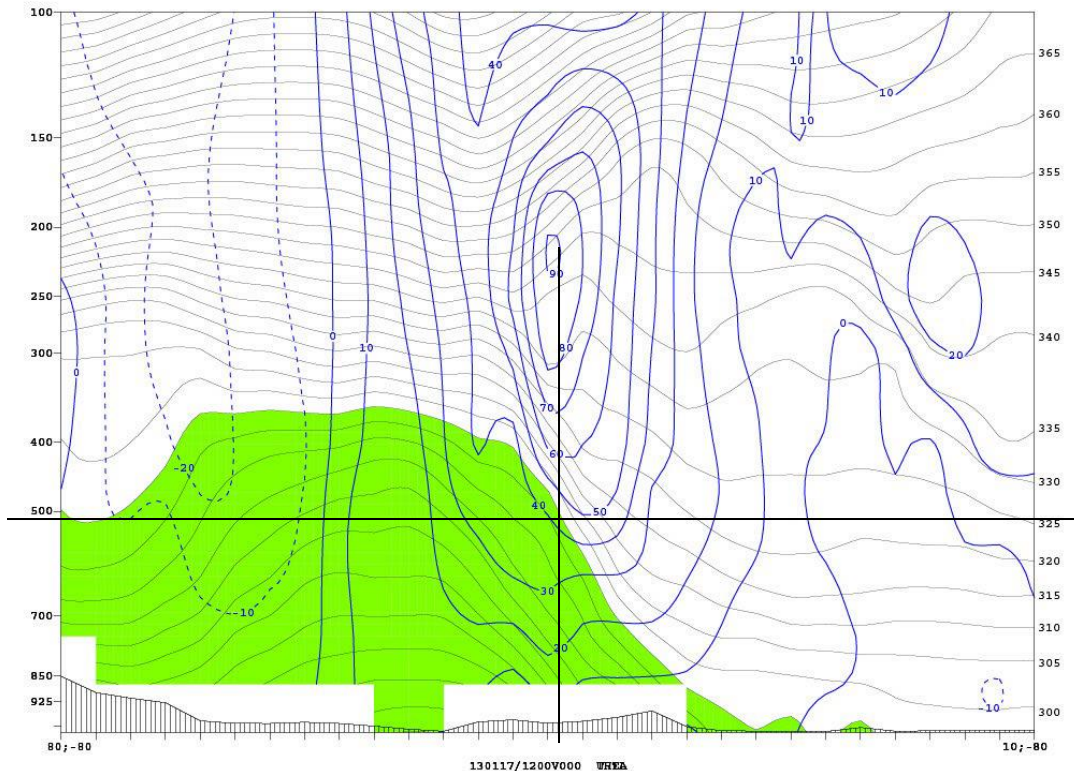
Margules relation for a real front-

What is the sloping of the front on Jan 17th 2013?

The Margules equation:

$$\tan \gamma = \frac{f(u_2 - u_1)}{g\left(\frac{\theta_2 - \theta_1}{\bar{\theta}}\right)}$$

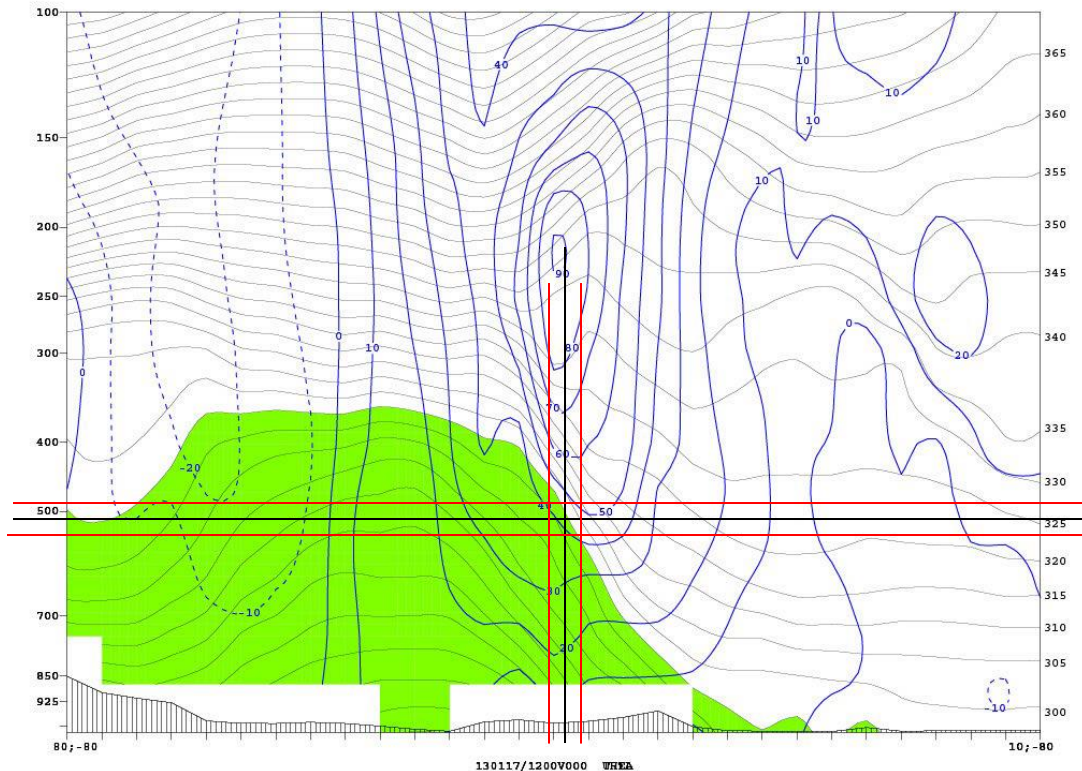
Often easier to identify the front and the cold dome in terms of *potential temperature*



What is the angle of the front? Calculate using Margules equation and verify from the figure using the estimated distances!

Margules relation for a real front-

What is the sloping of the front on Jan 17th 2013?



The Margules equation:

$$\tan \gamma = \frac{f(u_2 - u_1)}{g\left(\frac{\theta_2 - \theta_1}{\bar{\theta}}\right)}$$

$$\Delta u = u_2 - u_1 \approx 8 \text{ ms}^{-1}$$

$$\theta_2 - \theta_1 \approx 300\text{K} - 290\text{K} = 10\text{K}$$

$$\bar{\theta} \approx 295\text{K}$$

$$\tan \gamma \approx \frac{10^{-4} \cdot 8}{9.8 \left(\frac{10}{295}\right)} \rightarrow \gamma \approx 0.14^\circ$$

$$Z_{500} \approx 5.5 \text{ km}$$

$$\Delta y \approx 15^\circ \approx 15 * 110 \text{ km}$$

$$\tan \gamma \approx \frac{5.5}{1650} \rightarrow \gamma \approx 0.19^\circ$$



Advection in the atmosphere

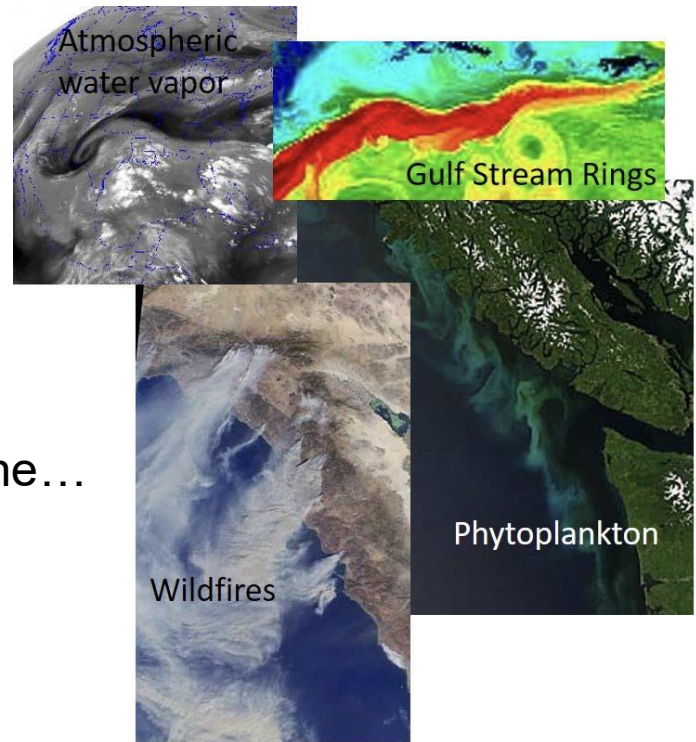
Tracer transport in the atmosphere

In the atmosphere:

- Aerosols
- Water vapor
- Temperature
- Dust, volcanic eruptions (ash)
- Chemical tracers: carbon (wildfires), ozone...
- Radioactive plumes (e.g., Fukushima)

In the ocean:

- Biological substances (e.g., Phytoplankton)
 - Marine pollution- plastics in the ocean
 - Oil Spill
 - ...
- Tracers are transported by winds and currents in the atmosphere & Ocean
 - Their dispersal depends on the motion and Earth's rotation



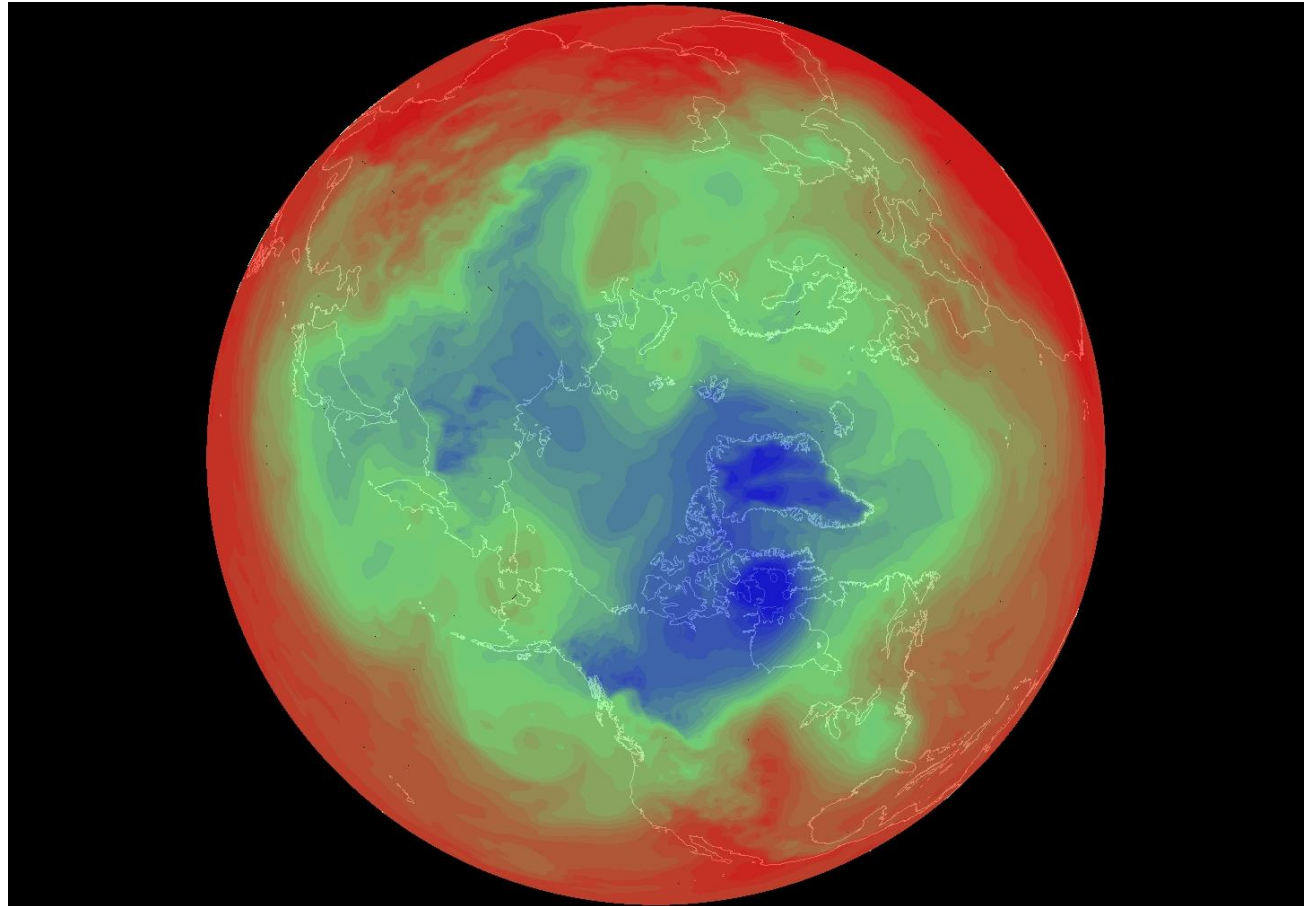
Temperature advection

Temperature
at 850 mb, ~1.5 km

Color scale:

red = hot

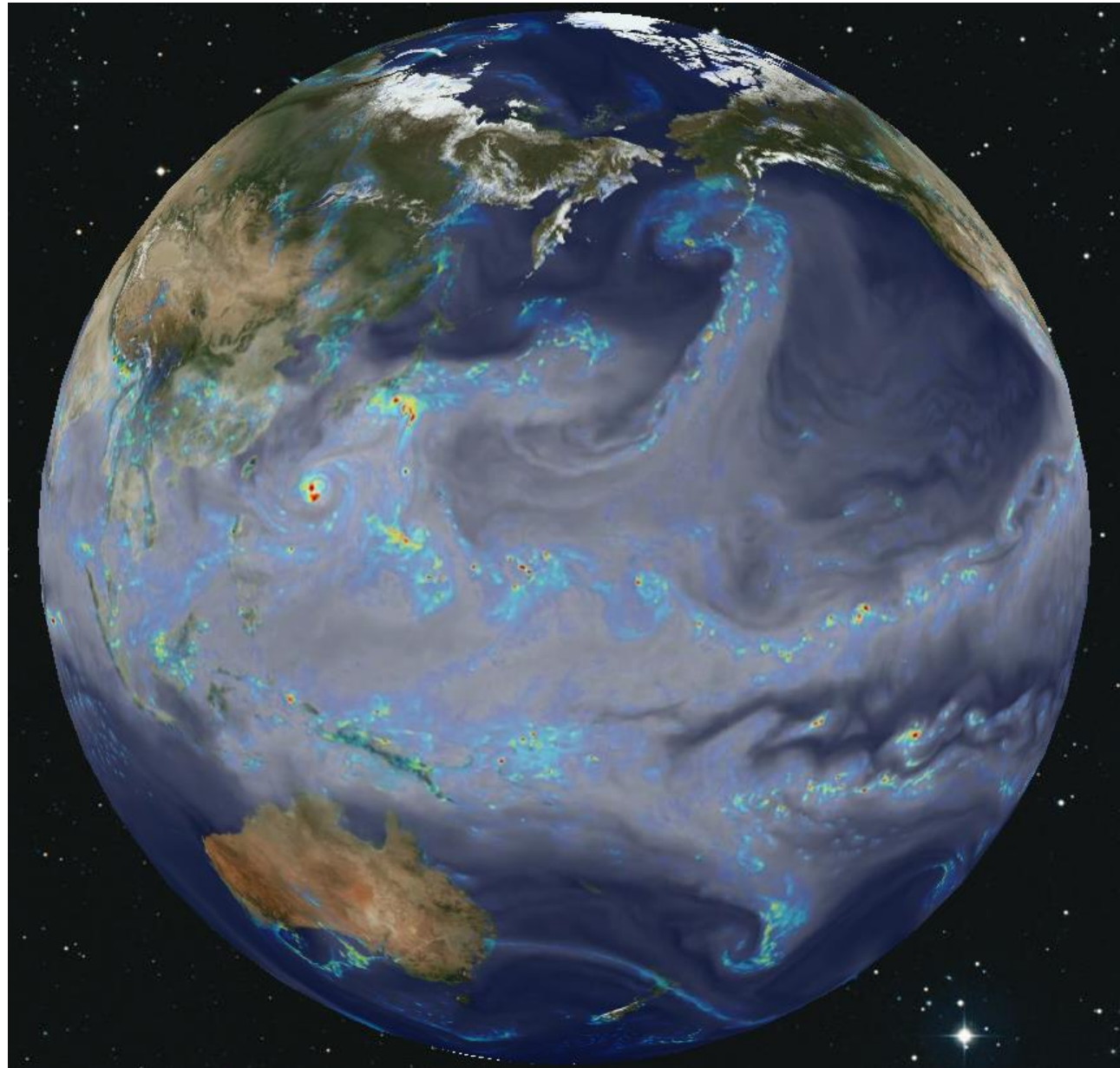
blue = cold



Water vapor

Total precipitable water (white)
and
rainfall (colors 0-15 mm/hr;
red=highest).

NASA Goddard Earth Observing System
Model (GEOS-5) – 10 km global simulation



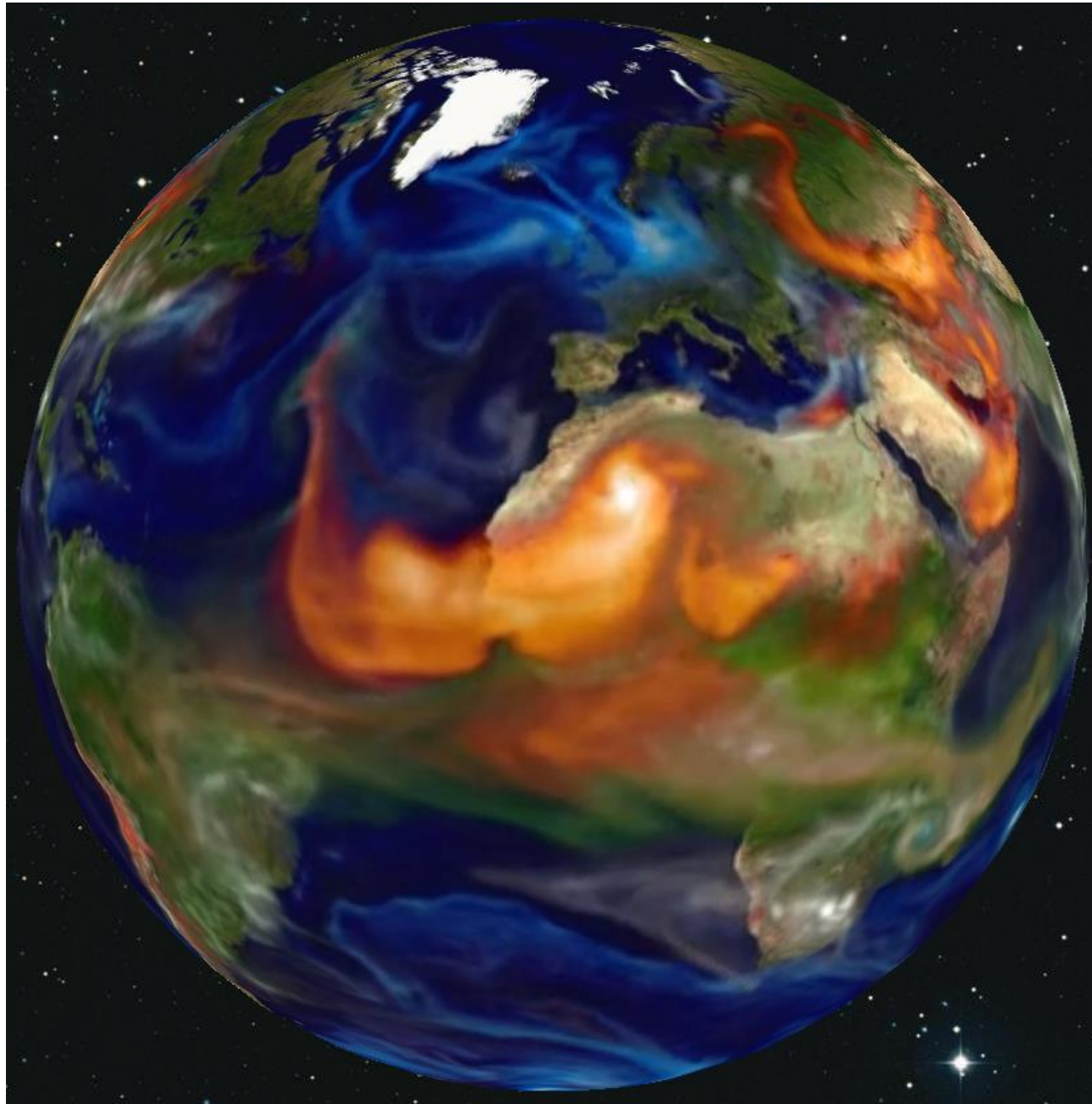
[Movie is available on the EsGlobe under
“GEOS-5 Water Vapor”](#)

Aerosols

The colors show four different aerosols:

- grey=sulfate
- green=organic and black carbon
- blue=sea-salt
- red=dust

The simulation uses GEOS-5 and the Goddard Chemistry Aerosol Radiation and Transport (GOCART) Model.



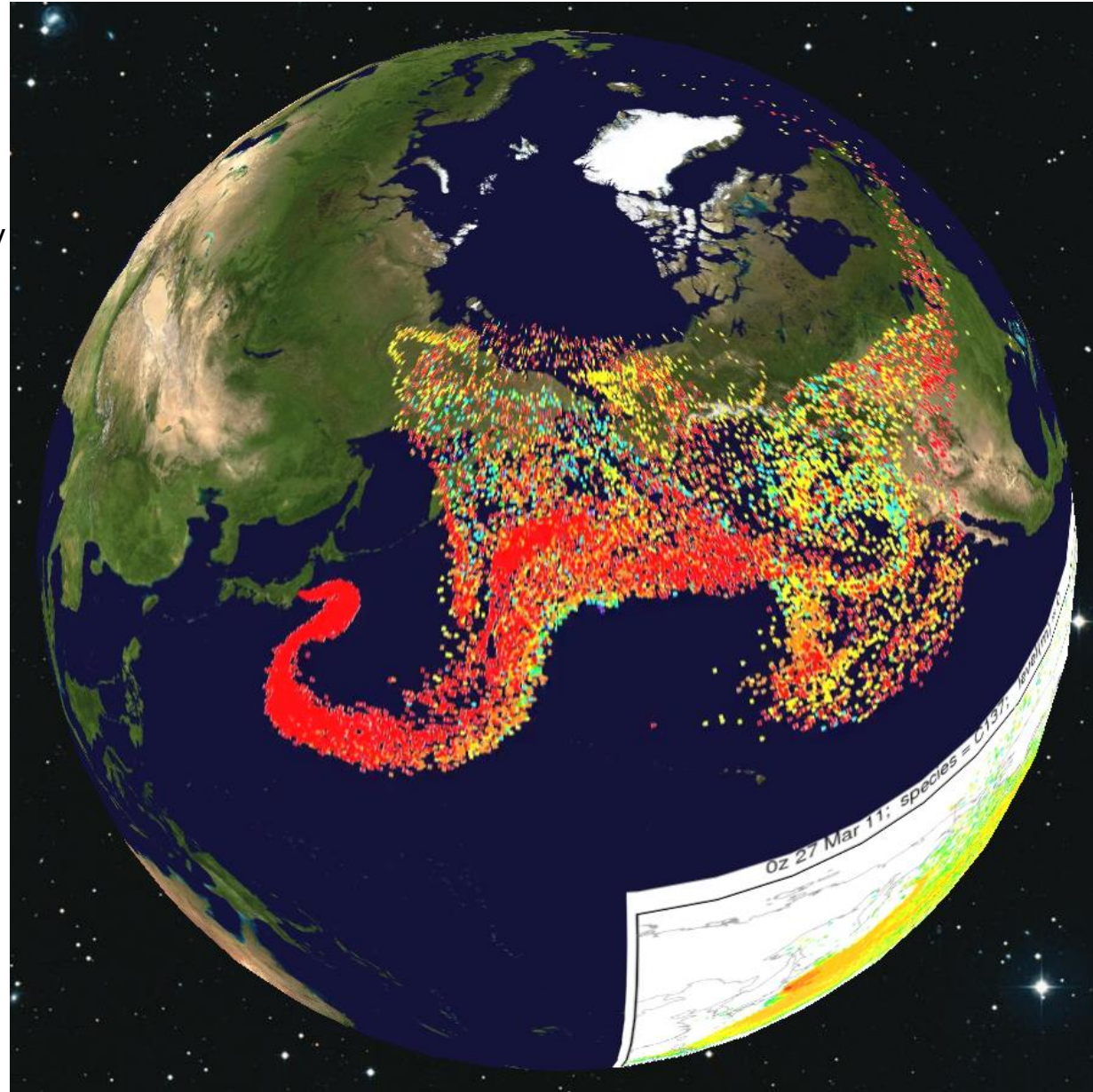
[Movie is available on the EsGlobe under "Atmospheric aerosols"](#)

Fukushima radioactive aerosols

March 11, 2011

Cesium-137 emitted from Fukushima

Each change in particle color represents a decrease in radioactivity by a factor of 10.



[Movie is available on the EsGlobe under "Fukushima radiation release"](#)

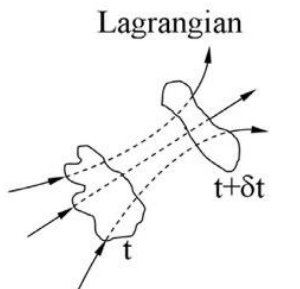
Lagrangian vs. Eulerian derivative

$$\rightarrow \left(\frac{\partial C}{\partial t} \right)_{\text{fixed particle}} = \underbrace{\frac{\partial C}{\partial t}}_{\text{fixed point}} + \underbrace{u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} + w \frac{\partial C}{\partial z}}_{\text{advection}} = \frac{DC}{Dt}$$

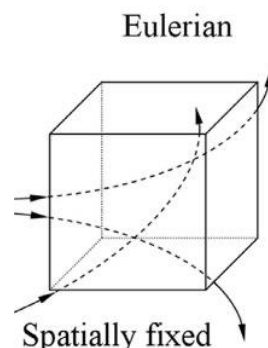
Where

$$\frac{D}{Dt} \equiv \frac{\partial}{\partial t} + u \frac{\partial}{\partial x} + v \frac{\partial}{\partial y} + w \frac{\partial}{\partial z} \equiv \frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla$$

$$\nabla \equiv \left(\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right) \rightarrow$$



Following the motion of the fluid element



Spatially fixed volume element

$$\boxed{\frac{D}{Dt} = \frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla}$$

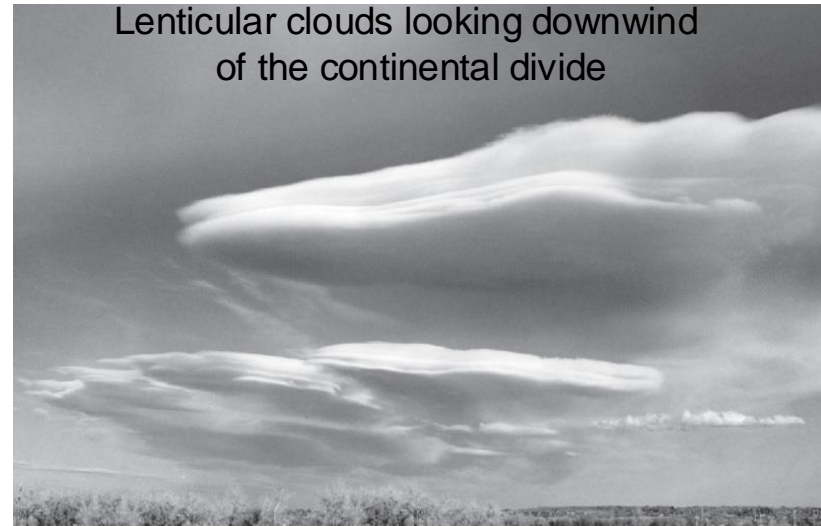
Lagrangian Eulerian Advection

Eulerian derivative

- Mountains produce Lee waves
- Steady state: pattern of clouds
- Cloud amount= C does not change with time

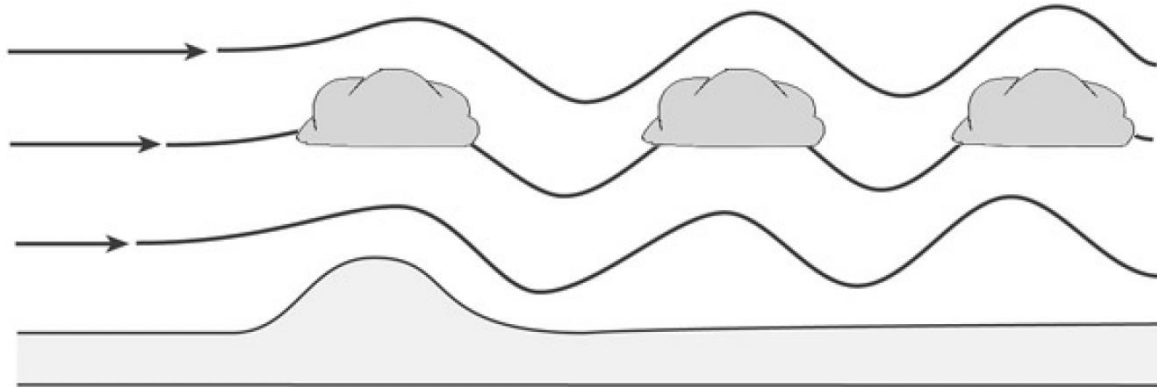
$$C = C(x, y, z, t)$$

$$\left(\frac{\partial C}{\partial t} \right)_{\text{fixed point in space}} = 0$$

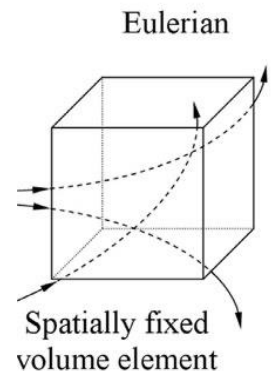


Lenticular clouds looking downwind of the continental divide

(Photo courtesy of Dale Durran, University of Washington.)



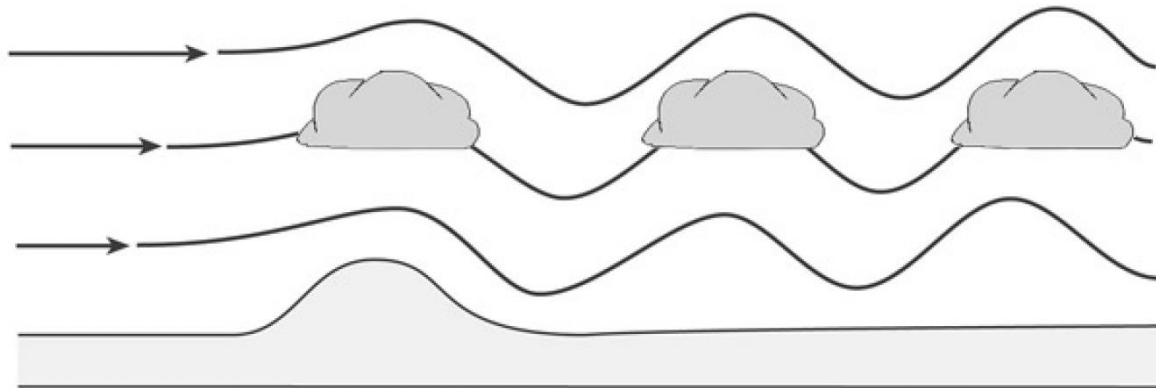
At any fixed location, cloud fraction does not change, even though the air is flowing through!



Lagrangian derivative

- However, C is not constant following a particular parcel $C = C(x, y, z, t)$
- As the parcel moves upward, it cools, water condenses out, cloud forms $\rightarrow C$ increases
- As the parcel moves downward, the water goes back into the gaseous phase, the cloud disappears $\rightarrow C$ decreases.

$$\left(\frac{\partial C}{\partial t} \right)_{\text{fixed particle}} \neq 0$$



Lagrangian derivative

- For small deviations of $C = C(x, y, z, t)$, which is a function of position and time:

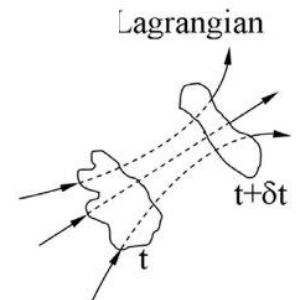
$$\delta C = \frac{\partial C}{\partial t} \delta t + \frac{\partial C}{\partial x} \delta x + \frac{\partial C}{\partial y} \delta y + \frac{\partial C}{\partial z} \delta z$$



$$(\delta C)_{\text{fixed particle}} = \left(\frac{\partial C}{\partial t} + u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} + w \frac{\partial C}{\partial z} \right) \delta t$$

Where we used: $\delta x = u \delta t$, $\delta y = v \delta t$, $\delta z = w \delta t$.

The variation of a property C following an element of fluid!



Following the motion of the fluid element

Lagrangian vs. Eulerian derivative

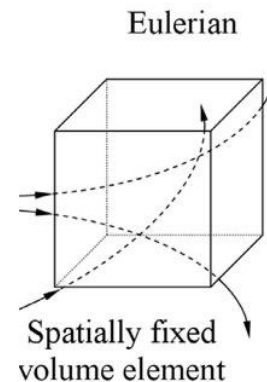
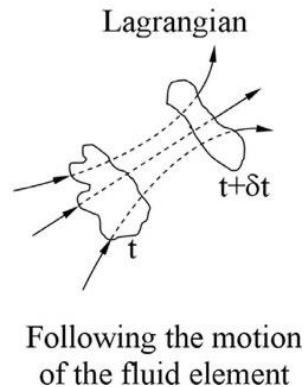
$$\boxed{\frac{D}{Dt} = \frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla}$$

Lagrangian Eulerian Advection

Where

$$\frac{D}{Dt} \equiv \frac{\partial}{\partial t} + u \frac{\partial}{\partial x} + v \frac{\partial}{\partial y} + w \frac{\partial}{\partial z} \equiv \frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla$$

$$\nabla \equiv \left(\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right)$$



Examples:

1) Velocity and position of a fluid parcel-

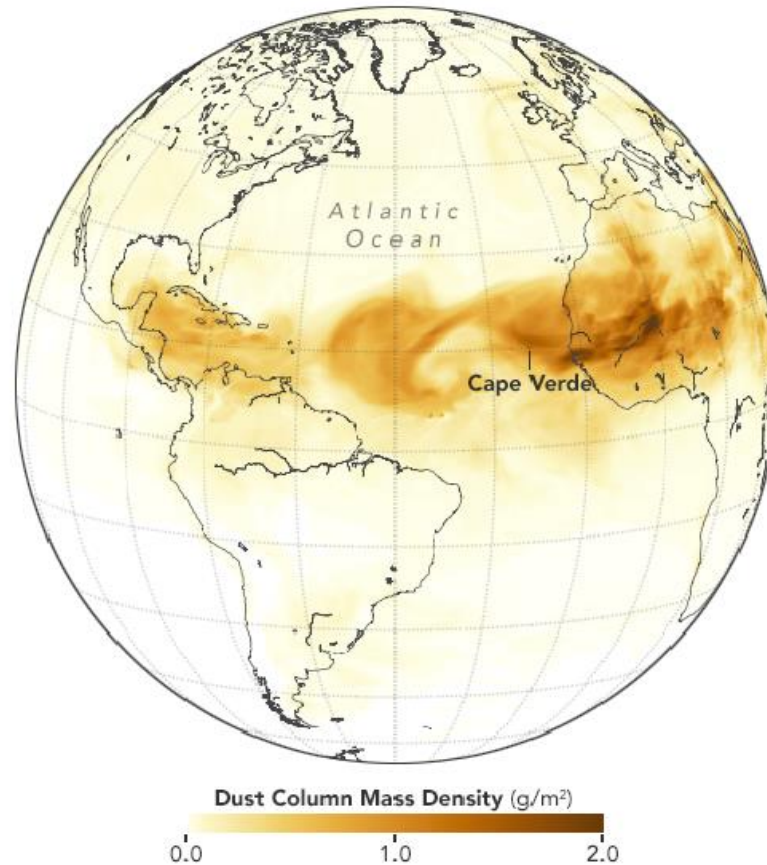
$$u = \frac{D}{Dt}x; \quad v = \frac{D}{Dt}y$$

$$x = \int u dt; \quad y = \int v dt$$

Where u is the speed in the x direction and v is the speed in the y direction

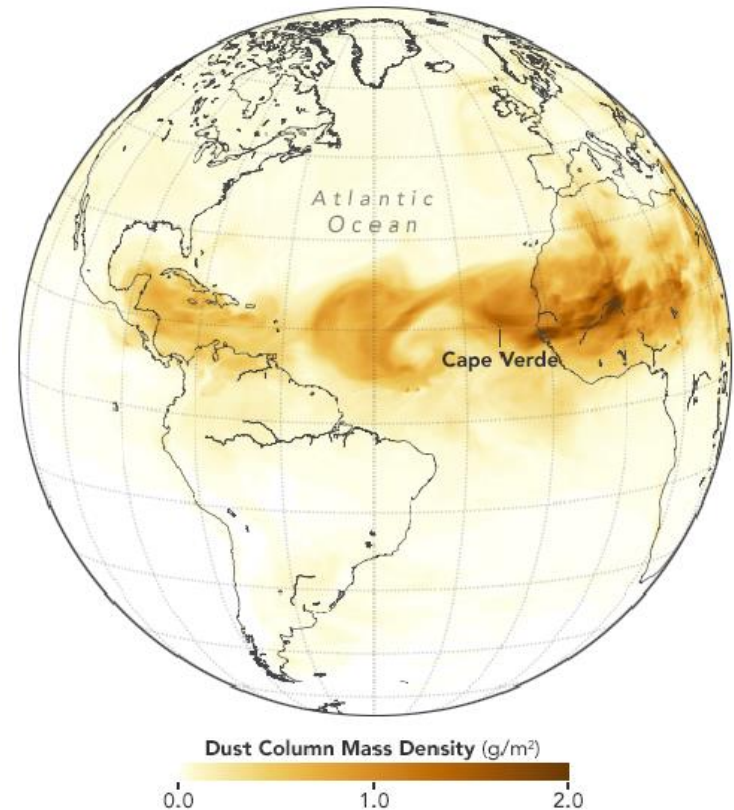
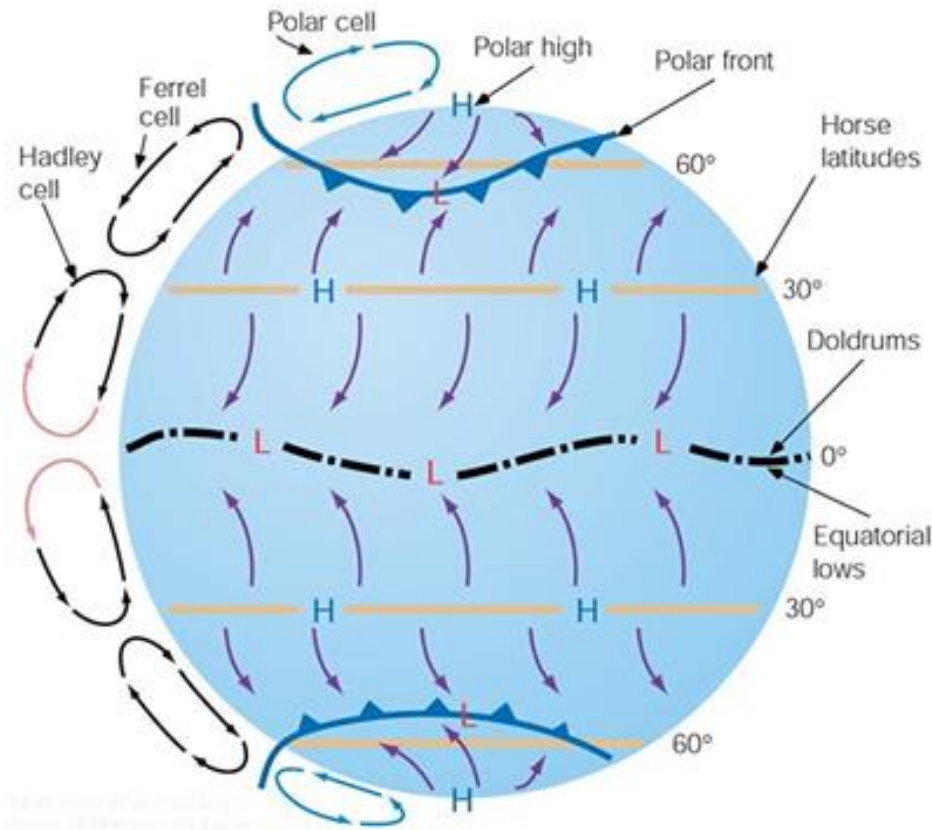
*The positions of a fluid particle can be determined
Lagrangianly from the winds!*

Saharan Dust - June/July 2018



On June 18, satellites began to detect thick plumes of Saharan dust passing towards the Atlantic Ocean. This brought the tropical Atlantic one of its dustiest weeks in 15 years.

How can dust from the Sahara reach the US?



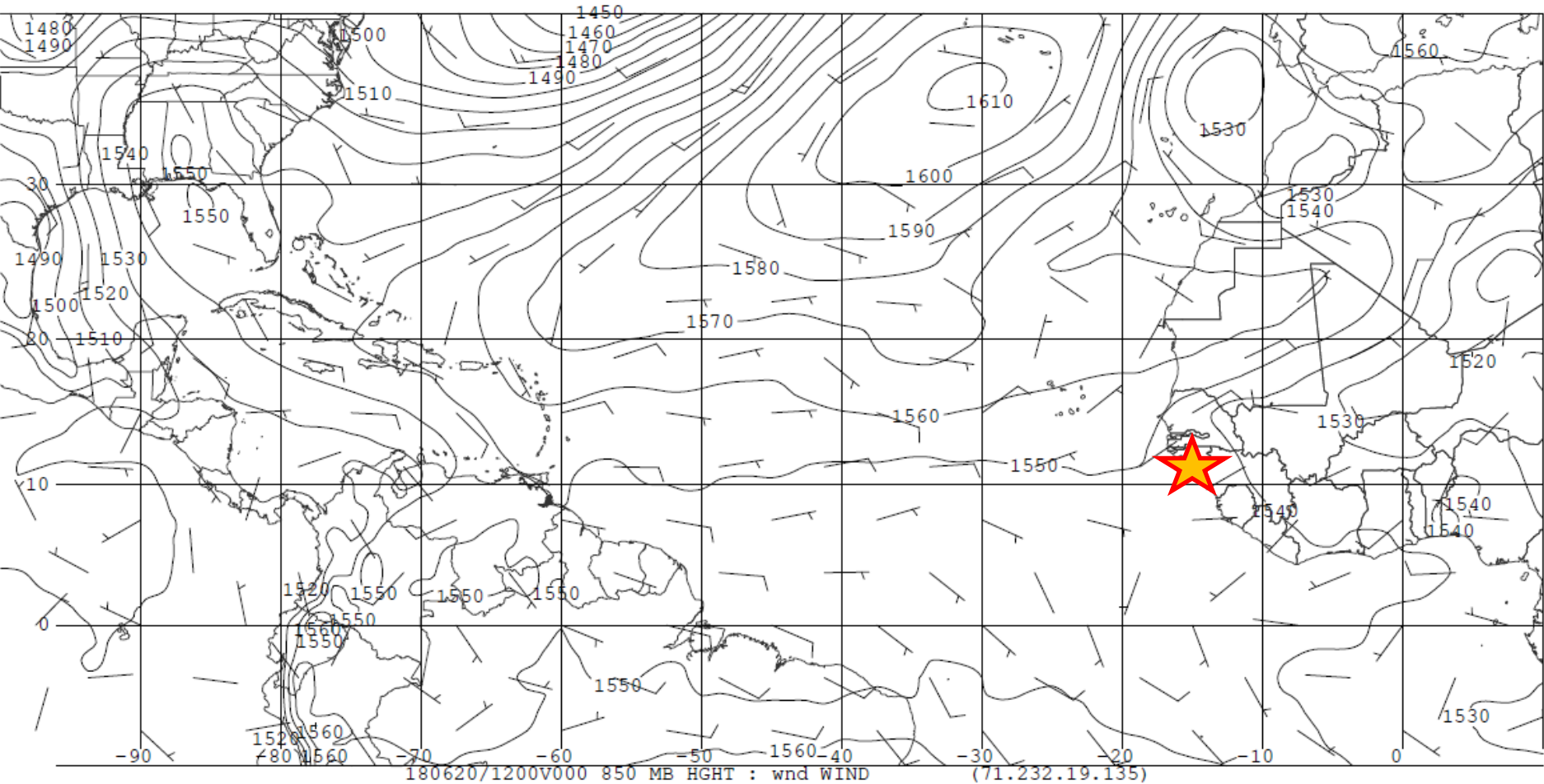
Coriolis force diverts the flow such that at the surface, we find **easterlies** (winds from the east) in the subtropics (also known as the **trade winds**)

Case study: June 20 - 21, 2018

- Build by hand trajectories using 850 mb wind (GFS analyses)
- Verify your calculation by using EsGlobe – atmospheric patch of particles

How long does it take Saharan dust to cross the Atlantic and reach Texas?

June 20 2018 12 GMT



Note: barbs are in m/sec

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1) Velocity and position of a fluid parcel-

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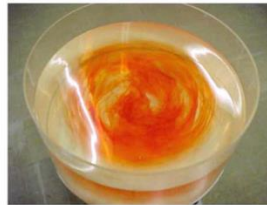
$$x = \int u dt; \quad y = \int v dt$$

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2) Tracer Transport- assume T is some conserved tracer

$$\frac{D}{Dt}T = 0$$

Fluid parcels conserve (except for small diffusive processes) the concentration of dye



Examples:

3) Temperature advection-

$$\frac{D}{Dt}T = 0$$

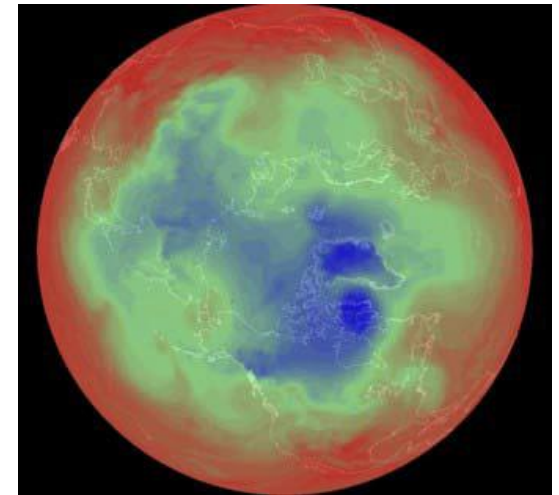
Assuming temperature is conserved (which is not entirely correct), and that meridional (north-south) advection is dominant, we can write-

$$\frac{\partial T}{\partial t} \simeq -v \frac{\partial T}{\partial y}$$

Where $\frac{\partial T}{\partial y} < 0$

Hence, $v < 0 \Rightarrow \frac{\partial T}{\partial t} \simeq -v \frac{\partial T}{\partial y} < 0$

$v > 0 \Rightarrow \frac{\partial T}{\partial t} \simeq -v \frac{\partial T}{\partial y} > 0$

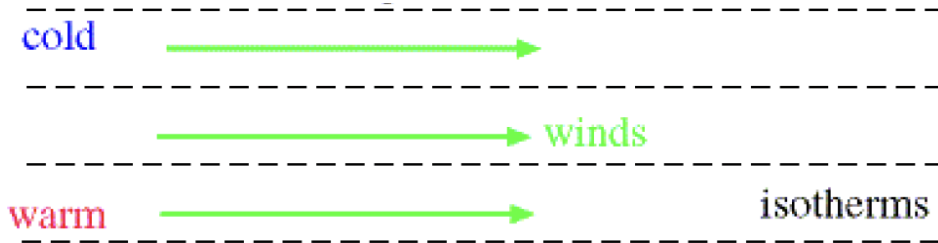


red = hot
blue = cold

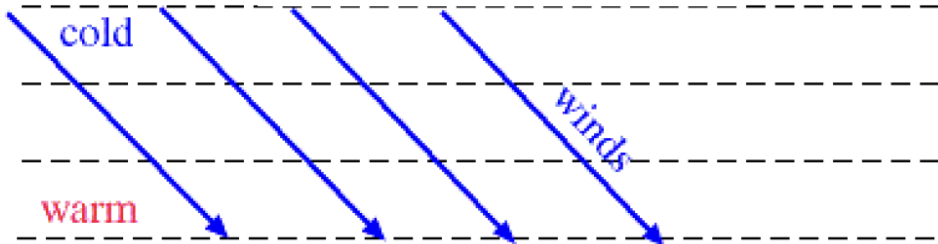
In regions where the cold air is moving south ($v < 0$) the local rate of change of temperature is negative (cooling). Similarly, local warming when $v > 0$

Temperature advection

No advection



Cold temperature advection



Warm temperature advection

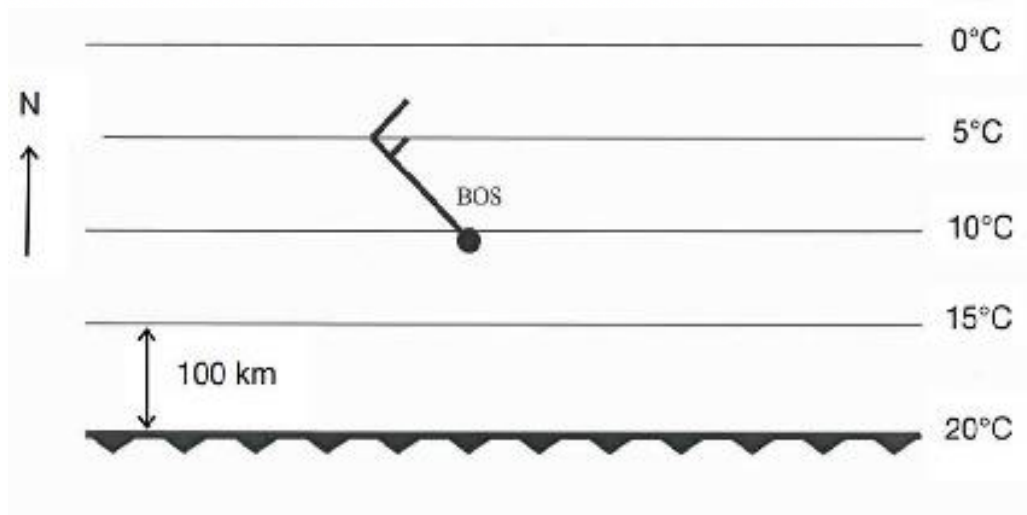


Temperature advection

Example: temperature changes in Boston due to a hypothetical front

If we assume that temperature T is conserved: $\frac{D}{Dt}T = 0$.

then: $(\partial T / \partial t)_{\text{at Boston}} = -u \partial T / \partial x - v \partial T / \partial y$



A Schematic front. Suppose a cold front has just passed over Boston. The front is oriented west to east and the temperature drops 5°C every 100 km (as sketched in Fig.11). As the wind blows from the NW at 15kts , where $1\text{kts} = 0.5\text{m/s}$, infer how much the temperature will be expected to drop in 12 hours due to cold air advection?

By how much did the temperature drop after 12 hours?