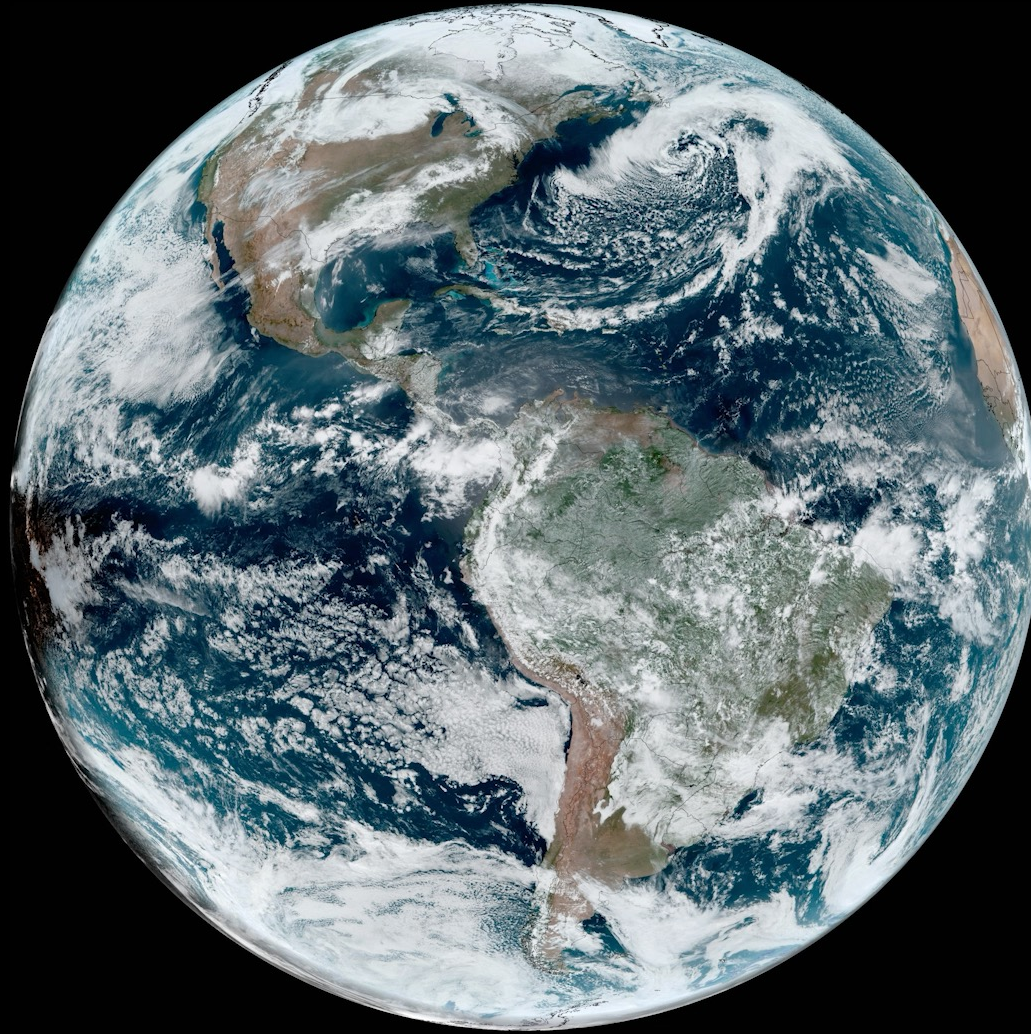


# P3: Heat and Moisture Transport

## The general circulation



But first...the eclipse! April 8<sup>th</sup> 2024

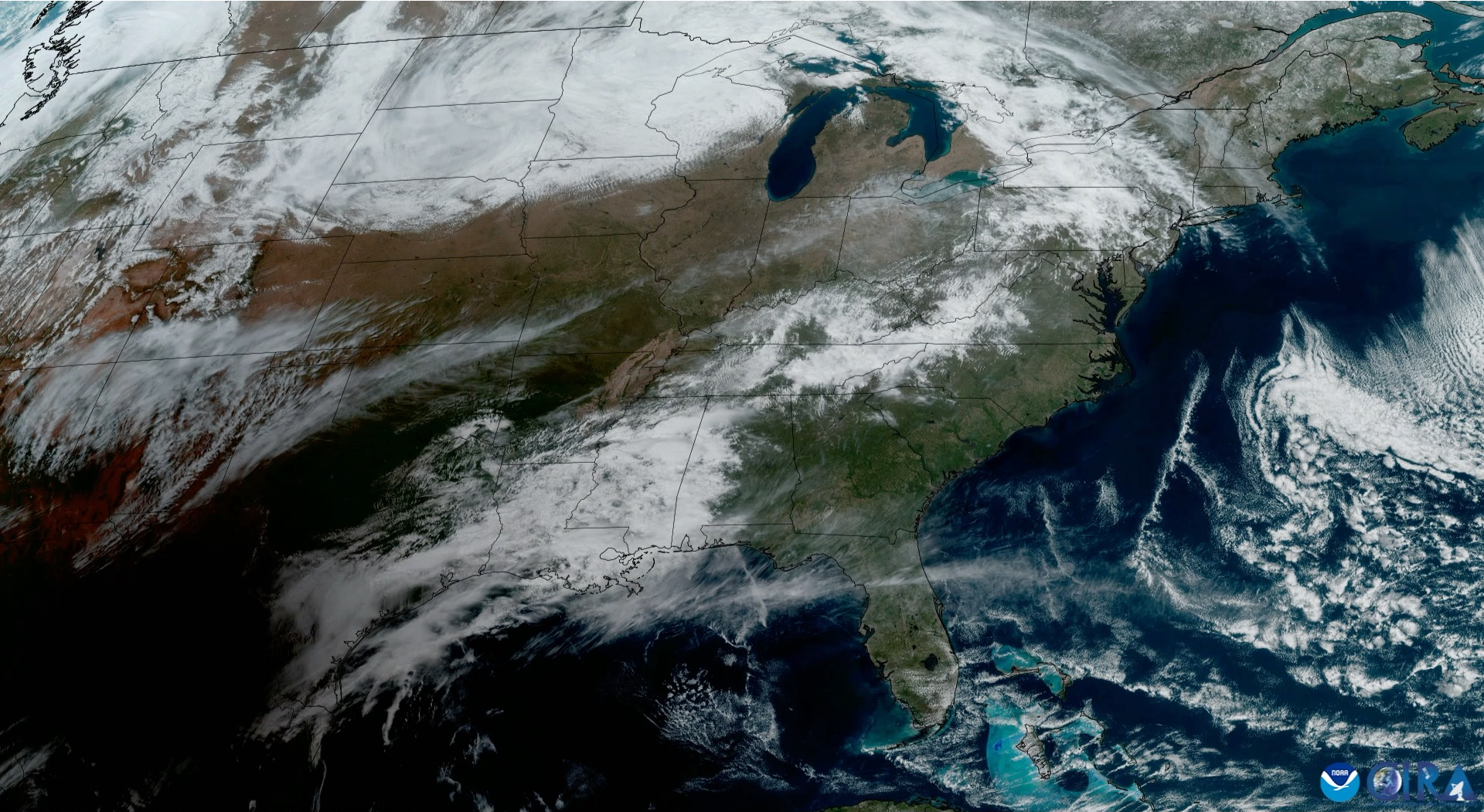


2024-04-08 | 16:30 UTC | GOES-16 | ABI | GeoColor

A Complete, Incredible View of The Great North American Eclipse



But first...the eclipse! April 8<sup>th</sup> 2024



2024-04-08 | 18:21 UTC | GOES-16 | ABI | GeoColor

Cloud suppression during the eclipse!

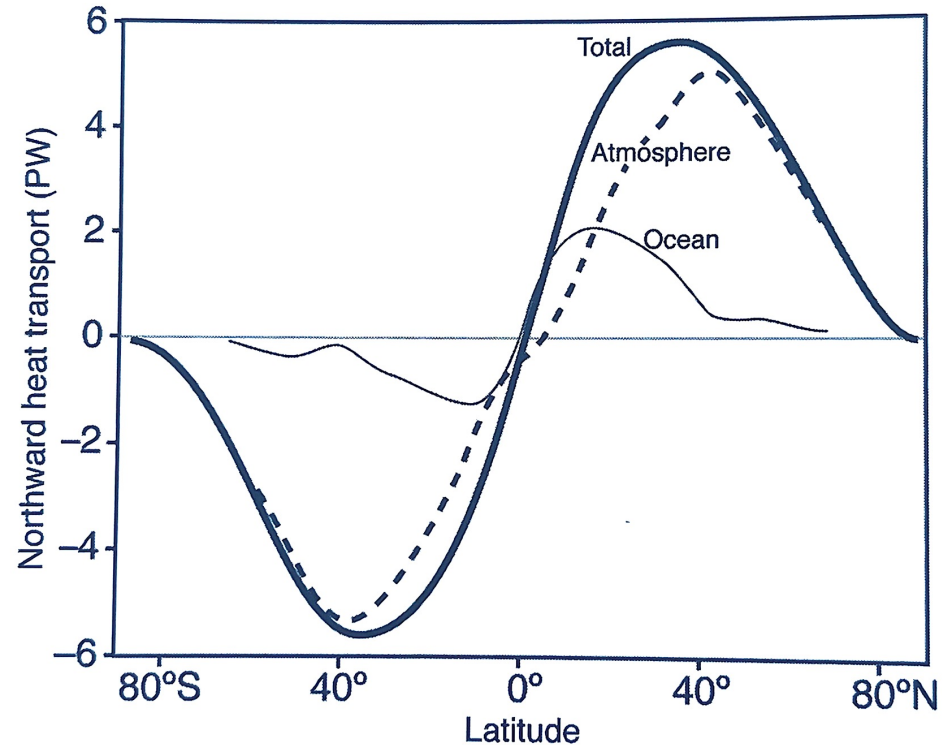
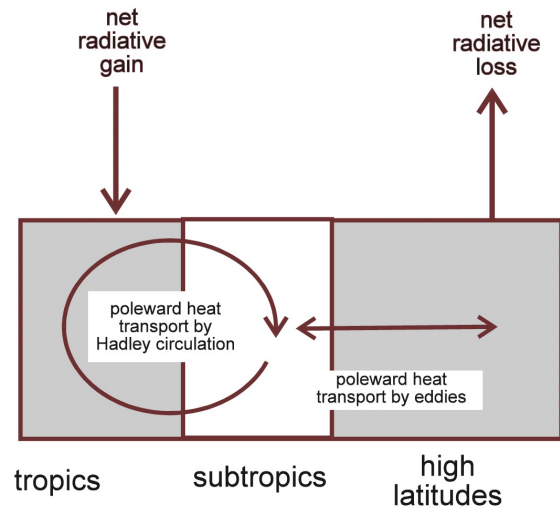
# 12.307- project 3 (data class 1)

## Hadley circulation in the atmosphere:

- Connection to Hadley tank experiment
- Atmospheric climatology using EsGlobe
- Identify the Hadley circulation
- **Break**
- N-S heat transport in the tropics
- Two layer model as in the tank experiment
- Moisture transport in the tropics
  
- Second class -
  - Heat and moisture transport in the tropics - review calculations
  - Eddy regime in the extra-tropics



# Meridional heat transport



- In the tropics, heat transport is mainly by the Hadley cell
- In the extratropics, heat transport is by the “eddy”
- The atmosphere transfer most of the heat, the ocean also contributes in the tropics

# Reminder- the three experiments that we saw in the lab:

$\Delta T = \text{large}$     $\Omega = \text{zero}$

*equator*

ice

The "reference" experiment

$\Delta T = \text{large}$     $\Omega = \text{small}$

*tropics*

ice

The Hadley experiment

$\Delta T = \text{large}$     $\Omega = \text{large}$

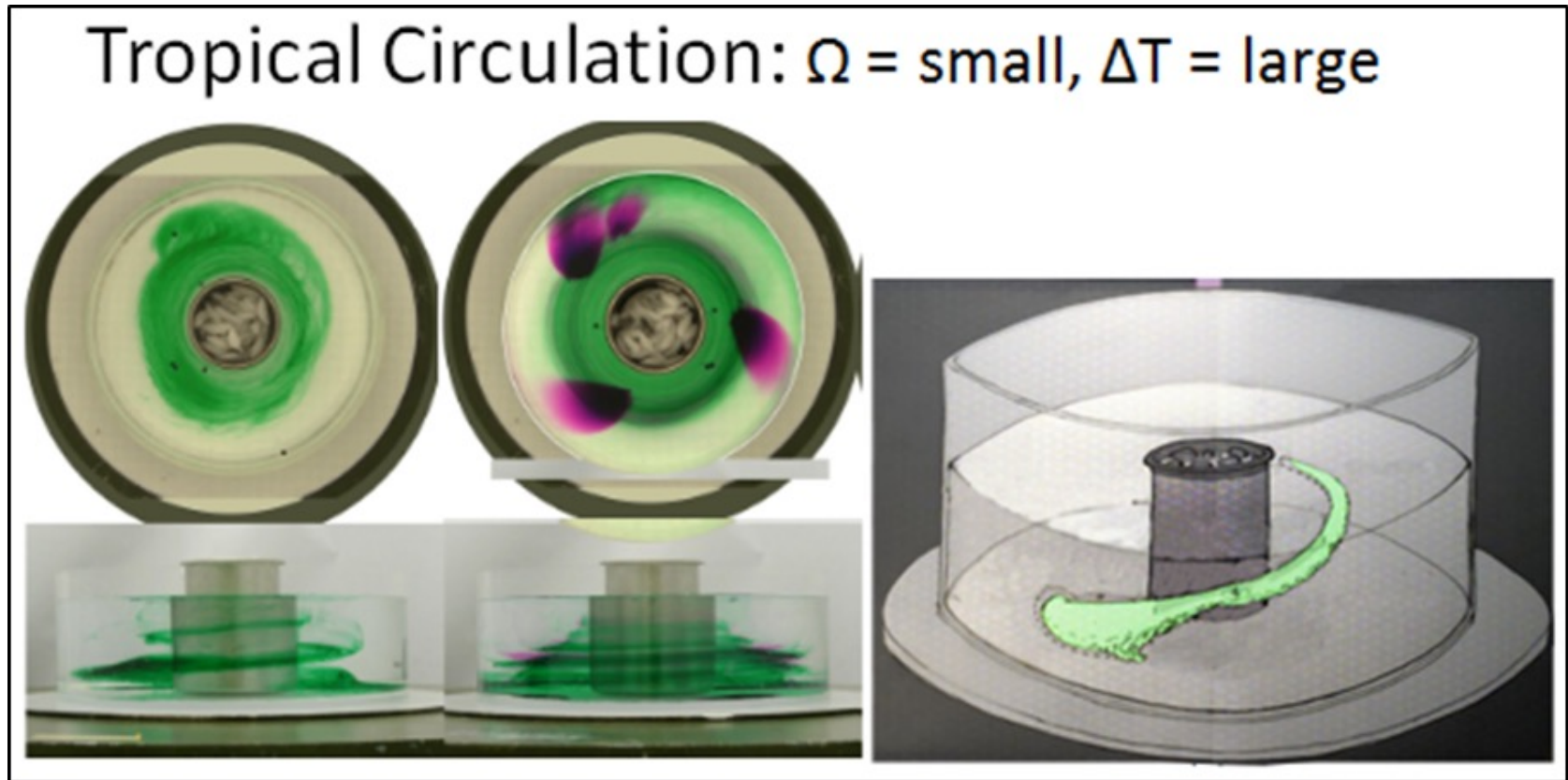
*extratropics*

ice

The Eddies experiment



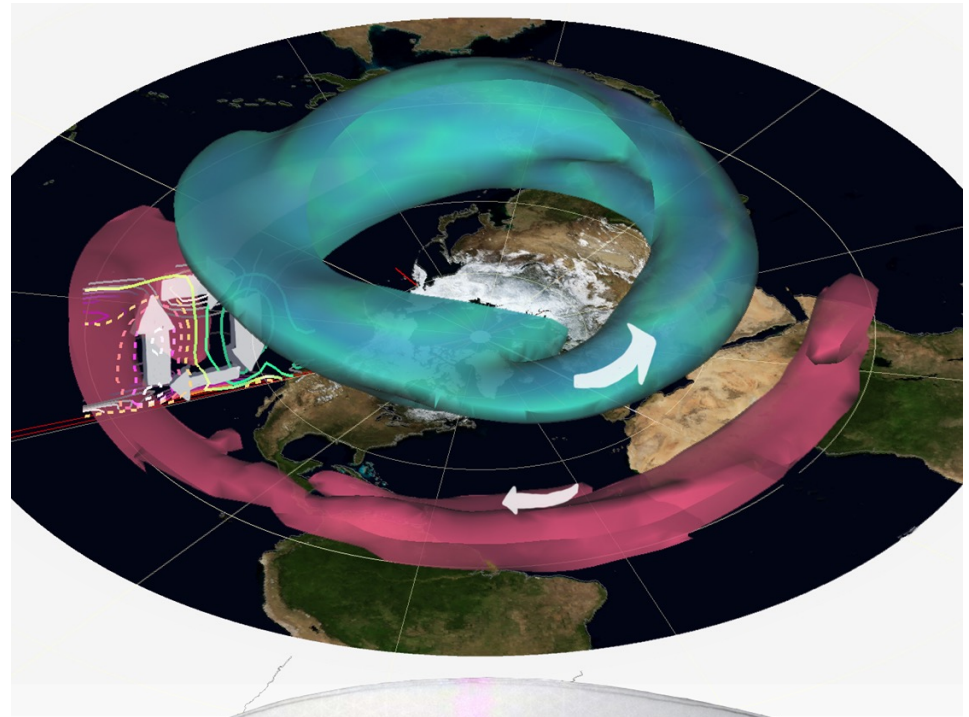
# Hadley Cell Experiment



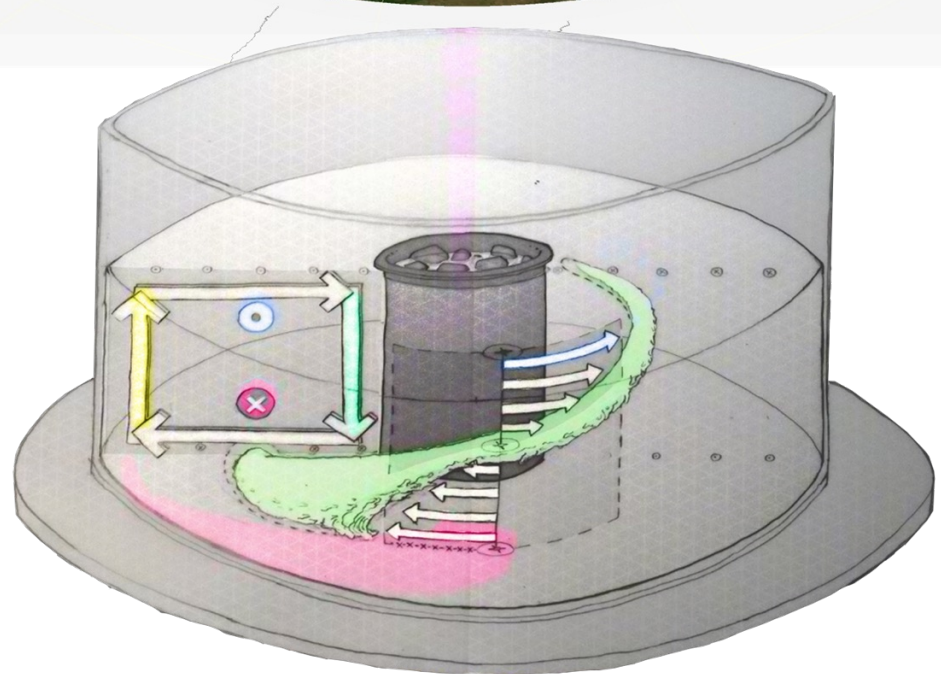
<http://lab.rotating.co>

We calculated the budget: amount of heat due to melting = the heat transport from the circulation

# Connection to the atmospheric circulation



Can we see evidence  
for this circulation in the  
atmosphere?





# Hadley Cell exercise

How can we find the Hadley Cell on earth?

Explore the General Circulation of the Atmosphere using climatological data on the EsGlobe

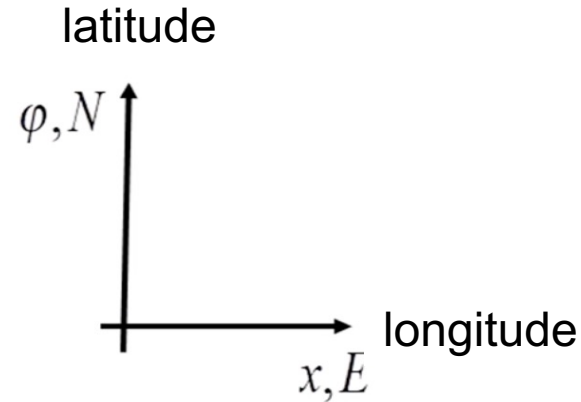
<http://eddies.mit.edu/307/>

Plot zonally averaged (January and July):

- Temperature (T) and potential temperature ( $\theta$ )
- Vertical velocity (omega)  $\omega = Dp/Dt$
- Meridional velocity (v)
- Zonal velocity (u)

# Time mean and zonal mean fields- reminder:

$$T(x, \varphi, p, t)$$



$$\bar{T}(x, \varphi, p) = \int_{t_1}^{t_2} T(x, \varphi, p, t) dt$$

Time mean

$$[\bar{T}(\varphi, p)] = \int_0^{360} \bar{T}(x, \varphi, p) dx$$

Zonal mean  
and time mean



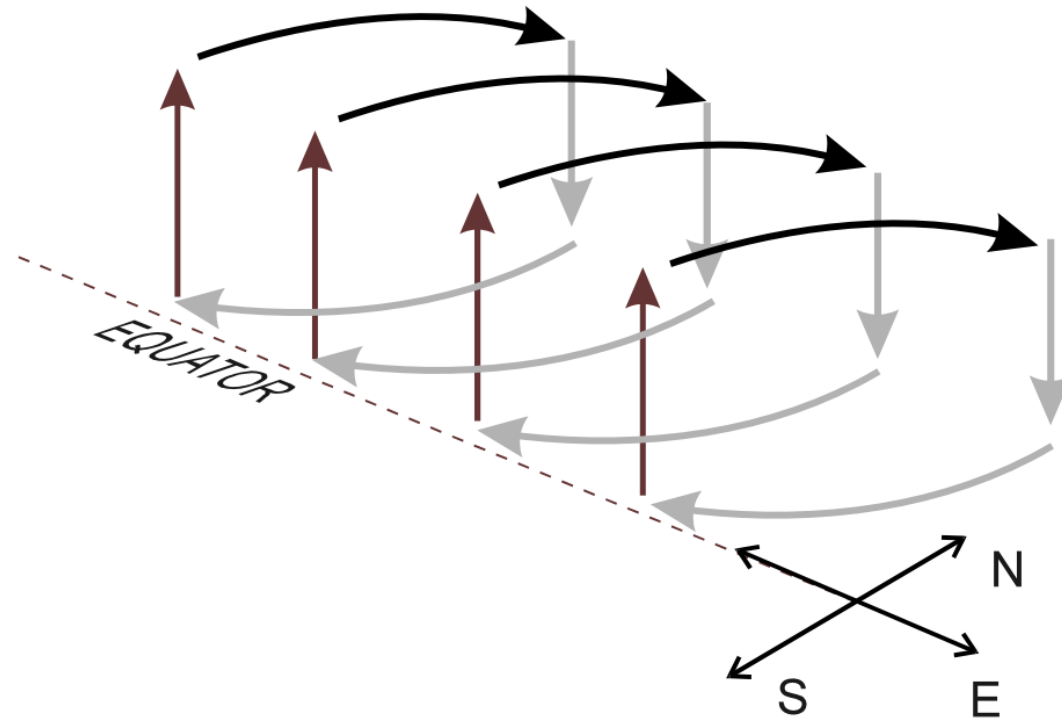


Figure 8: Schematic of the Hadley circulation (showing only the N Hem part of the circulation; there is a mirror image circulation south of the equator).

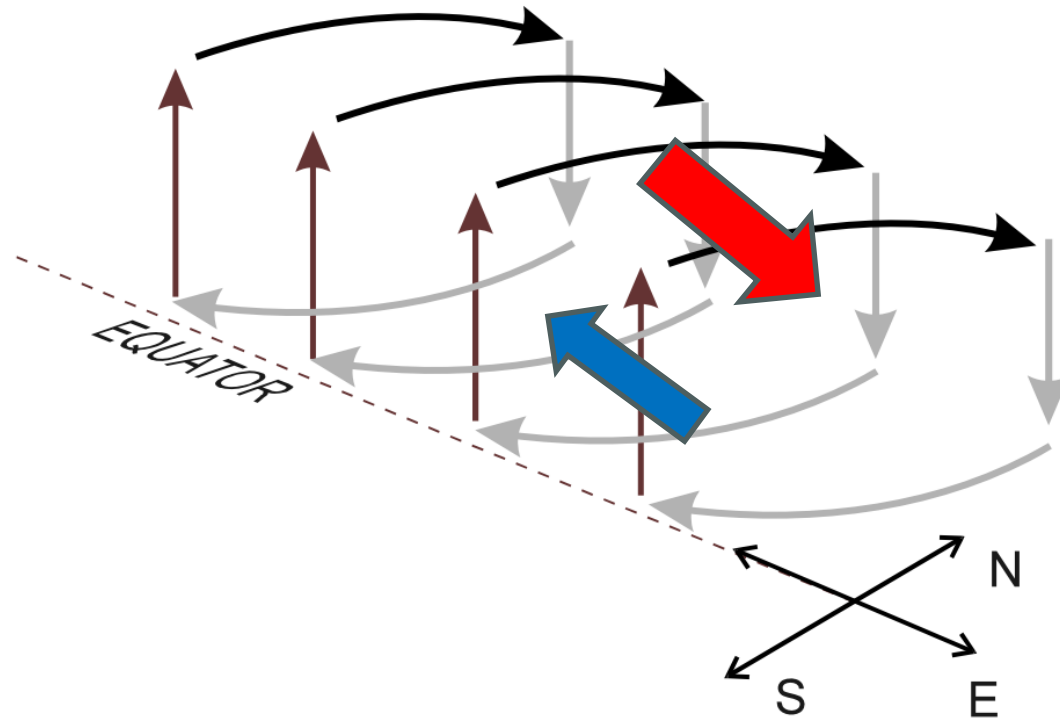
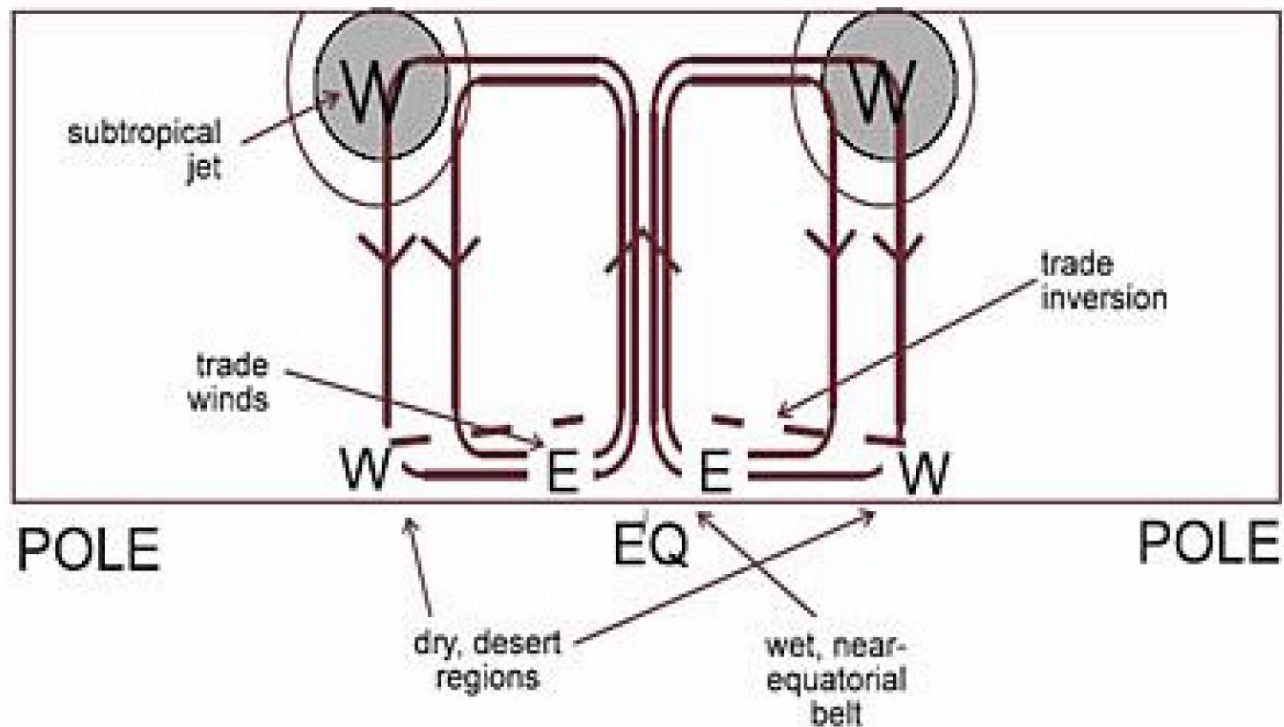


Figure 8: Schematic of the Hadley circulation (showing only the N Hem part of the circulation; there is a mirror image circulation south of the equator).

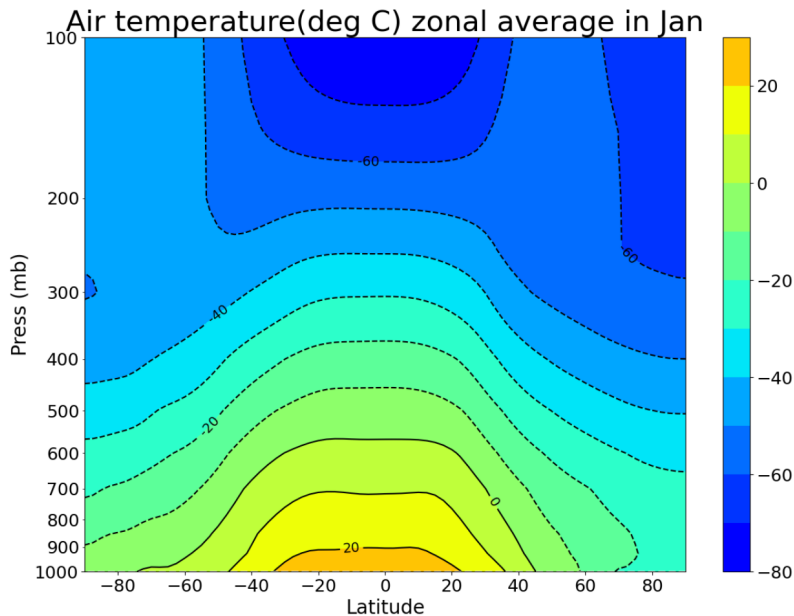
Can we identify a similar structure in the climatology?



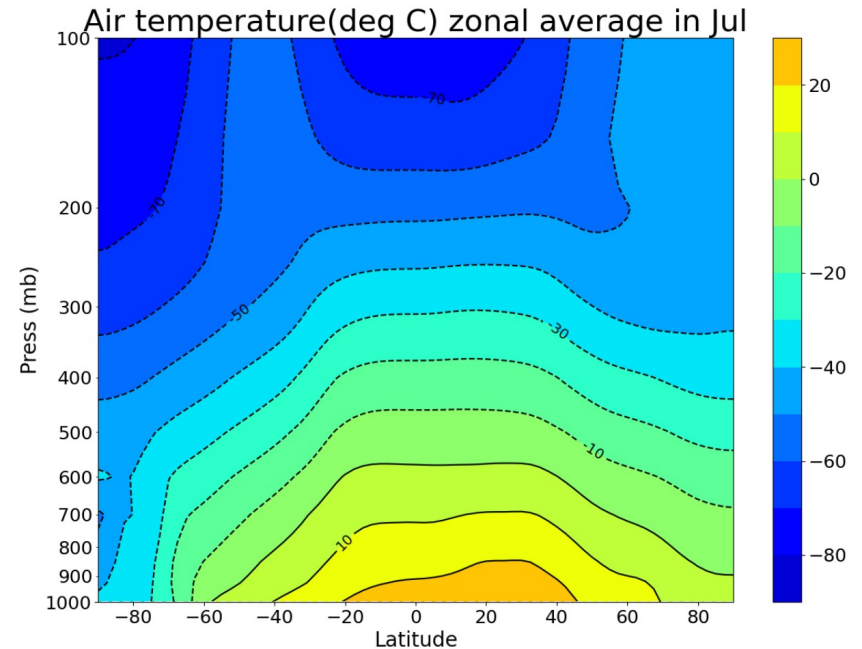


# Zonal mean temperature

January



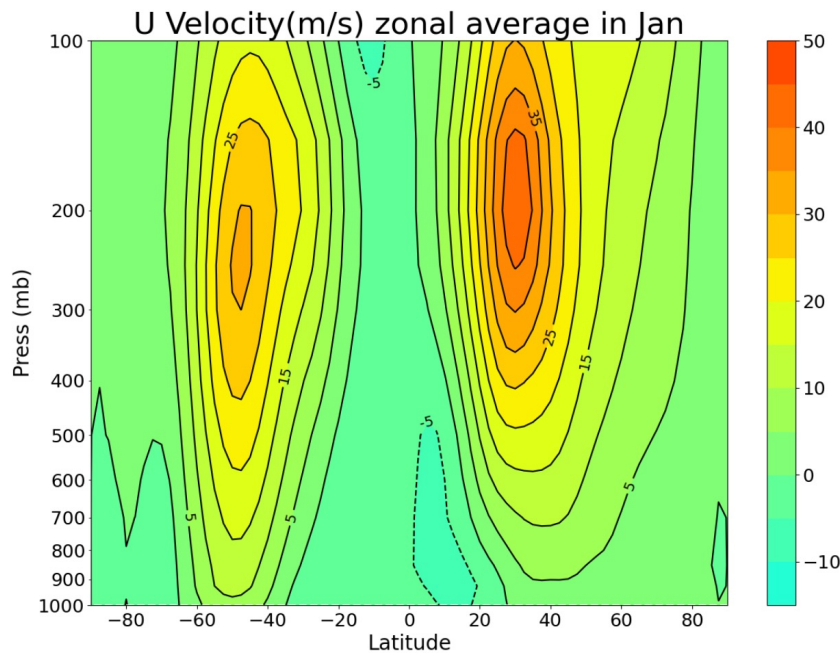
July



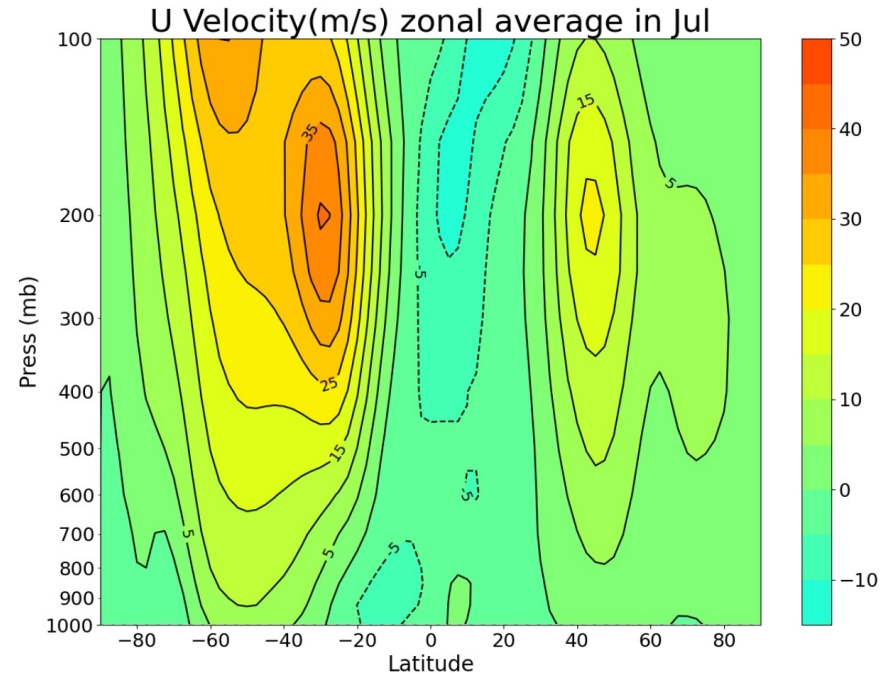
- Temperature more uniform in the tropics, decreases poleward and with height
- Where is the maximum surface temperature in each season?

# Zonal mean zonal wind

January



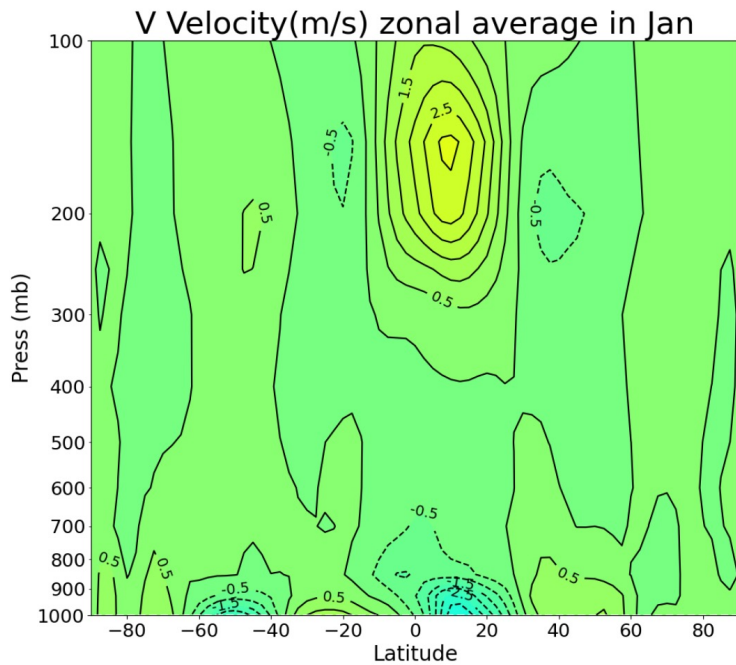
July



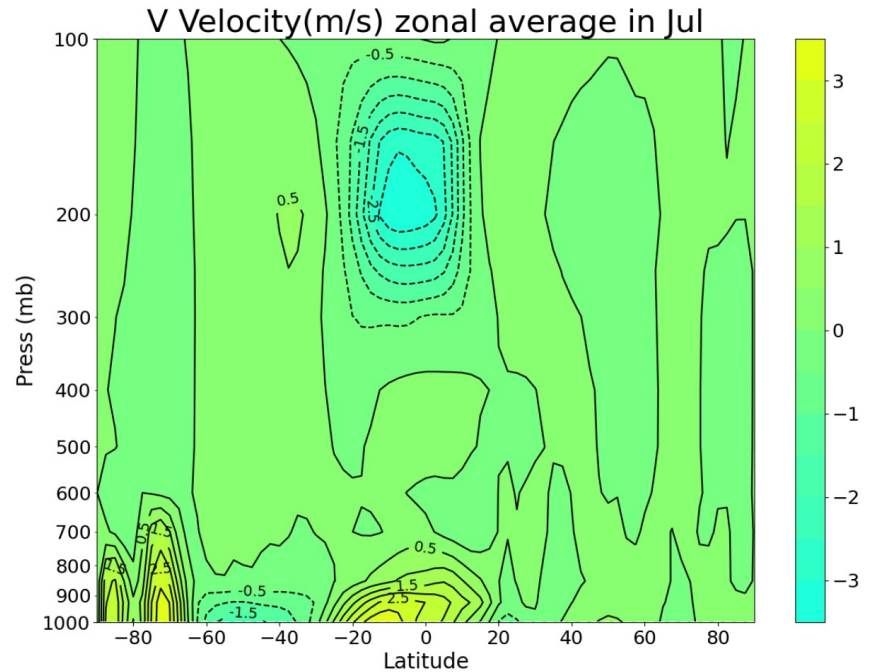
- One main jet stream in each hemisphere
- Can you identify the easterlies/westerlies? Where are they in each season?

# Zonal mean meridional wind

January



July



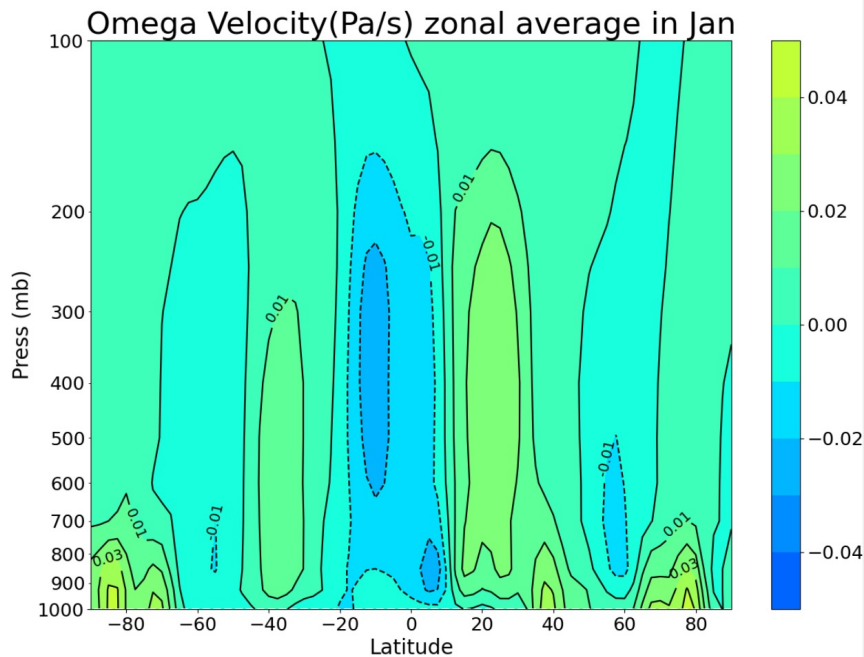
Mean  $V$  is only strong in the tropics (Hadley Cell), and mostly confined to either upper level or to the surface-

*Two layers!*

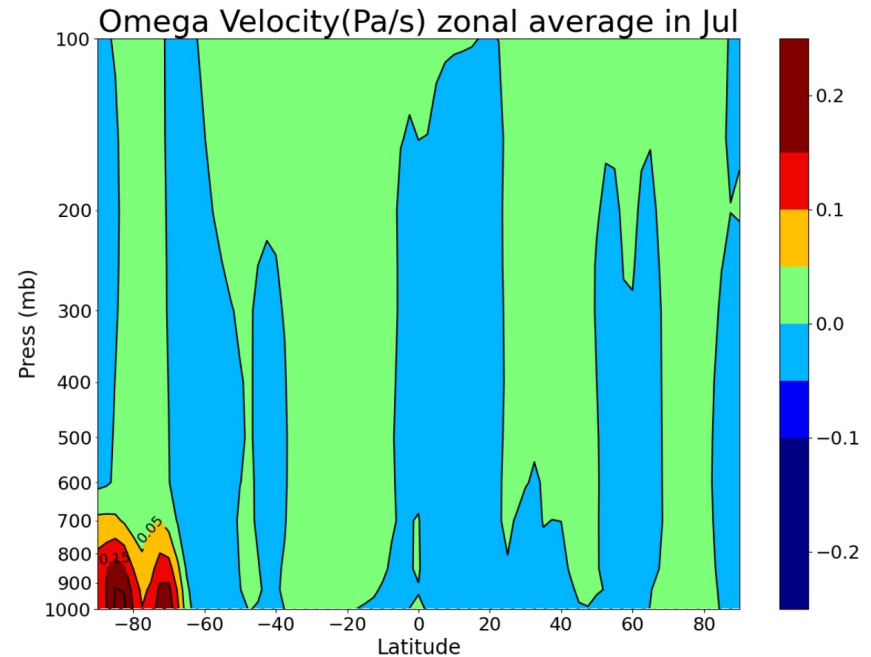


# Zonal mean vertical wind

January



July

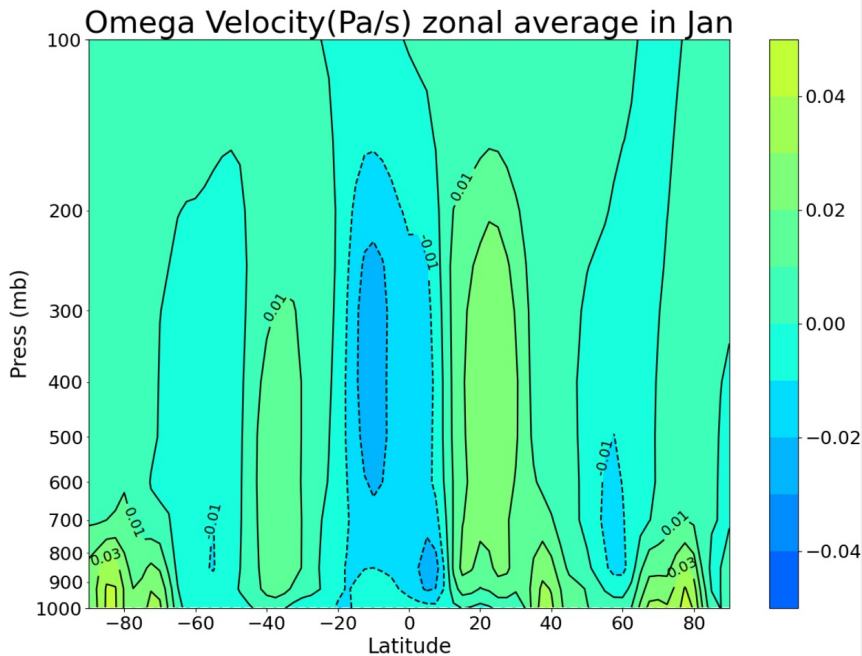


Note:  $w = \frac{Dz}{Dt} \left[ \frac{m}{sec} \right]$  and  $\omega = \frac{DP}{Dt} \left[ \frac{Pa}{sec} \right] \rightarrow \omega = -\rho g w$

- Where is the air ascending/descending in each season?
- Where do you expect to find deserts?

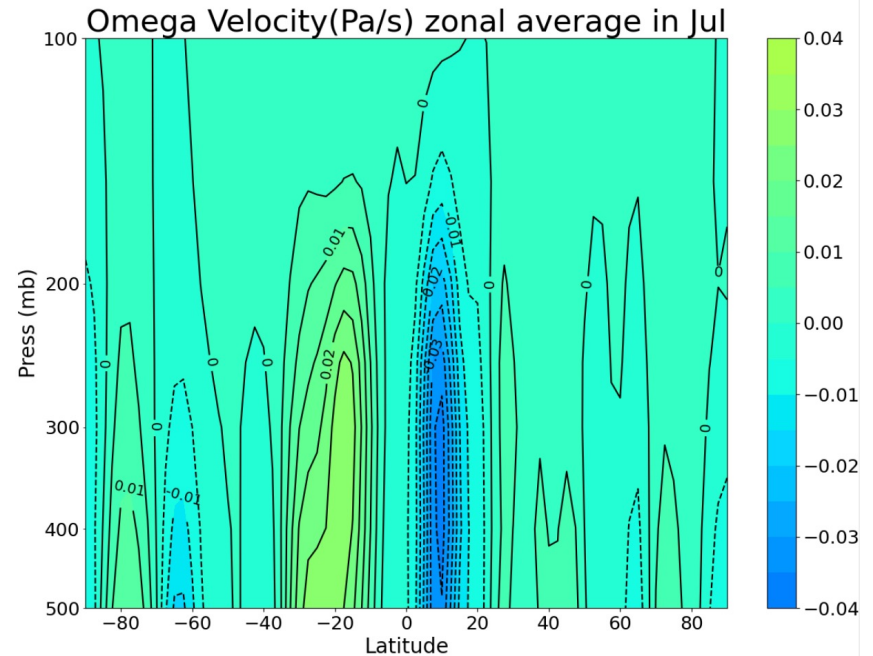
# Zonal mean vertical wind

January



July

Zoom in  
500-100 mb



Note:  $w = \frac{Dz}{Dt} \left[ \frac{m}{sec} \right]$  and  $\omega = \frac{DP}{Dt} \left[ \frac{Pa}{sec} \right] \rightarrow \omega = -\rho g w$

- Where is the air ascending/descending in each season?
- Where do you expect to find deserts?

# Hadley Cell exercise

Plot zonally averaged (January and July):

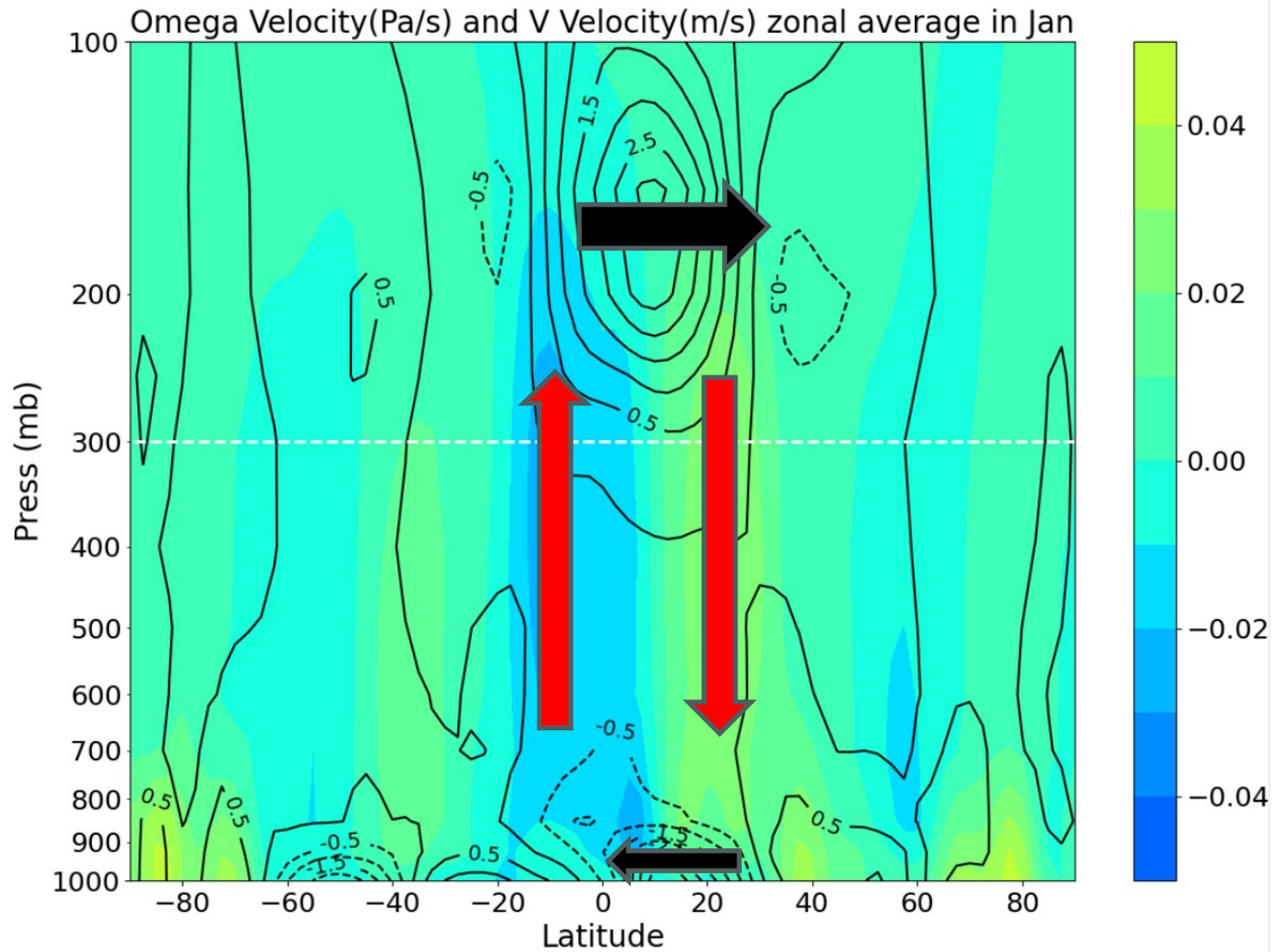
- Temperature (T)
- Meridional velocity ( $v$ )
- Vertical velocity ( $\omega$ ) & Meridional velocity ( $v$ )
- Zonal velocity ( $u$ ) & Meridional velocity ( $v$ )

Work in groups to look for:

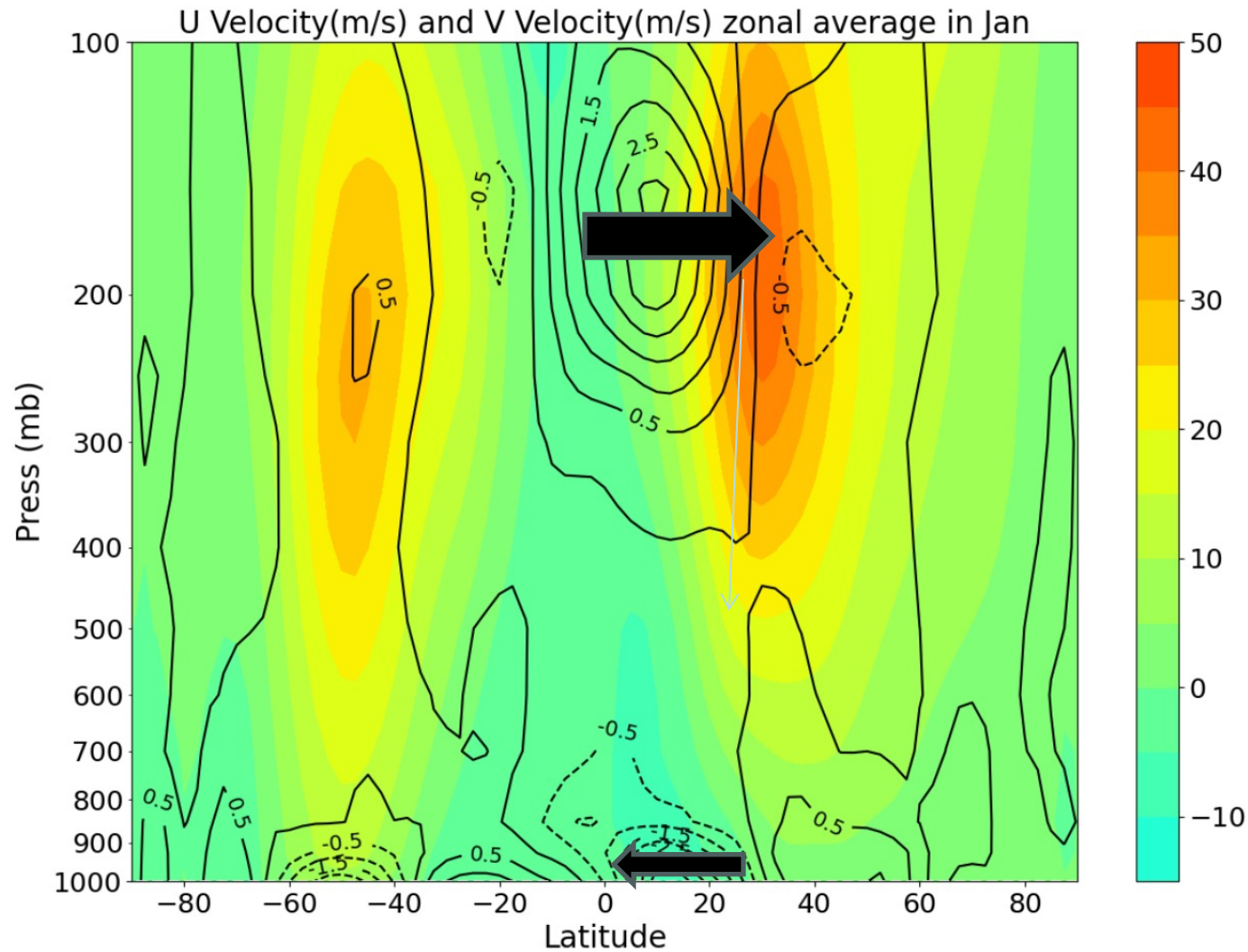
- Evidence of the Hadley cell
- Evidence of the upper-level westerlies and surface easterly (trade winds)
- Can you identify two layers?



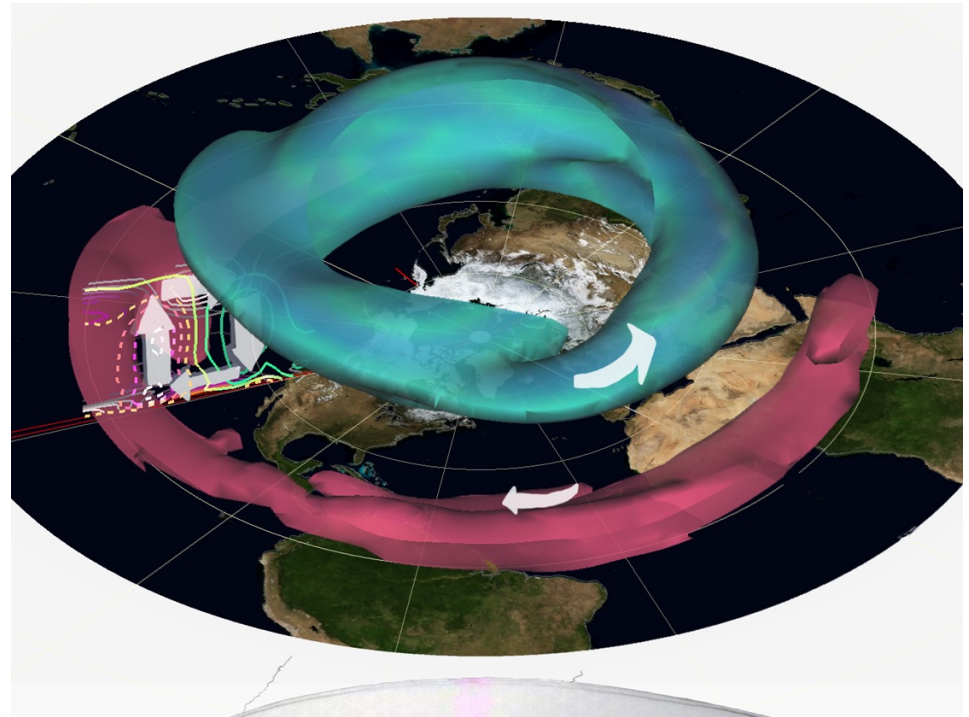
# Hadley Circulation! V and W superimposed



# Hadley Circulation! V and U superimposed

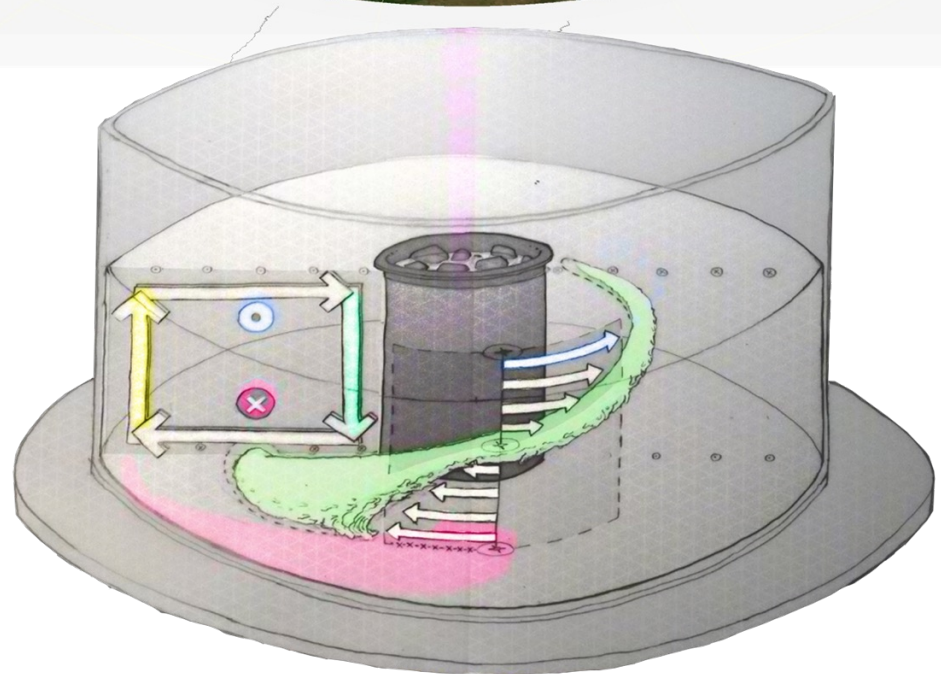


# Connection to the atmospheric circulation



Can we see evidence  
for this circulation in the  
atmosphere?

**Yes!**





*Can we estimate the poleward heat flux that this circulation transports?*

$$\begin{aligned}\overline{\mathcal{H}}_{atmos}^{\lambda} &= \iint \rho v E dA \\ &= a \cos \varphi \int_0^{2\pi} \int_0^{\infty} \rho v E dz d\lambda \\ &\xrightarrow{\rho dz = -dp/g} \frac{a}{g} \cos \varphi \int_0^{2\pi} \int_0^{p_s} v E dp d\lambda ,\end{aligned}$$

$$\overline{\mathcal{H}}_{tropics}^{\lambda} = \frac{2\pi a}{g} \cos \varphi \int_0^{p_s} v (c_p T + gz + Lq) dp$$

Before that, let's introduce an important quantity-

## Potential temperature:

The temperature that a parcel will acquire if it were compressed adiabatically from  $p$  and  $T$  to a standard pressure  $p_0$

$$\theta = T \left( \frac{p_0}{p} \right)^\kappa$$

with  $k = R/c_p = 2/7$  and conventionally  $p_0 = 1000mb$ .

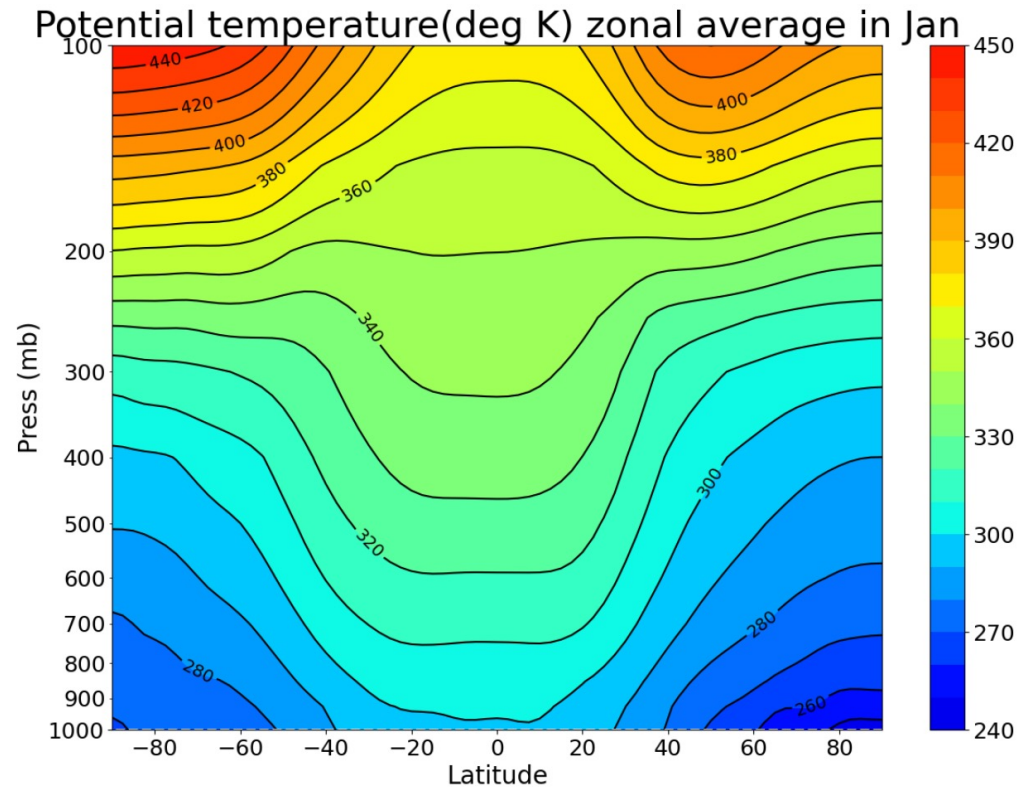
In adiabatic conditions, it follows that:

$$\frac{d\theta}{\theta} = \frac{dT}{T} - k \frac{dp}{p} = 0$$

*Potential temperature is conserved in an adiabatic process!*

Note that for an adiabatic process, it is also exact to write  $C_p\theta = C_pT + gz$

# Potential temperature:



- The poles are still colder, but potential temperature now ***increases*** with height

*Estimate the poleward heat flux using the EsGlobe and the schematic!*

## Meridional Heat transport

$$\begin{aligned}\mathcal{H} &= \rho c_p \int_0^{\infty} \oint \bar{v} \bar{\vartheta} dx dz = \frac{c_p}{g} \int_0^{p_s} \oint \bar{v} \bar{\vartheta} dx dp \\ &= \frac{c_p}{g} \times 2\pi a \cos \varphi \int_0^{p_s} [\bar{v} \bar{\vartheta}] dp\end{aligned}$$

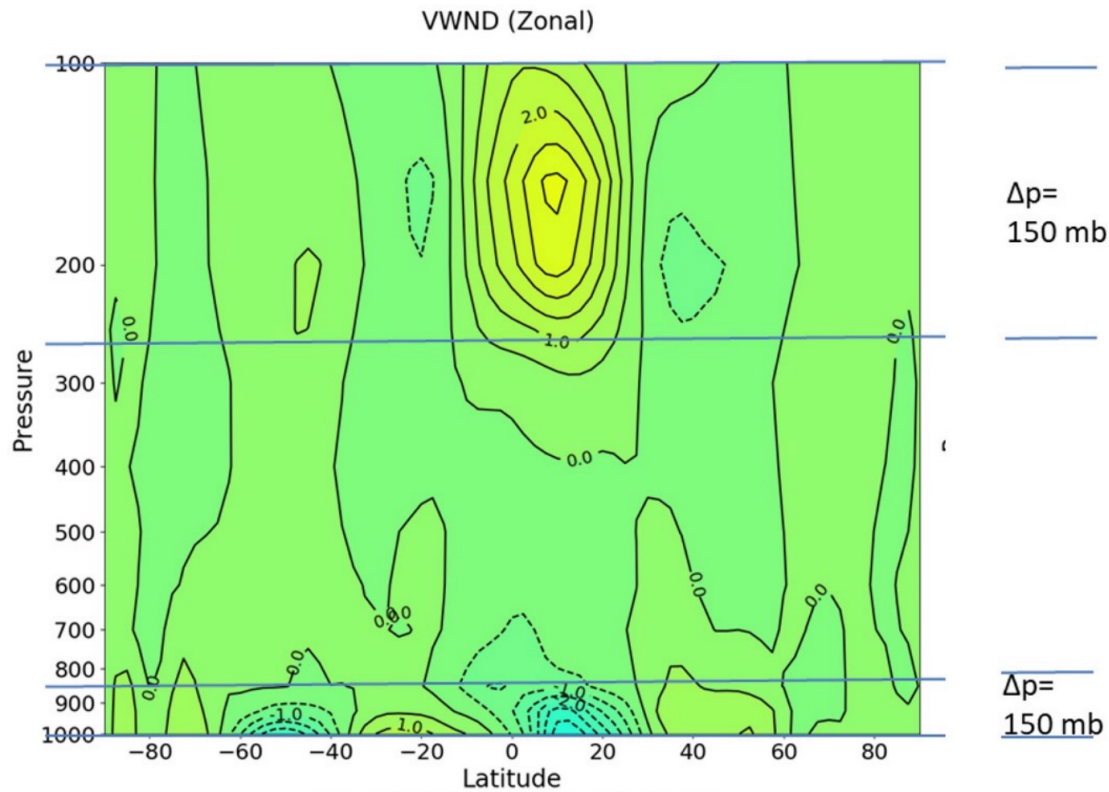
### Note:

- Here we used hydrostatic balance to replace dz with dp:  $\rho dz = -dp/g$
- The integral is from p=0 (top of the atmosphere) to the surface:  $p_s = 1000mb = 10^5 \text{ Pa}$
- The  $2\pi a \cos \varphi$  is related to the zonal averaging at latitude  $\varphi$ , i.e.  $2\pi r$  at radius  $r = a \cos \varphi$



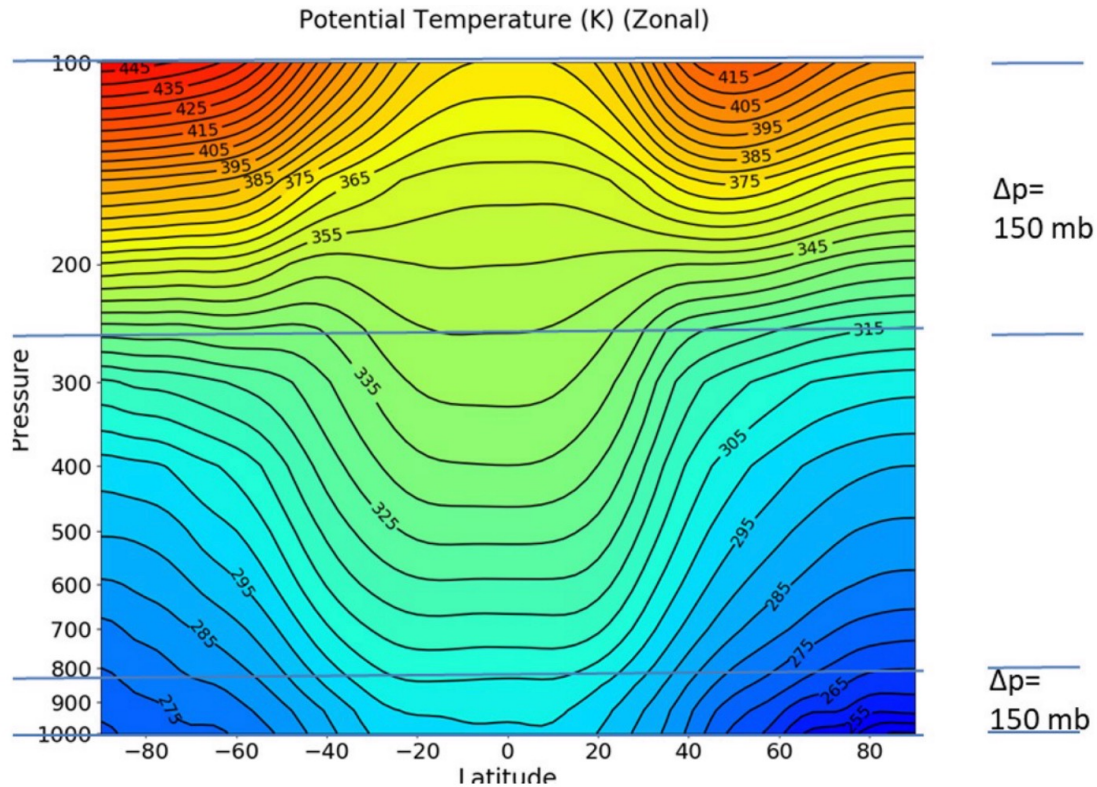
# Two layer model- just like we did in the lab

$$\int_0^{p_s} [\bar{v}][\bar{\vartheta}] dp = ([\bar{v}]_t[\bar{\vartheta}]_t + [\bar{v}]_b[\bar{\vartheta}]_b)\Delta p = [\bar{v}]_t([\bar{\vartheta}]_t - [\bar{\vartheta}]_b)\Delta p.$$

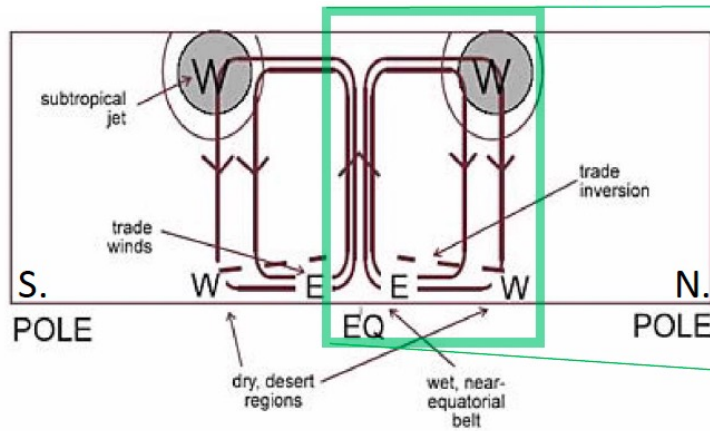


## Two layer model- just like we did in the lab

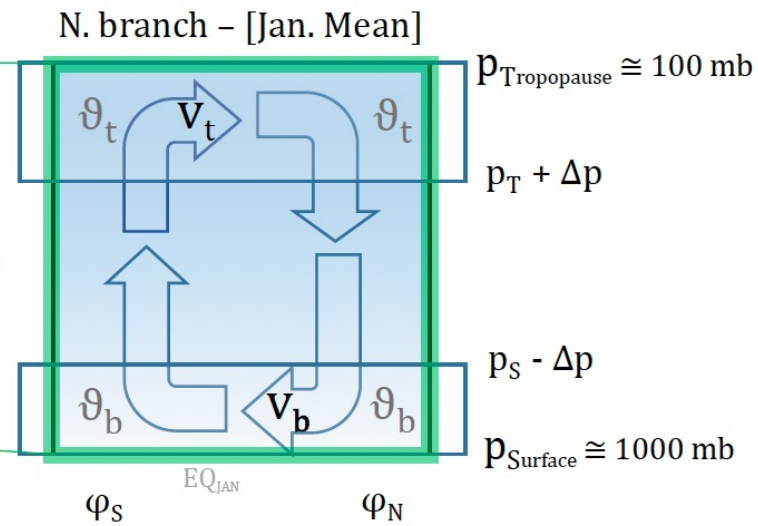
$$\int_0^{p_s} [\bar{v}][\bar{\vartheta}] dp = ([\bar{v}]_t[\bar{\vartheta}]_t + [\bar{v}]_b[\bar{\vartheta}]_b)\Delta p = [\bar{v}]_t([\bar{\vartheta}]_t - [\bar{\vartheta}]_b)\Delta p.$$



# General circulation - Hadley cell



2-LAYER MODEL →



Eqns. 7 → 8 [pg. 4]

$$\mathcal{H} = \rho c_p \int_0^{\infty} \oint \bar{v} \bar{\vartheta} dx dz = \frac{c_p}{g} \int_0^{p_s} \oint \bar{v} \bar{\vartheta} dx dp = \frac{c_p}{g} \times 2\pi a \cos \varphi \int_0^{p_s} [\bar{v} \bar{\vartheta}] dp$$

## Constants

Specific heat (for atmospheric air)

$$c_p = 1005 \text{ J/(kg K)}$$

$$g = 9.8 \text{ m/s}^2$$

$$a \cong 6.4 \times 10^6 \text{ m}$$

(^ Earth's radius)

## Estimate values for:

[ $\bar{v}$  : velocities]

$$\bar{v}_t =$$

$$\bar{v}_b =$$

[ $\bar{\vartheta}$  : potential temp.]

$$\bar{\vartheta}_t =$$

$$\bar{\vartheta}_b =$$

$\varphi$  : latitude

$$\varphi_{\text{avg}} =$$

1 millibar =  $10^2$  Pascals

p : pressure

$$\Delta p =$$

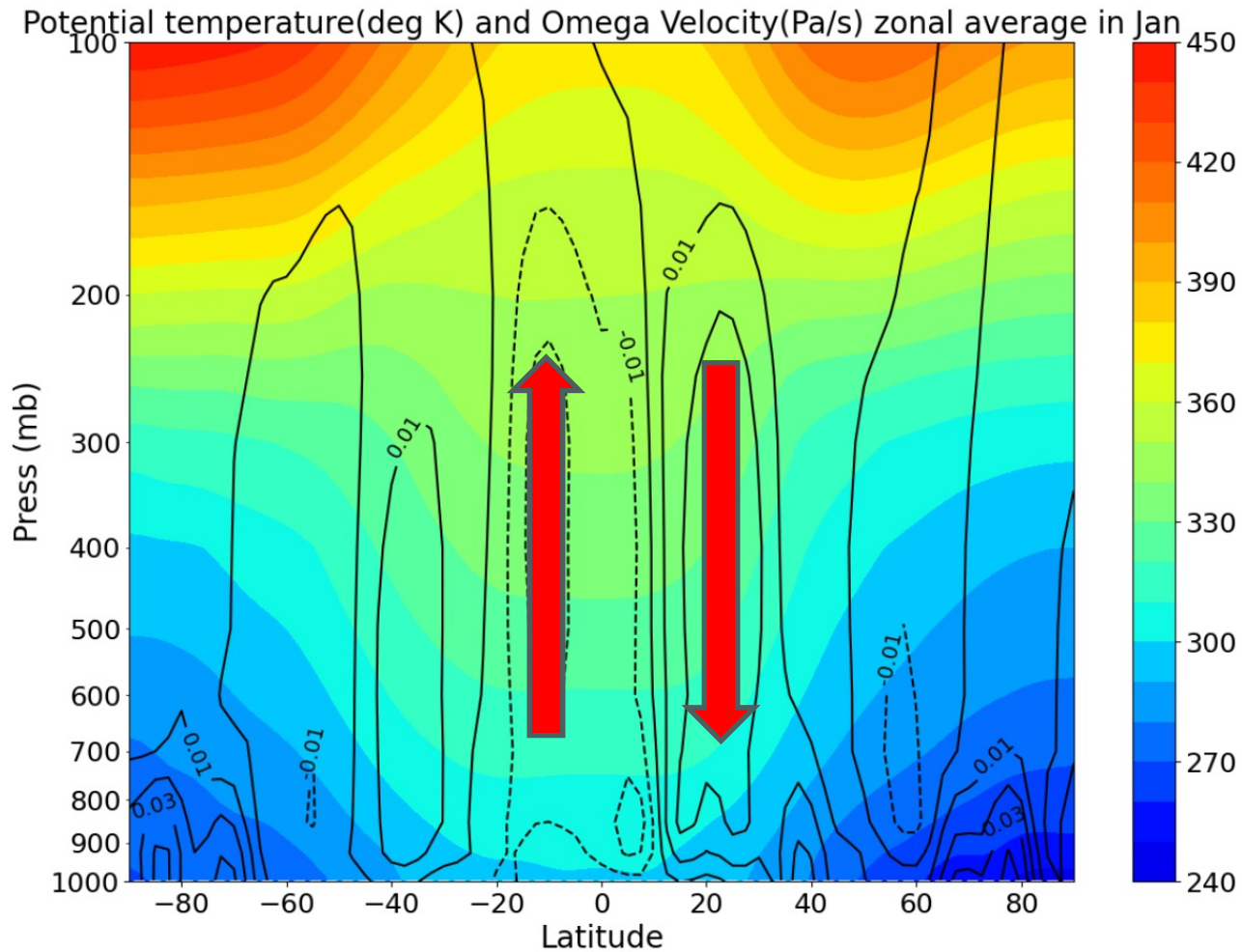
Eqn. 9 [pg. 8]

If  $v_t \cong -v_b$  then..

$$\int_0^{p_s} [\bar{v}] [\bar{\vartheta}] dp = ([\bar{v}]_t [\bar{\vartheta}]_t + [\bar{v}]_b [\bar{\vartheta}]_b) \Delta p \stackrel{\text{If } v_t \cong -v_b \text{ then..}}{=} [\bar{v}]_t ([\bar{\vartheta}]_t - [\bar{\vartheta}]_b) \Delta p$$

→ Express  $\mathcal{H}$  in Petawatts, PW =  $10^{15}$  W.

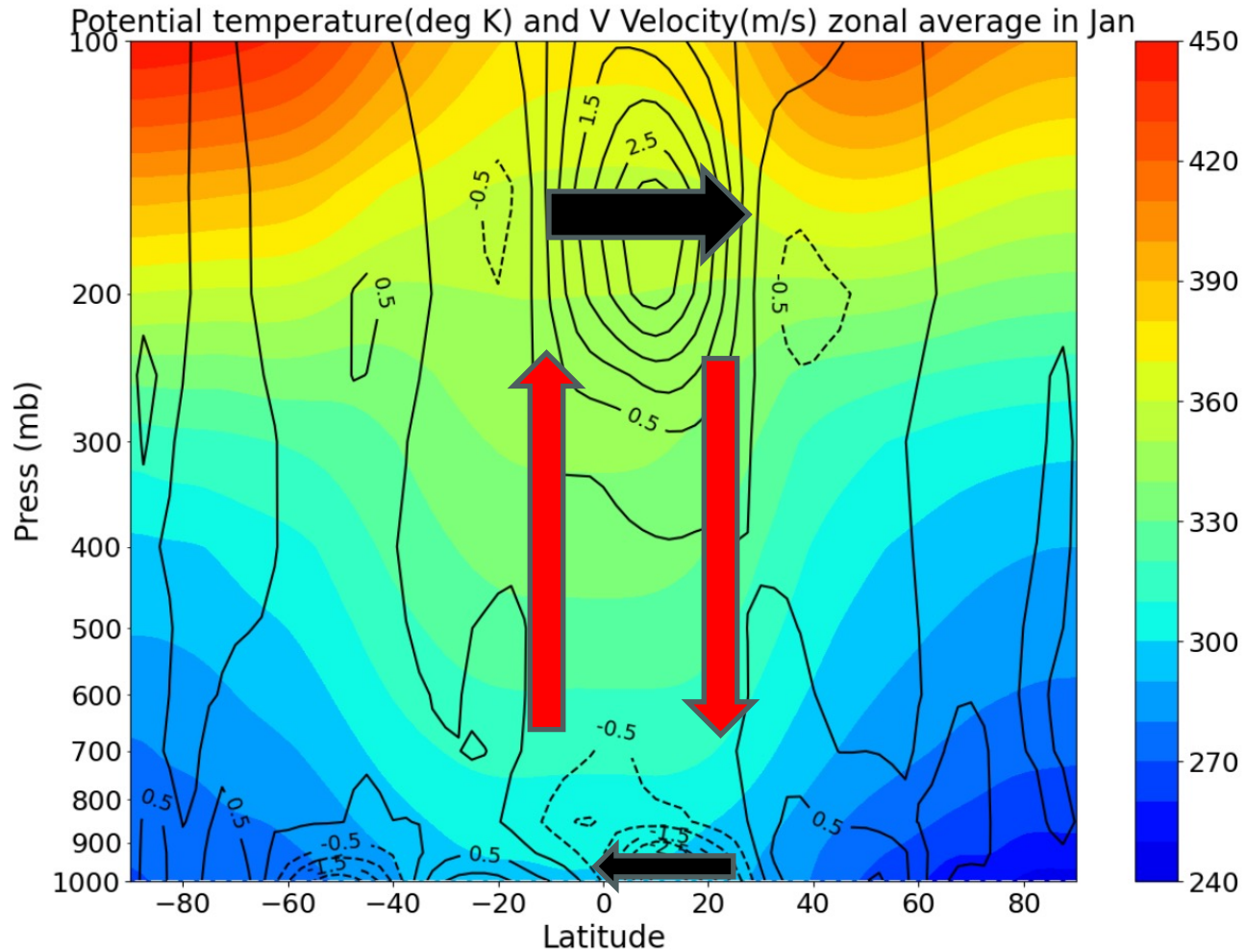
# Two layer model to estimate the heat transport



Tip: plot potential temperature + vertical velocity



# Two layer model to estimate the heat transport



Tip: plot potential temperature + meridional velocity



# 12.307- project 3 (data class 2)

## Last class

- Connection to Hadley tank experiment
- Atmospheric climatology using EsGlobe
- Identify the Hadley circulation
- N-S heat transport in the tropics

## Today

- Heat transport in the tropics (2-layer model)- review calculations
- Moisture climatology and meridional transport
- Eddy-regime in the extra-tropics
- Meridional heat transport by eddies
- Project 4- brief intro

## Meridional Heat transport- two-layer approach:

$$\begin{aligned}\mathcal{H} &= \rho c_p \int_0^{\infty} \oint \bar{v} \bar{\vartheta} dx dz = \frac{c_p}{g} \int_0^{p_s} \oint \bar{v} \bar{\vartheta} dx dp \\ &= \frac{c_p}{g} \times 2\pi a \cos \varphi \int_0^{p_s} [\bar{v} \bar{\vartheta}] dp\end{aligned}$$

$$\int_0^{p_s} [\bar{v}] [\bar{\vartheta}] dp = ([\bar{v}]_t [\bar{\vartheta}]_t + [\bar{v}]_b [\bar{\vartheta}]_b) \Delta p = [\bar{v}]_t ([\bar{\vartheta}]_t - [\bar{\vartheta}]_b) \Delta p.$$

$$\begin{aligned}H &= [(10^3)/10] \times (6 \times 6 \times 10^6) \times 1 \times (2 \times 60) \times (150 \times 10^2) \\ &\approx 6.5 \times 10^{15} \text{ W} = 6.5 \text{ PW}\end{aligned}$$

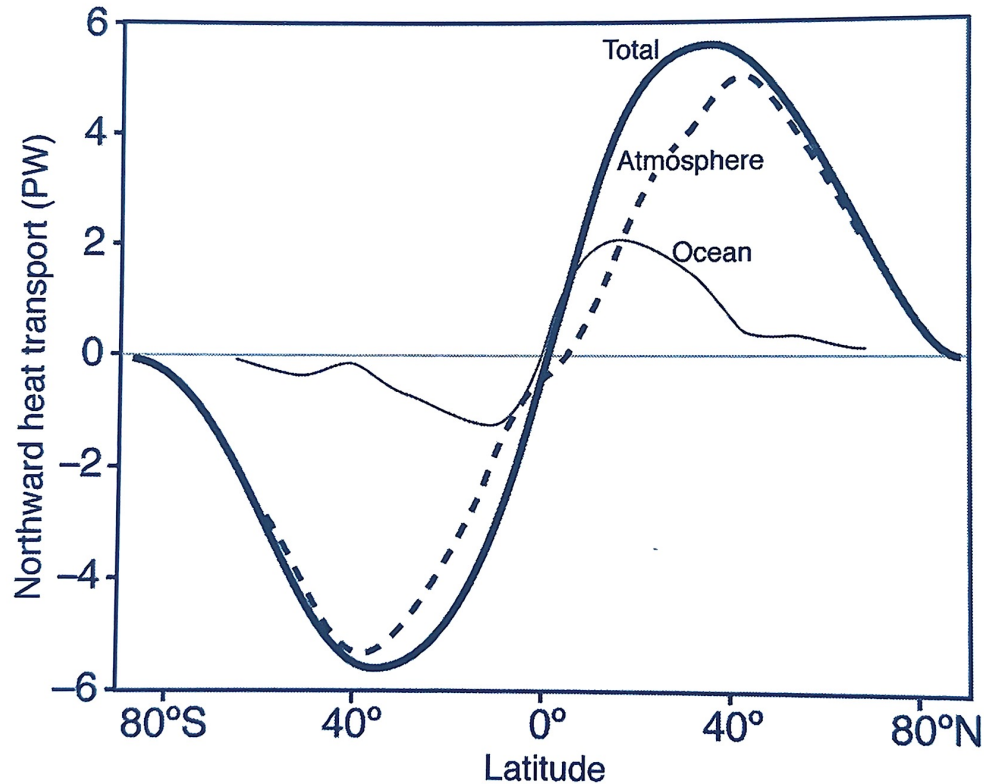
## Meridional Heat transport- two-layer approach:

$$\begin{aligned}\mathcal{H} &= \rho c_p \int_0^\infty \oint \bar{v} \bar{\vartheta} dx dz = \frac{c_p}{g} \int_0^{p_s} \oint \bar{v} \bar{\vartheta} dx dp \\ &= \frac{c_p}{g} \times 2\pi a \cos \varphi \int_0^{p_s} [\bar{v} \bar{\vartheta}] dp\end{aligned}$$

$$\int_0^{p_s} [\bar{v}] [\bar{\vartheta}] dp = ([\bar{v}]_t [\bar{\vartheta}]_t + [\bar{v}]_b [\bar{\vartheta}]_b) \Delta p = [\bar{v}]_t ([\bar{\vartheta}]_t - [\bar{\vartheta}]_b) \Delta p.$$

$$**H \approx 6.5 PW!**$$

Compare our estimates to reanalysis estimates:

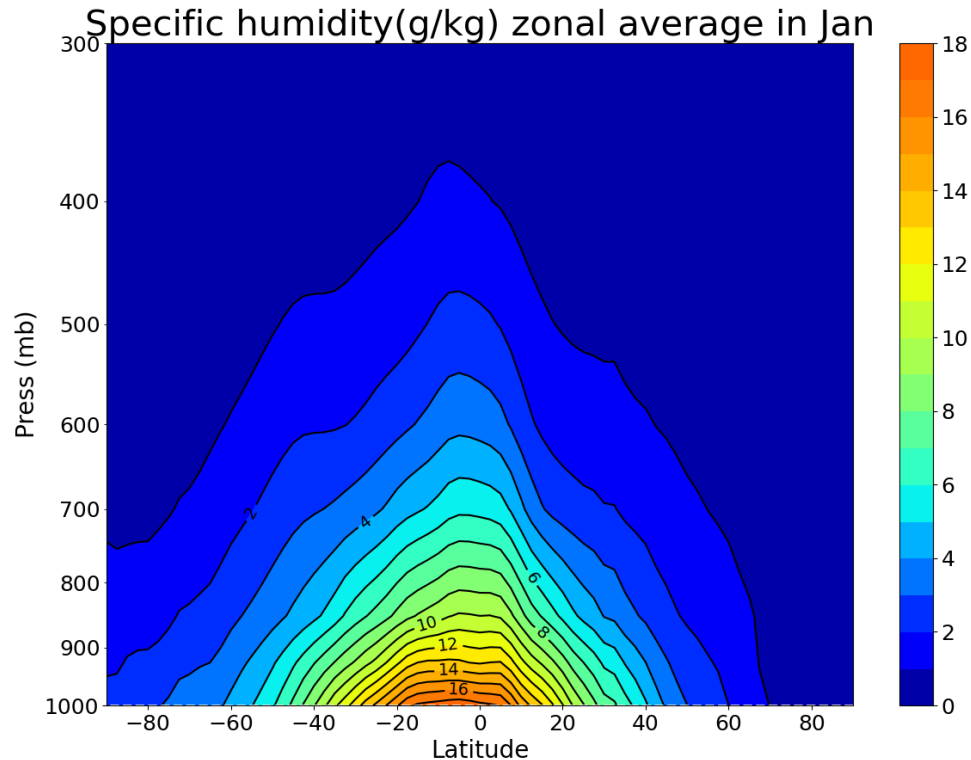


Why do we get 6.5 PW?? seems too high!

We need to consider also latent heating!

# Moisture distribution

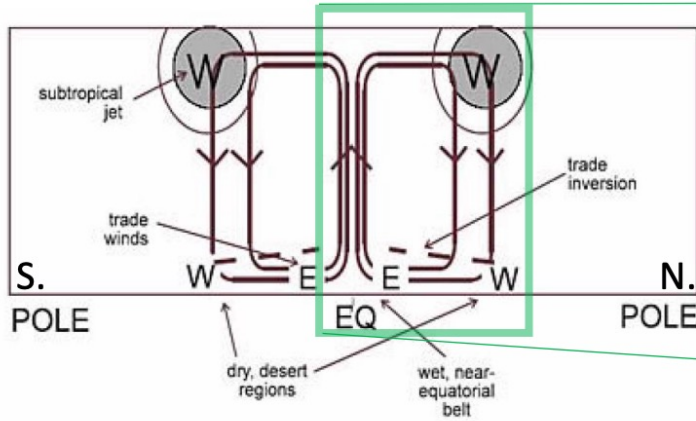
Plot zonally averaged field of **specific humidity (g/kg)**



- **Specific humidity**= amount of water vapour (in grams) in 1kg of air
- Confined to low-levels (note max pressure is 300mb) higher in tropics

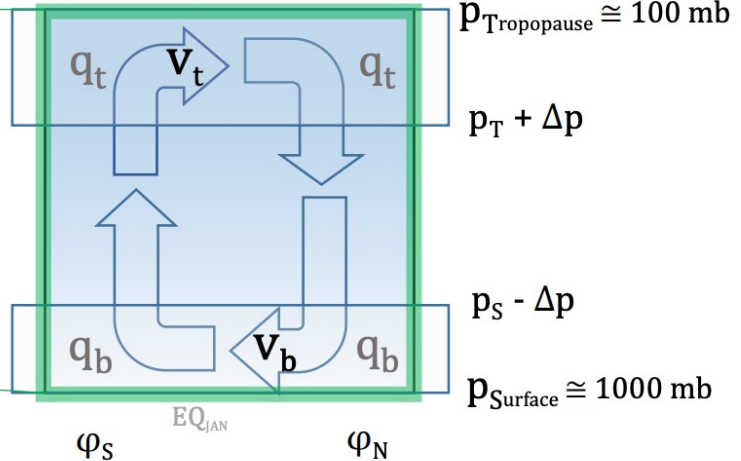


# General circulation – Hadley cell



2-LAYER MODEL →

## N. branch – [Jan. Mean]



### Latent Heat Flux Contribution

Eqn. 10 [pg. 9]

If  $q_t \approx 0$  then...

$$\mathcal{L} = \frac{L}{g} \times 2\pi a \cos \varphi \int_0^{p_s} \bar{v} \bar{q} dp \approx \frac{L}{g} \times 2\pi a \cos \varphi [\bar{v}]_b [\bar{q}]_b \Delta p.$$

- Constants** (for atmospheric air)
- Latent heat of fusion
  - $L = 2.25 \times 10^6 \text{ J/kg}$
  - $g = 9.8 \text{ m/s}^2$
  - $a \approx 6.4 \times 10^6 \text{ m}$  (^ Earth's radius)

- Estimate values for:
- [ $\bar{v}$  : velocities]
  - $\bar{v}_t =$
  - $\bar{v}_b =$

Spec. humidity  $q$  is units of **g/kg**  
Use MKS system for calculations.

- [ $\bar{q}$  : specific humidity]
- $\bar{q}_t =$
- $\bar{q}_b =$

- $\varphi$  : latitude
- $\varphi_{\text{avg}} =$

- 1 millibar =  $10^2$  Pascals
- $p$  : pressure
- $\Delta p =$

Tip: convert specific humidity to kg/kg

→ Express  $\mathcal{L}$  in Petawatts,  $\text{PW} = 10^{15} \text{ W}$ .

Total Heat Flux =  $\mathcal{H} + \mathcal{L}$

## Meridional transport of moisture

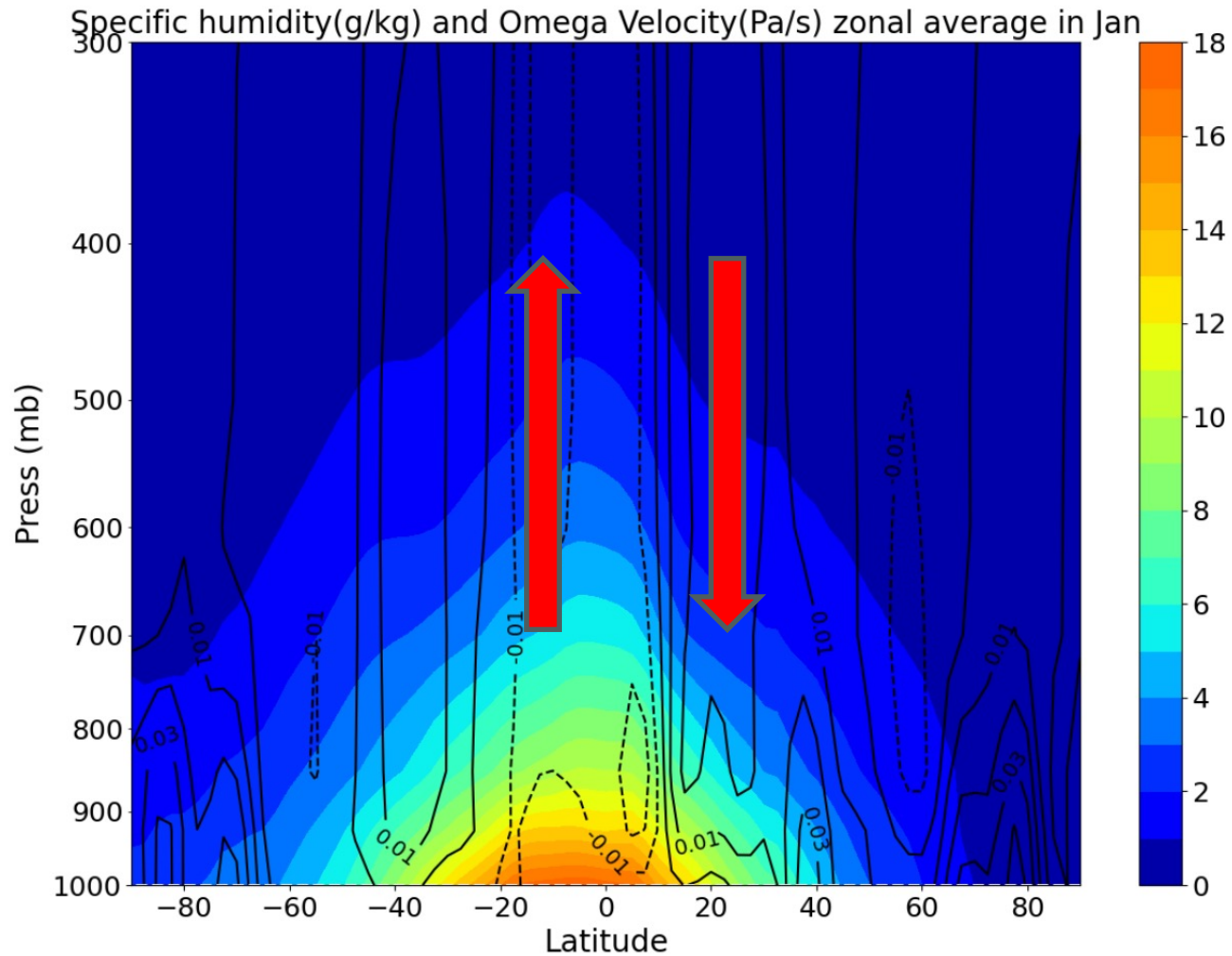
$$\mathcal{L} = \frac{L}{g} \times 2\pi a \cos \varphi \int_0^{p_s} \overline{vq} dp$$

Two layer  
approximation

$$\approx \frac{L}{g} \times 2\pi a \cos \varphi [\overline{v}]_b [\overline{q}]_b \Delta p.$$

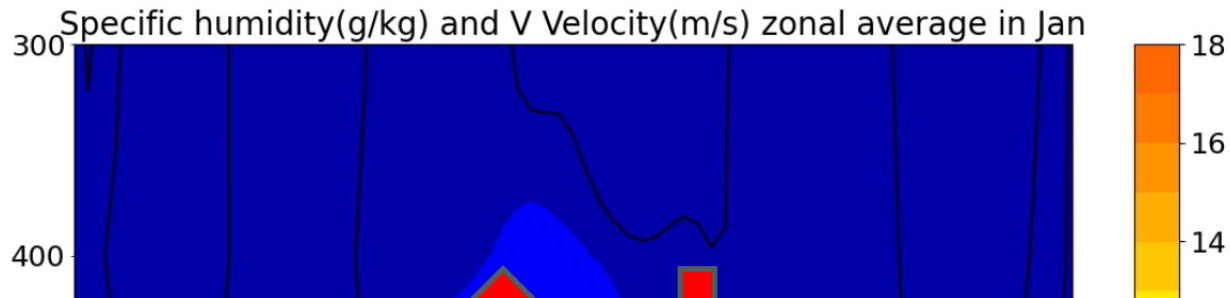
# Meridional transport of moisture

$$\mathcal{L} \simeq \frac{L}{g} \times 2\pi a \cos \varphi [\bar{v}]_b [\bar{q}]_b \Delta p.$$

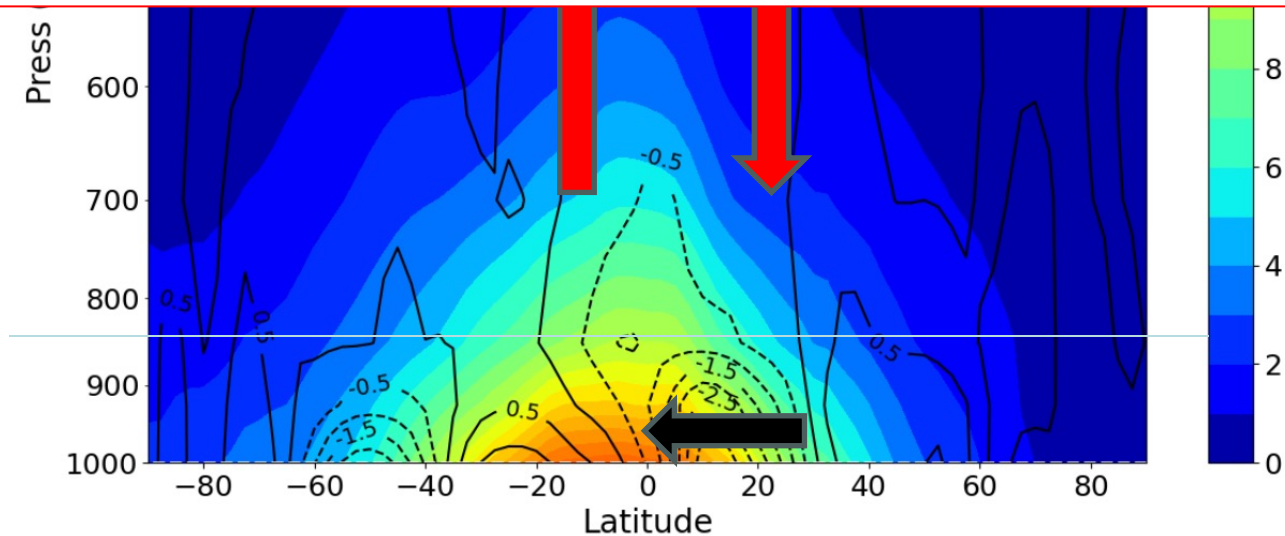


# Meridional transport of moisture

$$\mathcal{L} \simeq \frac{L}{g} \times 2\pi a \cos \varphi [\bar{v}]_b [\bar{q}]_b \Delta p.$$



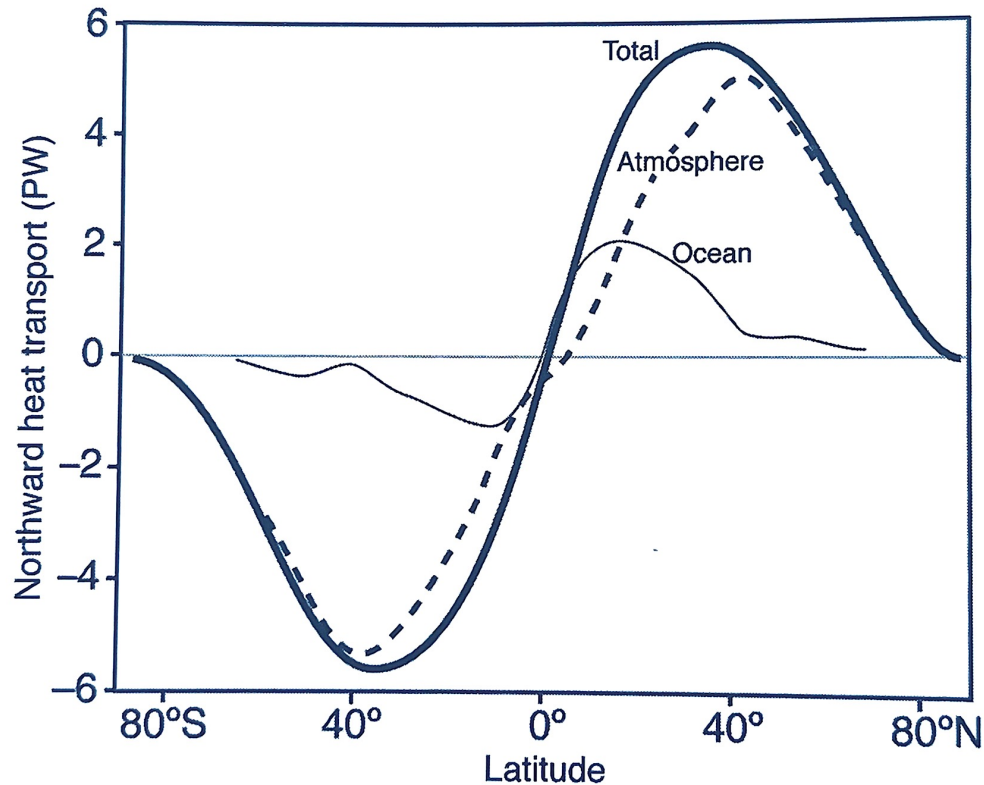
The moisture transport is negative (equatorward), since  $v$  is negative and moisture is larger near the surface!



$$L = [(2.25 \times 10^6) / 10] \times (6 \times 6 \times 10^6) \times 1 \times (-2 \times 13 \times 10^{-3}) \times (150 \times 10^2)$$

$$= 5.4 \times 10^{15} \text{ W} = -3 \text{ PW}$$

Compare our estimates to reanalysis estimates:



Total heat transport = H + L  $\sim 6.5 - 3 = 3.5$  PW

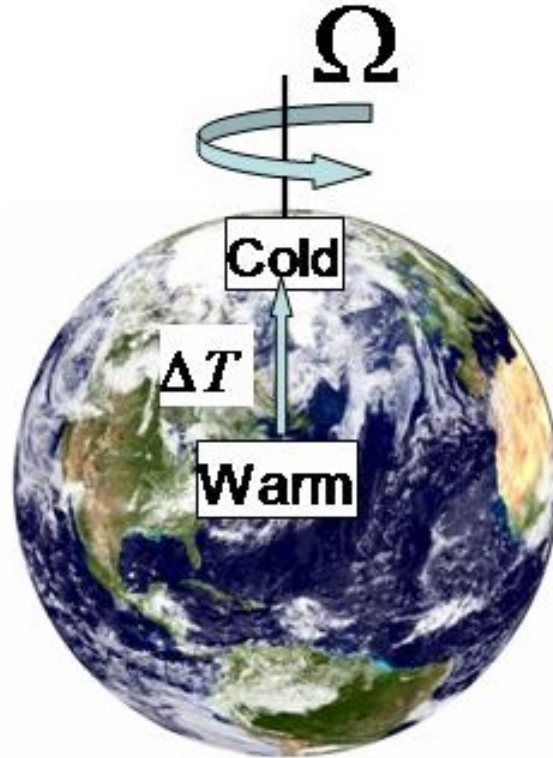
→ Not a bad rough estimation!



What about the midlatitudes, where the “eddy regime” is dominating?

# General Circulation of the atmosphere

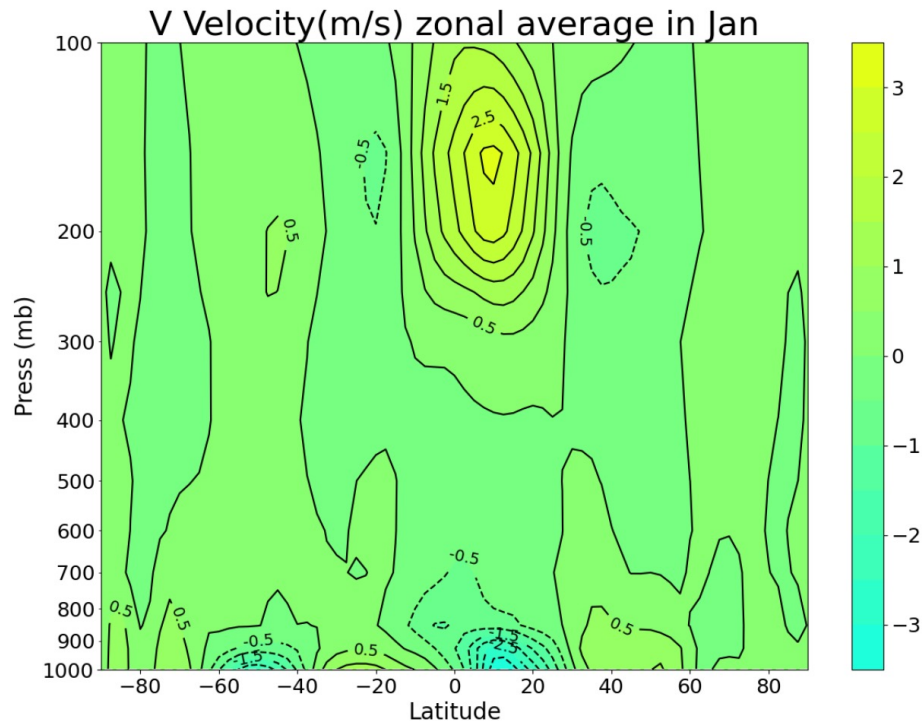
1. Pole – Equator Temperature Difference
2. Earth rotation



| Two experiments  | Two regimes                      |
|--|----------------------------------|
| $\Omega = \text{large}$<br>$\Delta T = \text{large}$ → | Mid-latitude weather systems     |
| $\Omega = \text{small}$<br>$\Delta T = \text{large}$ → | Tropical Hadley cell circulation |

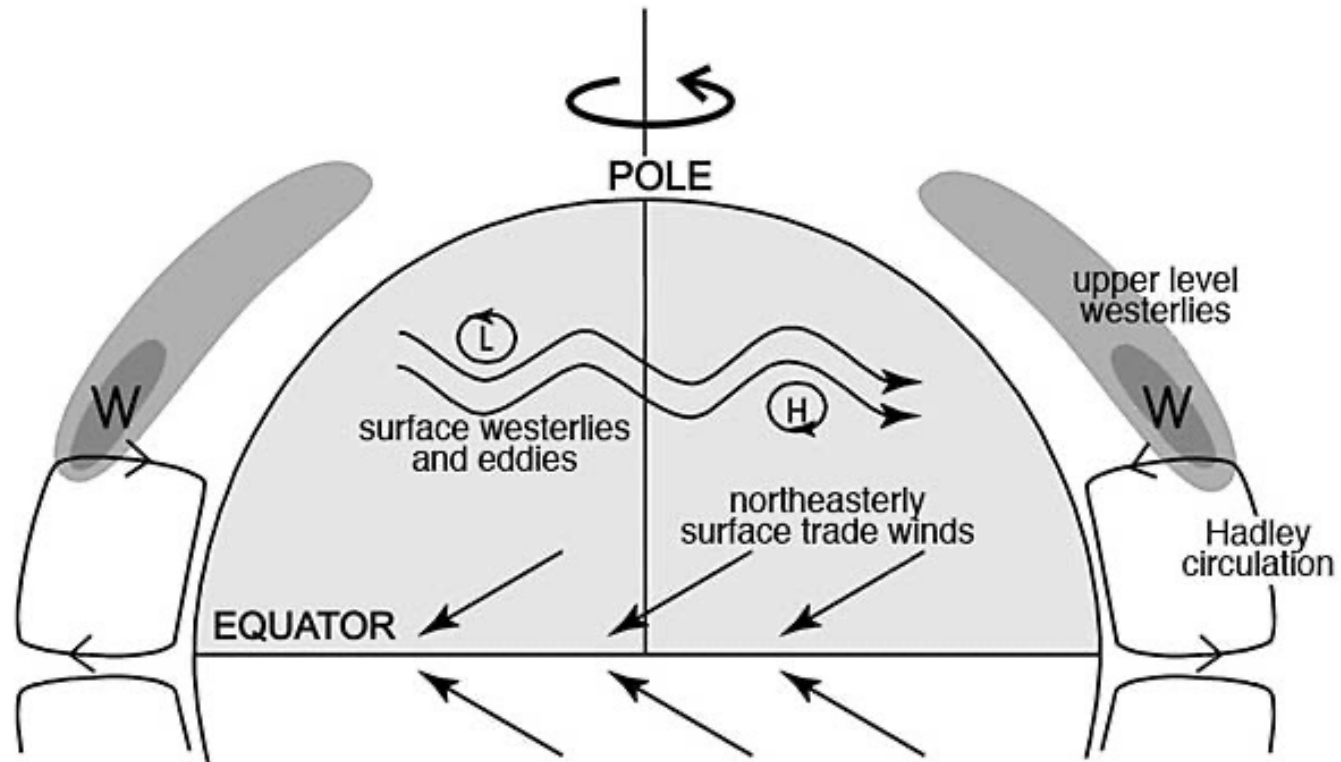
Laboratory abstraction of Earth's weather

Let's look again at the mean  $V$  structure:



- $V$  is mainly large in the tropics (in the two 'layers') but generally very small in the midlatitudes (weak 'Ferrel Cell')
- So how can heat be transported poleward??
- In the midlatitudes,  $\overline{VT}$  is small since  $\overline{V}$ , but in fact  $\overline{V'T'}$  is not!

# Schematic of Earth's global circulation

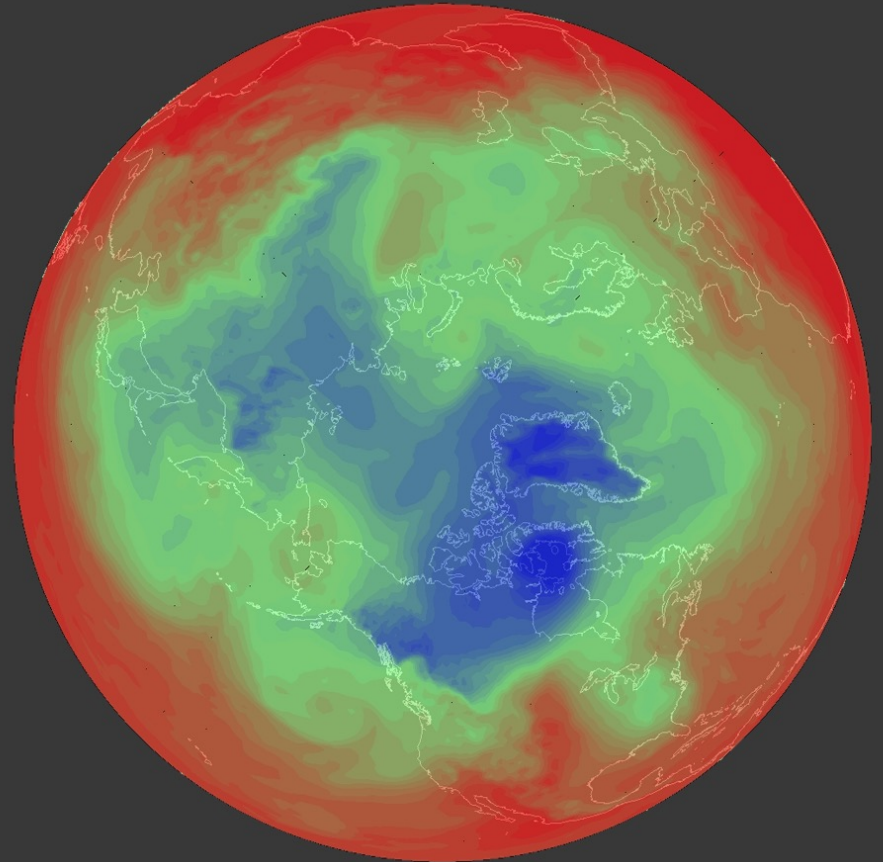
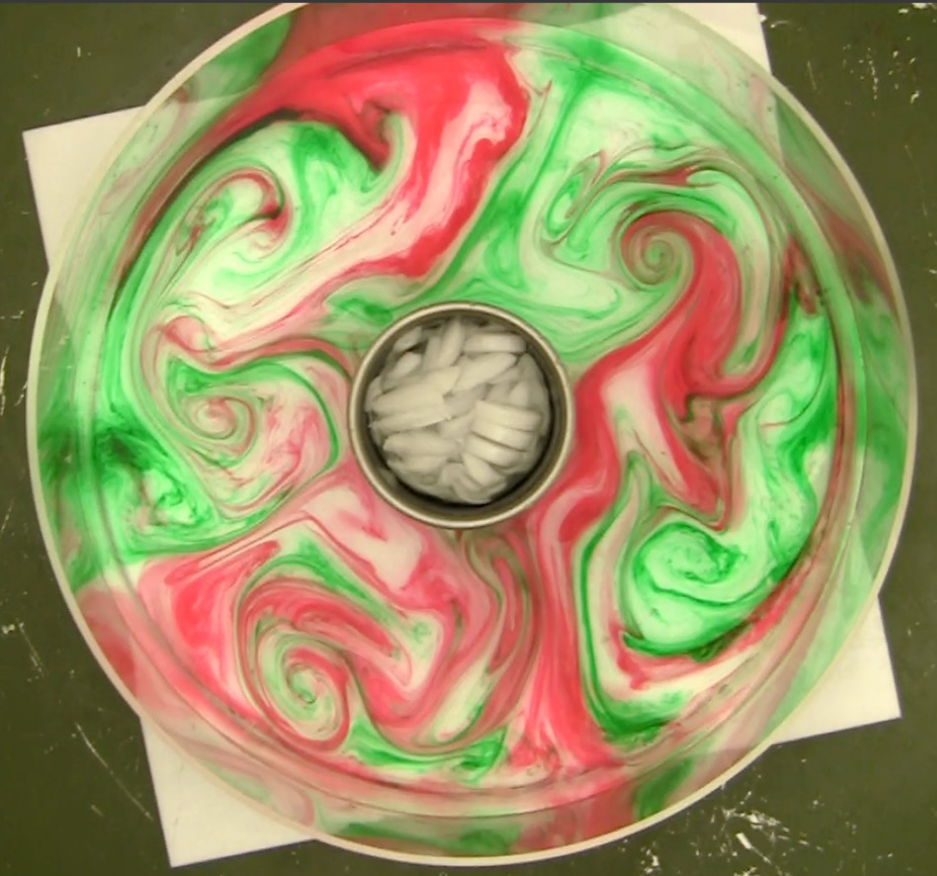


# Eddies regime

**Weather Systems**

**$\Omega = \text{large}$**

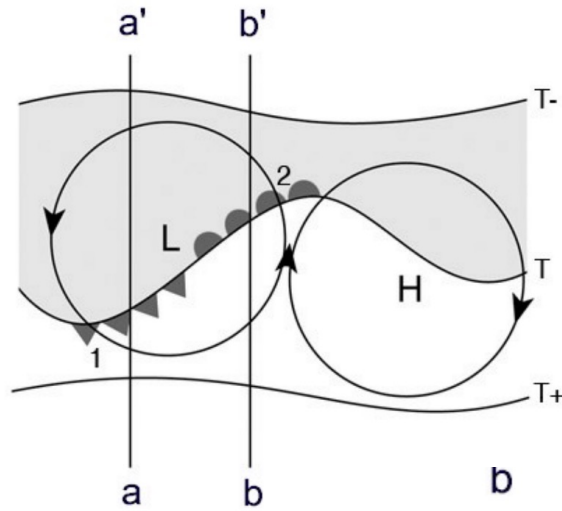
**$\Delta T = \text{large}$**



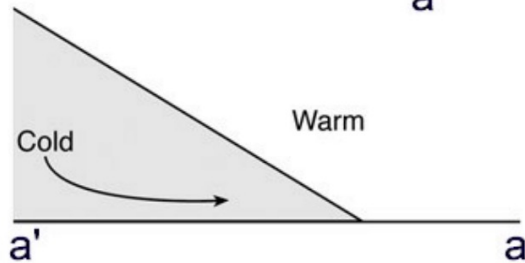
How do midlatitude eddies  
transfer heat poleward?



# How do midlatitude eddies transfer heat poleward?



**Cold front**



**Warm front**

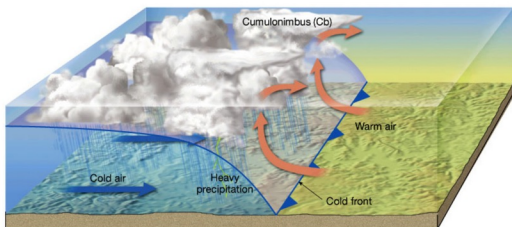
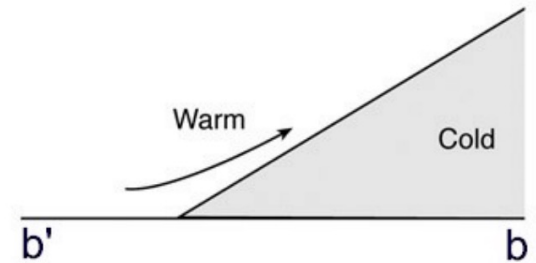


Figure 9.6 in *The Atmosphere, 8th edition*, Lutgens and Tarbuck, 8th edition, 2001.

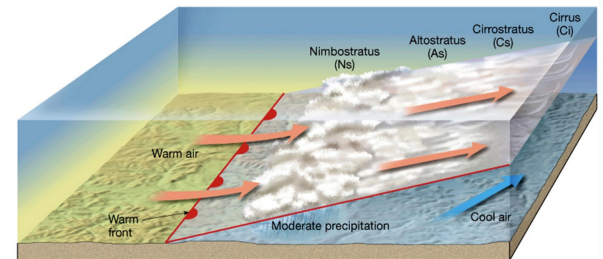
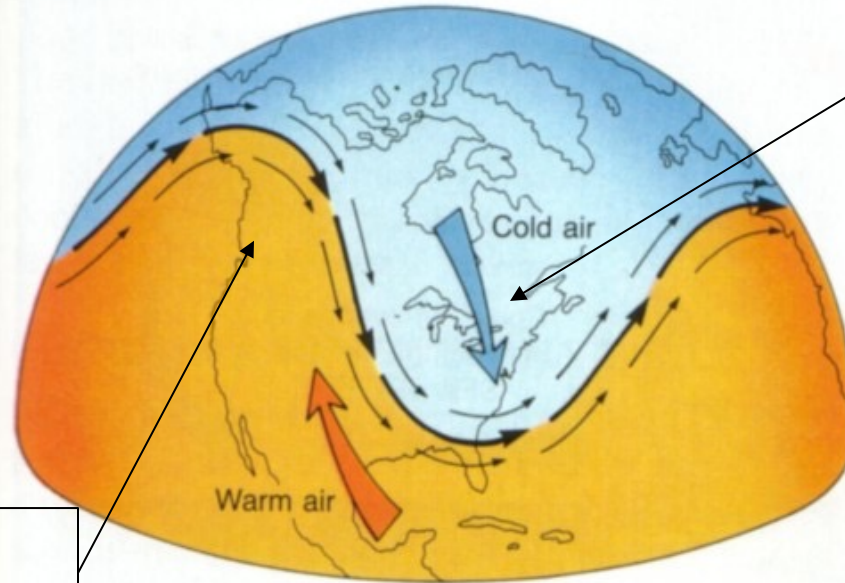


Figure 9.6 in *The Atmosphere, 8th edition*, Lutgens and Tarbuck, 8th edition, 2001.

# How do midlatitude eddies transfer heat poleward?



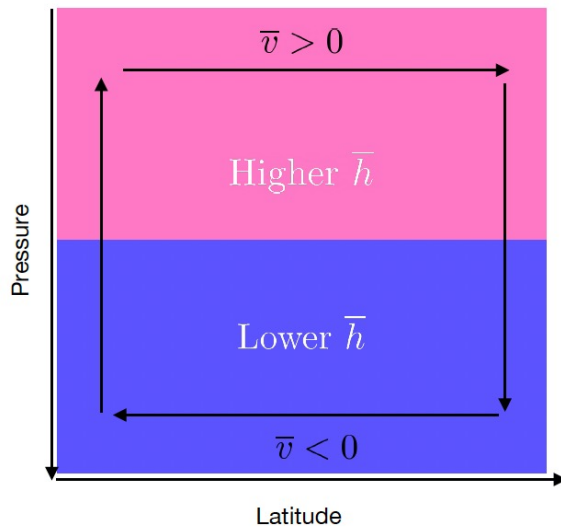
$v' < 0$  negative  
 $T' < 0$  negative  
 $v'T' > 0$  positive

$v' > 0$  positive  
 $T' > 0$  positive  
 $v'T' > 0$  positive

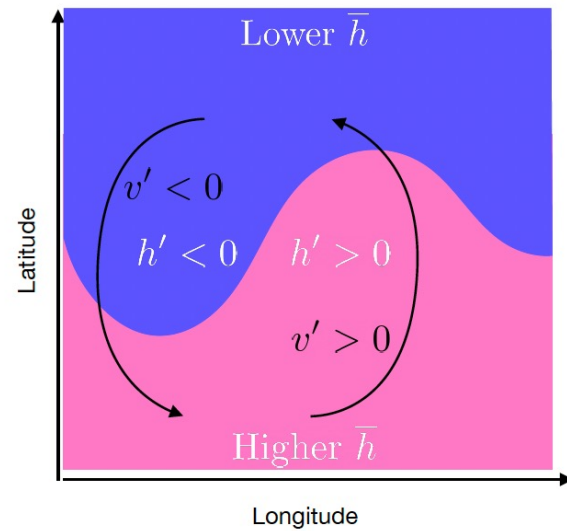
- Warm air is transported poleward, cold air is transported equatorward
- Hence, in both cases, the heat flux is positive (poleward), and acting to reduce the background temperature gradient

# Mechanisms for poleward heat transport

$$h = c_p T + gz + L_v q,$$



Hadley overturning  
circulations



Midlatitude eddies

$$\overline{vh} = \overline{v\bar{h}} + \overline{v'h'}$$

# Energy transport in the atmosphere

## *Exercise*

$$\begin{aligned} H &= \rho \iint v h dA \rho \iint v h dz dx \\ &= a \cos \varphi \int_0^{2\pi} \int_0^{\infty} v h dz d\lambda \\ &= \frac{a}{g} \cos \varphi \int_0^{2\pi} \int_0^{p_s} v h dp d\lambda \\ &= \frac{2\pi a}{g} \cos \varphi \int_0^{p_s} [v h] dp \end{aligned}$$

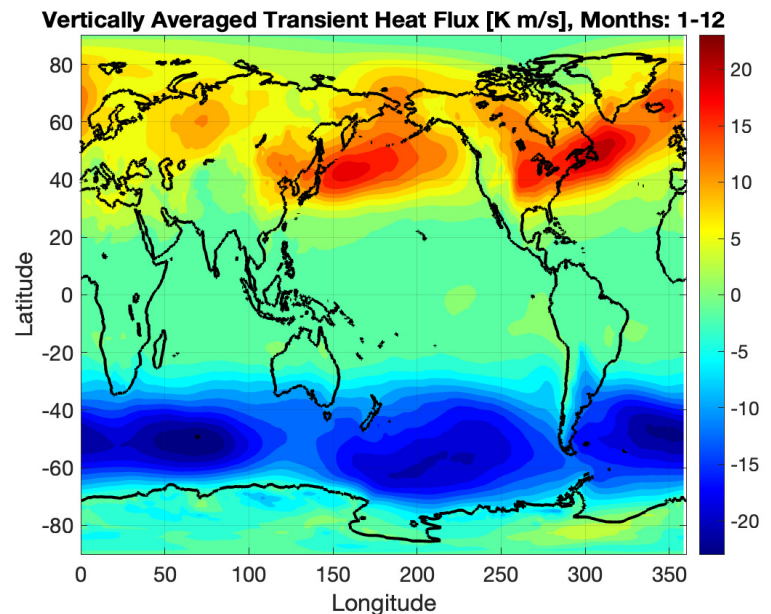
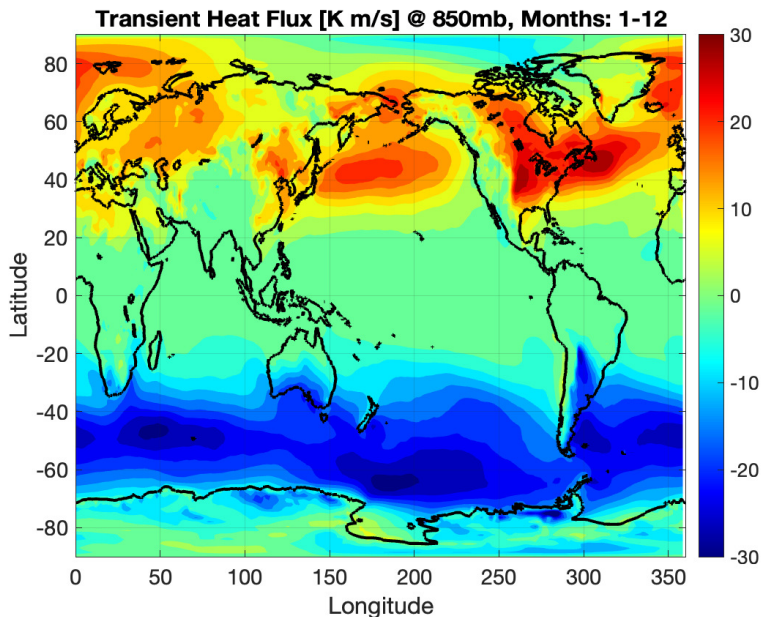
$$H = \frac{2\pi a}{g} \cos \varphi \int_0^{p_s} (c_p [v\theta] + L_v [vq]) dp$$

# Transient energy transport in the atmosphere- *Exercise*

$$H = \frac{2\pi a}{g} \cos \varphi \int_0^{p_s} (c_p [\overline{v'\theta'}] + L_v [\overline{v'q'}]) dp$$

- Go to Project 3 Observation Data page:  
<http://weatherclimatelab.mit.edu/projects/heat-and-moisture-transport/observation-data>
- Press the link “[Instructions for plotting transient heat fluxes](#)”
- Download the data file, and the Matlab/Python scripts
- Follow the instruction only and inside the scripts

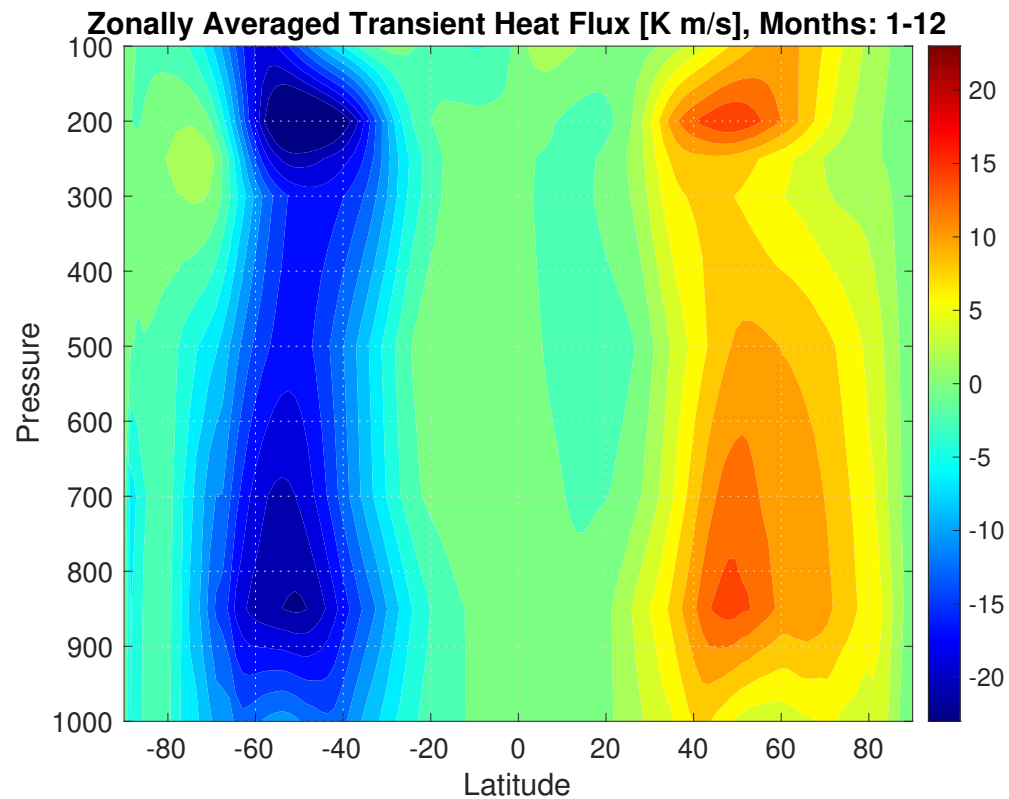
- The data supplied: annual mean  $\overline{v'\theta'}$  and  $\overline{v'q'}$  from the ERA5 Reanalysis data over the years 2010-2020
- The script should produce the transient heat flux [K m/s] at a chosen level (e.g., 850 mb below) and vertically averaged





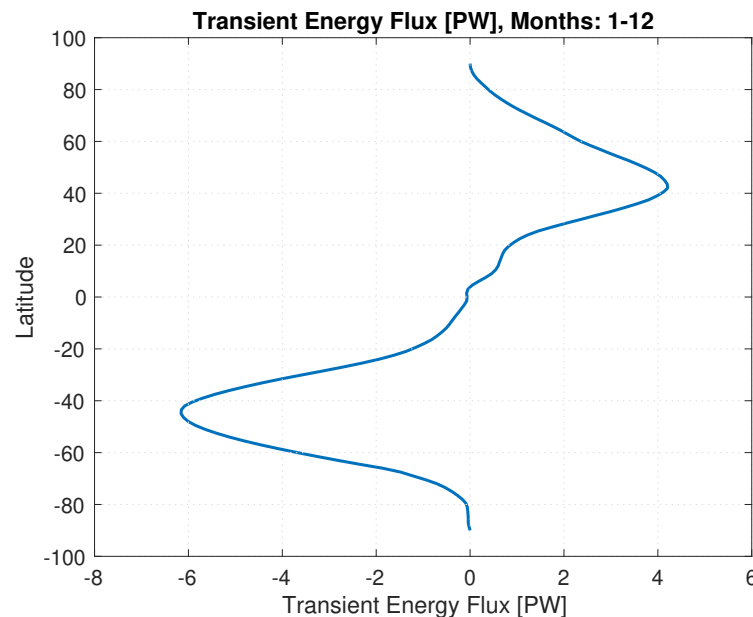
## *What you need to do:*

- Calculate and plot the zonal mean transient heat flux



## What you need to do:

- Calculate and plot the total transient poleward energy flux



$$H = \frac{2\pi a}{g} \cos \varphi \int_0^{p_s} (c_p [\overline{v'\theta'}] + L_v [\overline{v'q'}]) dp$$

## Comments about reports

- No need to repeat all the theory in the notes!! Only the relevant equations that you actually use to calculate things

### *Report 2-*

- Atmosphere: dust advection, front (optional), temperature variability (explain variance and gradient connection, explain why variance decreases)

### *Report 3-*

- Hadley cell: proof of existence (figures from EsGlobe), heat transport in the Hadley cell and in the midlatitudes

## Project 4- dig deeper!

- Go back and dig deeper into one of the projects, or come up with another project
- Should be short as there is not much time
- Next class we will brainstorm ideas for projects

Initial thoughts on the Dig Deeper project:

- Lab/observations data?
- Atmosphere/ocean/fluid dynamics more generally?
- Previous projects/new project?

## Some ideas-

- Tornados (we have a dataset)
- Ocean currents
- New lab experiments (Weather in a Tank website for ideas, e.g., Fronts, Taylor-Proudman columns)
- CMIP6 climate change simulation data (temperature, model-to-model spread, year-to-year variability...)
- ERA5 reanalysis data (e.g., seasonal variation of poleward heat flux)
- Extratropical cyclones (dataset of storm tracks)
- Migration of the Hadley Cell
- ...