3 Vortices in the atmosphere

We will make use of what we have learned about the nature of laboratory vortices in rotating systems to explore atmospheric vortices using atmospheric data. Just as in our study of laboratory vortices, the Rossby number will be the key non-dimensional number that threads through our exploration. We begin by estimating the Rossby number in atmospheric vortices on large and small scales.

3.1 Examples of intense atmospheric vortices on large and small scales

The atmosphere is full of swirling wind patterns which often comprise intense vortex structures, as can be seen in Fig.8, a global IR satellite image of clouds on Feb 11, 2019. We observe vortical patterns of varying sizes, from large ones with scales of thousands of kilometers to small-scale vortices within which are embedded intense convective clouds clusters and thunderstorms. Tornadoes, which have a scale of only few km, can often develop in regions of severe thunderstorms, but are too small to be seen in such global images.

Many types of atmospheric vortices exist, which can be organized as a function of scale, from large to small, as listed below:

The Jet Stream (scale = 3000 km): a current of fast-moving winds at the height of 10 km or so, flowing from west to east around a low pressure area located over the cold polar regions. It is sometimes called the "Polar Vortex" — see Fig.9 and accompanying video. A similar jet stream flows around the South Pole.

Blizzards (scale = 1000 km) — winter snow storms associated with strong winds circulating anti-clockwise around a low pressure center. They tend to develop along the "Polar Front", a mid-latitude region of strong temperature gradient, marking the boundary between cold polar air and warm tropical air — see Fig.10.

Hurricanes (scale = few 100s km): — tropical storms associated with very strong winds circulating anti-clockwise around a very low pressure center, the 'eye' of the hurricane. Hurricanes are fueled by energy in warm surface waters of the ocean and tend to occur in the summer/fall season — see Fig.11.

Tornados (scale = 1 km) — small-scale vortices with extremely strong, damaging winds, which can develop out of strong thunderstorms — see Fig.12. In a tornado the air can swirl either clockwise or anti-clockwise.

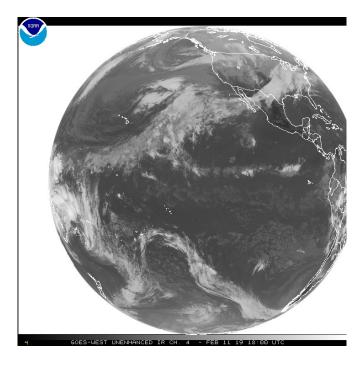


Figure 8: A global satellite image of Earth from Feb 11, 2019. The white areas are clouds and the darker areas clear sky. You can view an accompanying movie loop here: https://www.goes.noaa.gov/dml/west/fd.

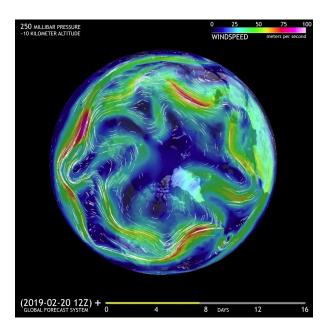


Figure 9: The jet stream at 250 HPa (at a height of, roughly, $10\,\mathrm{km}$) as seen on Feb 20, 2019. The areas shaded in red correspond to wind speeds that exceed $50\,\mathrm{m\,s^{-1}}$. The jet stream is in constant motion, as the 'ribbon' of intense winds undulates north and south, as can be seen in the accompanying movie - see https://vimeo.com/318678158 .



Figure 10: A satellite image of clouds showing the system that brought the blizzard of January 4, 2018 to the east coast. We see cold air moving down from the Arctic on the west of the system and warm air moving up from the tropics on the east — for more see: https://www.weather.gov/okx/Blizzard_Jan42018.



Figure 11: Hurricane Harvey (category 5) which reached landfall on the coast of Texas on August 25, 2017 — for more see: https://earthobservatory.nasa.gov/images/90822/hurricane-harvey-approaches-texas



Figure 12: A tornado in Iowa on July 19, 2018, one of 19 tornadoes that developed over the central planes. For more see: https://www.weather.gov/dmx/20180719 Tornadoes.

3.2 Estimating the Rossby number as a function of scale

We will now estimate the Rossby number of various atmospheric vortices, in a manner which is exactly analogous to that used in our laboratory experiments in Section 1.1. Rather than using paper dots, we will launch 'virtual' particles in to the evolving wind patterns using the EsGlobe, an interface for displaying and interacting with data — 12.307 website.

Planetary scale – the jet stream. Use the EsGlobe particle tracking interface to explore how long it takes for a parcel of air in the jet stream to circumnavigate the globe (set level = $10 \,\mathrm{km} \sim 250 \,\mathrm{mb}$, where the jet speed typically reaches a maximum). Estimate the $R_{timescales}$ (as a ratio of time scales) defined by Eq.(1). Note that the Rossby number, Eq.(12), is given by $R_o = \frac{1}{2} R_{timescales}$ for an axi-symmetric vortex (see footnote on page 11). Is the Rossby number large or small and what does that tell us about the balance of forces that maintains the jet stream?

Mid-latitude cyclones — blizzards and Nor'easters. How long does it take for a parcel of air associated with a blizzard (or a mid-latitude cyclone) to travel full circle around the low pressure center? Use the same trajectory interface but set level = $5 \,\mathrm{km}$, $\sim 500 \,\mathrm{mb}$, the level that sets the speed of propagation of mid-latitude cyclones. Again, estimate the Rossby number and discuss the typical balance of forces in a large-scale blizzard.

Tropical cyclones — hurricanes. Repeat the same procedure but for hurricane Harvey (August, 2018). Use the Harvey winds available from the EsGlobe interface and set level =

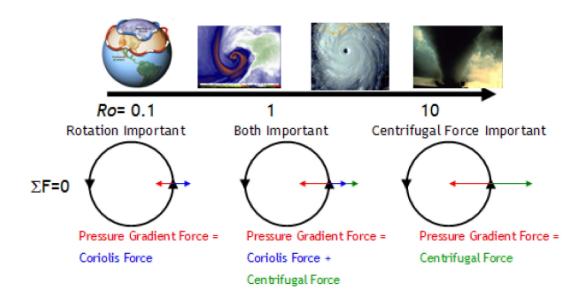


Figure 13: Significance of Rossby number as it relates to the balance of forces in vortices of different scales. On the planetary scale (lhs) $R_o \ll 1$ and pressure gradient forces are balanced by Coriolis forces. On the scale of a tornado (rhs) $R_o \gg 1$ and pressure gradient forces are balanced by centrifugal forces.

 $1 \,\mathrm{km}$, $\sim 850 \,\mathrm{mb}$, the level at which hurricane winds are the strongest. Estimate the Rossby number and discuss the typical balance of forces for a hurricane.

What about a tornado? Discuss the likely balance of forces.

In summary you should find that R_o depends on scale, broadly as sketched in Fig.13. On the large-scale, $R_o \ll 1$, and the dynamics is dominated by Earth's rotation, i.e. the Coriolis force. In this case the dominant radial force balance is given by Eq.(13). In contrast, if $R_o \gg 1$, then centrifugal forces acting on the fluid parcel are dominant. In this case the dominant radial force balance is given by Eq.(15). In each of these cases, the force directed radially-outwards from the center of the vortex (whether Coriolis or centrifugal) is balanced by the pressure gradient force directed inwards, toward the low pressure at the center.

3.3 Jet stream in Geostrophic balance

Use the EsGlobe Atmospheric climatology interface to plot the zonal component of the wind field at 250mb, together with the height of the 250mb surface. An example is shown in Fig.14 from a January climatology. The globe has been orientated so that the north pole (NP) is at the center of the plot. Note:

1. the wind blows from west to east, circling cyclonically (anti-clockwise, looking down

from the NP) around the pole. The reddest areas are the fastest, reaching speeds of $50\,\mathrm{m\,s^{-1}}$ or so.

- 2. the 250mb surface is low over the pole (a height of 9600 m or so) and gently rises moving in to the tropics (to a height of 10800 m or so).
- 3. since $R_o \ll 1$, the zonal flow is in geostrophic balance with the poleward-directed pressure gradient force and Eq.(13) pertains. Thus, rearranging,

$$v_{\theta} = \frac{g}{2\Omega} \frac{\partial h}{\partial r} \simeq \frac{g}{2\Omega} \frac{\Delta h}{\Delta r},$$

where Δh is the increase in the height of the 250mb surface moving outward from the pole, typically 1.5km and Δr is the lateral scale over which it occurs, typically 3000km or so. Plugging in numbers we obtain, including Earth's rotation rate and the acceleration due to gravity:

$$v_{\theta} = \frac{9.81 \,\mathrm{m \, s^{-2}}}{2 \times 7 \times 10^{-5} \,\mathrm{s^{-1}}} \frac{(10.8 - 9.6) \times 10^{3} \,\mathrm{m}}{3 \times 10^{3} \,\mathrm{km}} \simeq 30 \,\mathrm{m \, s^{-1}},$$

or so, of the same order as the observed zonal wind speed — see Fig.14(top).

Connections to our radial inflow experiment should be clear. The center of our bucket represents the NP, a region of low pressure, the tilt of the free surface of the water is analogous to the tilt of atmospheric pressure surfaces, and the anti-clockwise trajectories of the paper dots are analogous and the west to east winds of the jet stream.

3.4 Hurricane flow — balance of forces

We now consider hurricane flow in more detail. Following the notation of Fig. 6, v_{θ} is the azimuthal velocity and r is the distance from the center of the hurricane and the radial momentum equation for the hurricane is:

$$\frac{v_{\theta}^2}{r} = g \frac{\partial h}{\partial r} \underbrace{-f v_{\theta}}_{\text{Coriolis acc}^n} : \text{ gradient wind balance atmosphere}$$
 (17)

where $f = 2\Omega$ sinlat is the Coriolis parameter and h is the height of a constant pressure surface. Note the similarity with Eq.(11) for the tank experiment. The only difference is the dependence of f on latitude due to the sphericity of the Earth.⁴

⁴What matters on a rotating sphere is the rotation vector in the direction of gravity, i.e. $f = 2\Omega$ sinlat. Thus at the Pole the effect of rotation is at a maximum with $f = 2\Omega$, whilst it is exactly zero at the equator where $\Omega = 0$ and f = 0.

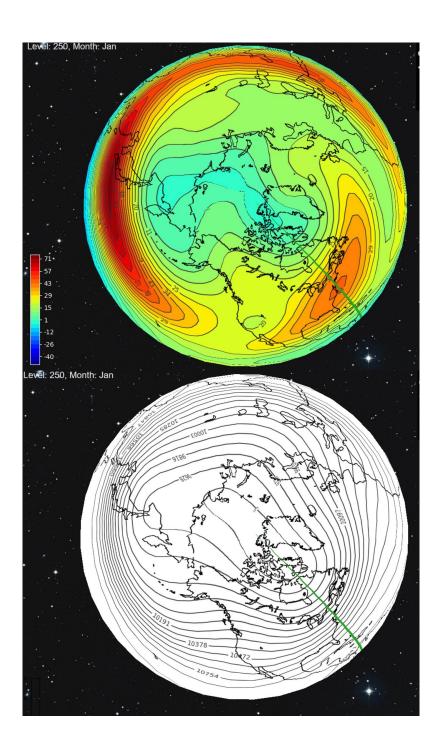


Figure 14: (top) The monthly-averaged January zonal (west to east) wind at 250mb, showing the jet stream. The north pole is in the center. Color scale on the left in $m\,s^{-1}$. Green and red colors indicate eastward flow. (bottom) The monthly-averaged January height of the 250mb surface in meters varying from a height of 9600m over the pole to 10800m over the equator.

Choose a hurricane and plot the observed winds, following the instructions in here: http://weatherclimatelab.mit.edu/scatterometer-instructions.

From the wind field compute the Rossby number defined as in Eq.(12) $R_o = \frac{|v_{\theta}|}{fr}$. How does R_o vary with radius? How does it compare to that observed in the tank experiment? Hence infer the balance of forces typical of an hurricane from the eye to the outer edge.